

Nonreciprocal Phenomena in Chiral Materials

- Left and Right in Quantum Dynamics -

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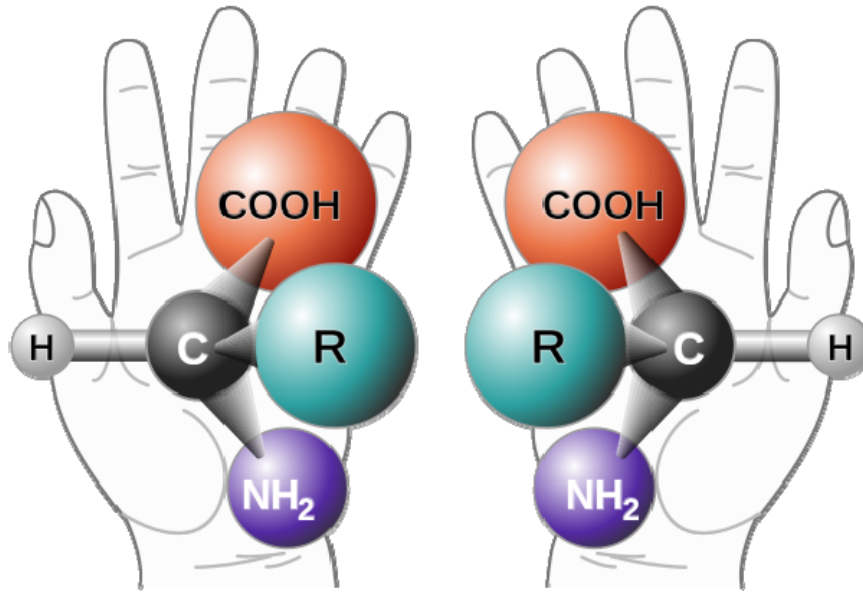
Collaborators

U.Tokyo: Ryohei Wakatsuki, Keita Hamamoto,
Hiro Ishizuka, Motohiko Ezawa

Saitama Univ.: Shintaro Hoshino

Exp: Y. Tokura, Y. Iwasa, K.S. Takahashi, K. Yasuda,
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T. Ideue, H. Yasuda, R. Yoshimi

Left and Right (chirality) is a crucial issue in sciences



No Inversion I
No Mirror M

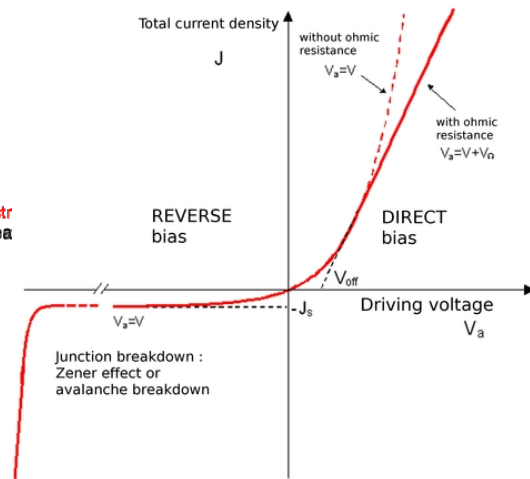
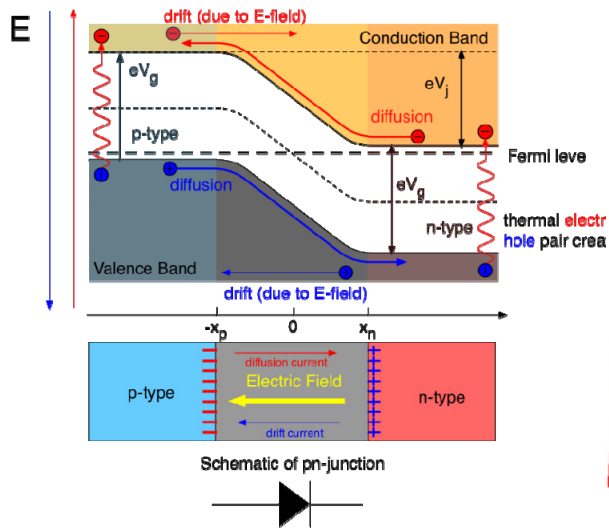
From Wikipedia

Physics	parity violation of weak interaction
Chemistry	chiral molecules
Biology	chirality of DNA

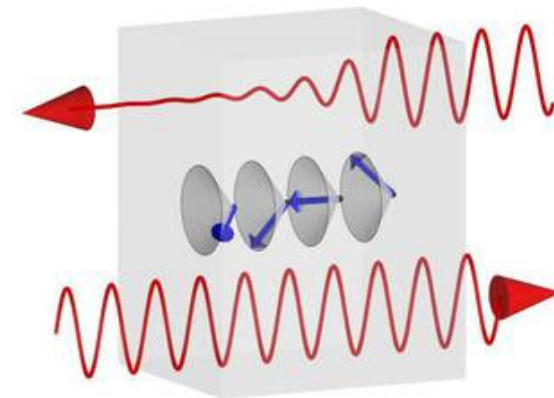
M. Gardner, *The Ambidextrous Universe. Left, Right and the Fall of Parity*,
Basic Books Inc. (1964)

Directional response is useful

pn junction



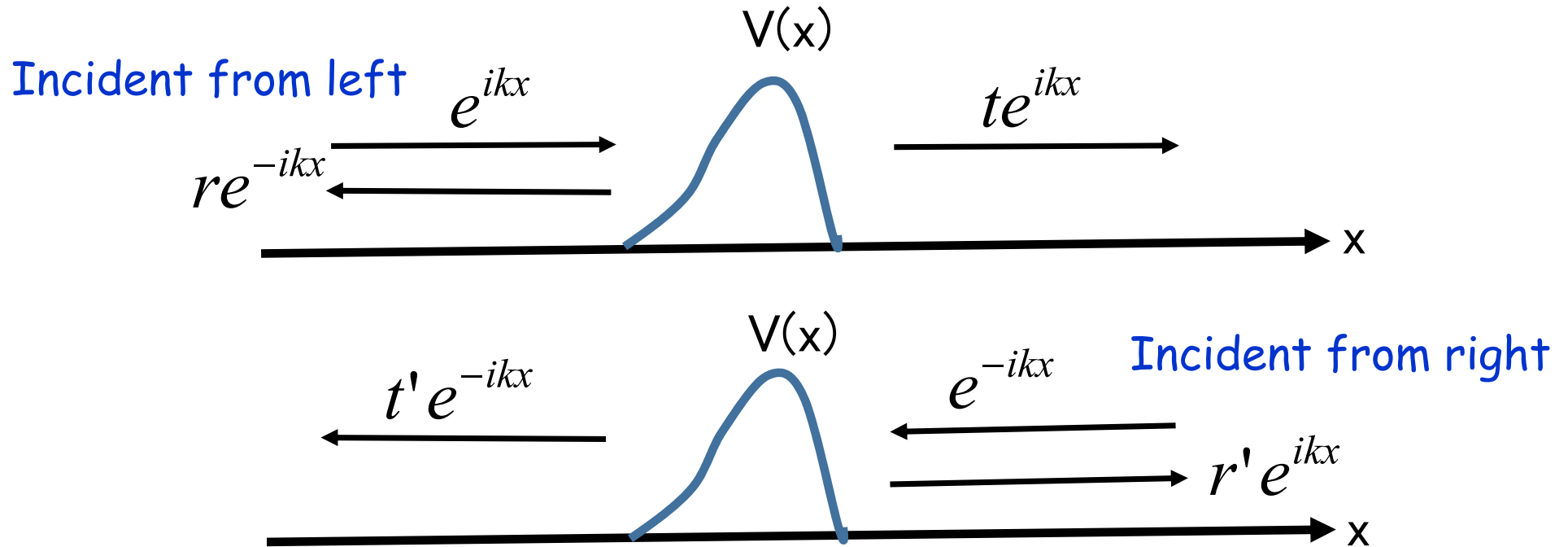
optical isolator



<http://quantumwise.com/publications/tutorials/item/828-silicon-p-n-junction>

http://www.optique-ingenieur.org/en/courses/OPI_ang_M05_C02/co/Contenu_09.html

Fundamental viewpoint from physics Right and Left directions of flow



$$|t'|^2 = |t|^2$$

$$|r'|^2 = |r|^2$$

$$t' = t$$

Unitary nature of S matrix: conservation of prob.

➔ Role of dissipation and classical nature

Time-reversal symmetry T : $S = S^{\wedge} \text{Transpose}$

Asymmetry between t and $-t$

1. Microscopic time-reversal symmetry breaking

external magnetic field B
magnetic ordering M

2. Macroscopic irreversibility

dissipation of energy
diffusion

Non-reciprocal transport in non-centrosymmetric system

Time-reversal symmetry of microscopic dynamics vs irreversibility

$$\sigma_{\mu\nu}(k, \omega, B) = \sigma_{\nu\mu}(-k, \omega, -B)$$

Onsager's reciprocal relation
for linear response

Magneto-chiral optical effect
directional dichroism

$\varepsilon_{\mu\mu}(k, \omega, B) = \varepsilon_0 + \alpha k \cdot B$
e.g. electromagnon in multiferroics
A. Loidl, Y. Tokura

$k \rightarrow I$ G. L. J. A. Rikken (2001)

"dichroism" of the electric current

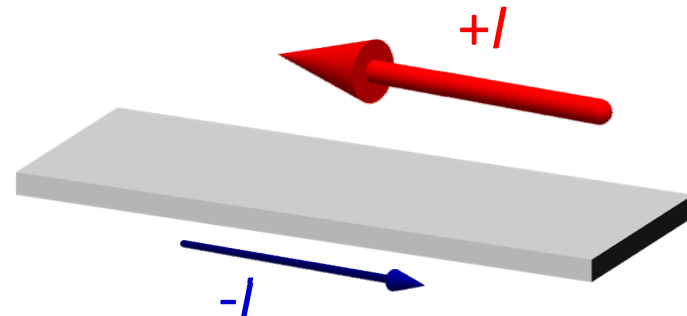
magneto-chiral anisotropy

$$R(+I) \neq R(-I)$$

$$R = R_0 (1 + \beta B^2 + \gamma BI)$$

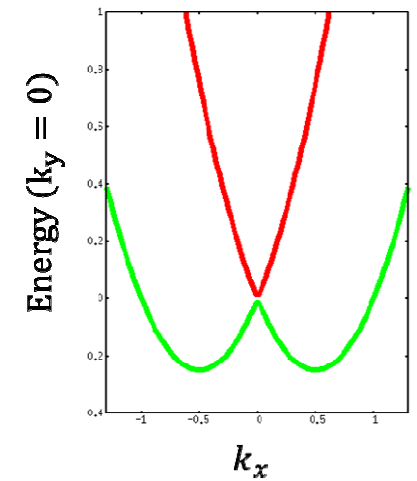
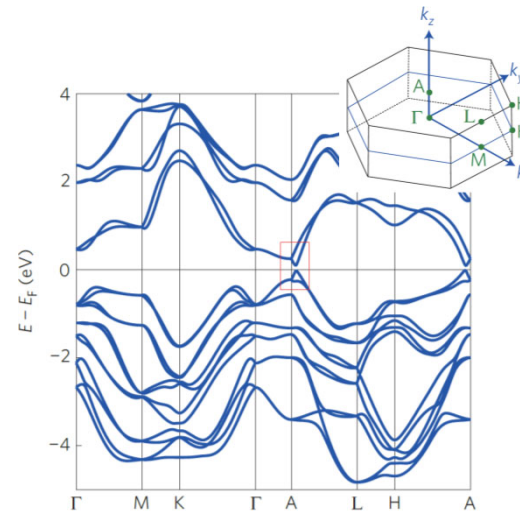
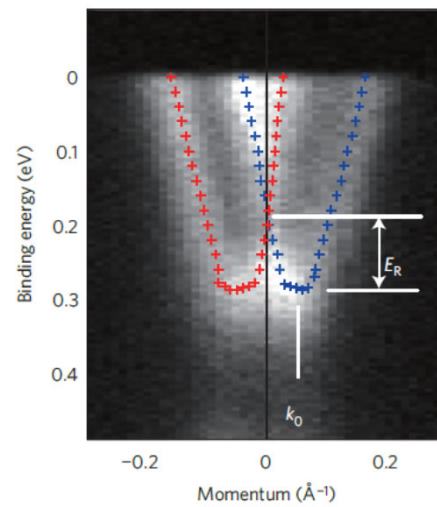
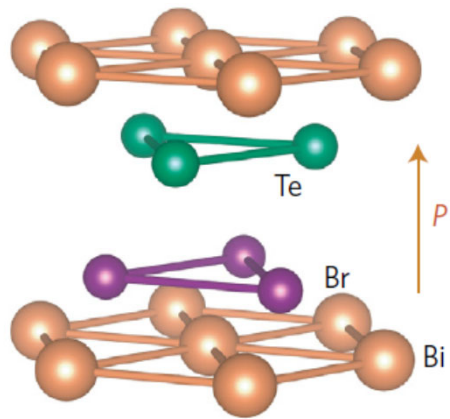
Broken inversion symmetry $\Leftrightarrow \gamma \neq 0$

Nonlinear response $J = \sigma E + \alpha B E^2$



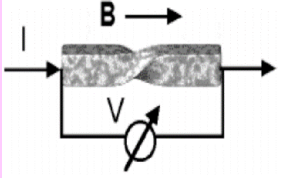
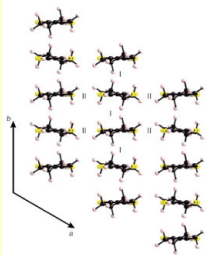
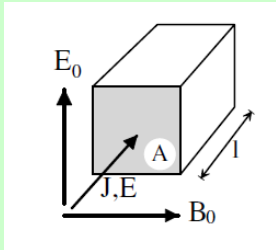
Band structure in noncentrosymmetric crystal

Time-reversal symmetry $\rightarrow \varepsilon_{\uparrow}(k) = \varepsilon_{\downarrow}(-k)$



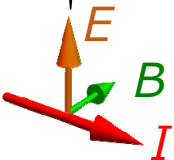
K. Ishizaka *et al.* *Nat. Mater.* **10**, 521 (2011).

Magneto-chiral anisotropy - tiny effect

	Bi helices	Organics	Si FET
	 <p>G. L. J. A. Rikken et al. <i>PRL</i> 87, 236602 (2001).</p>	 <p>F. Pop et al. <i>Nat. Commun.</i> 5, 3757 (2014).</p>	 <p>G. L. J. A. Rikken et al. <i>PRL</i> 94, 016601 (2005).</p>
$\gamma (T^{-1}A^{-1})$	10^{-3}	10^{-2}	10^{-1}

$$\gamma \sim 10^4 T^{-1} A^{-1}$$

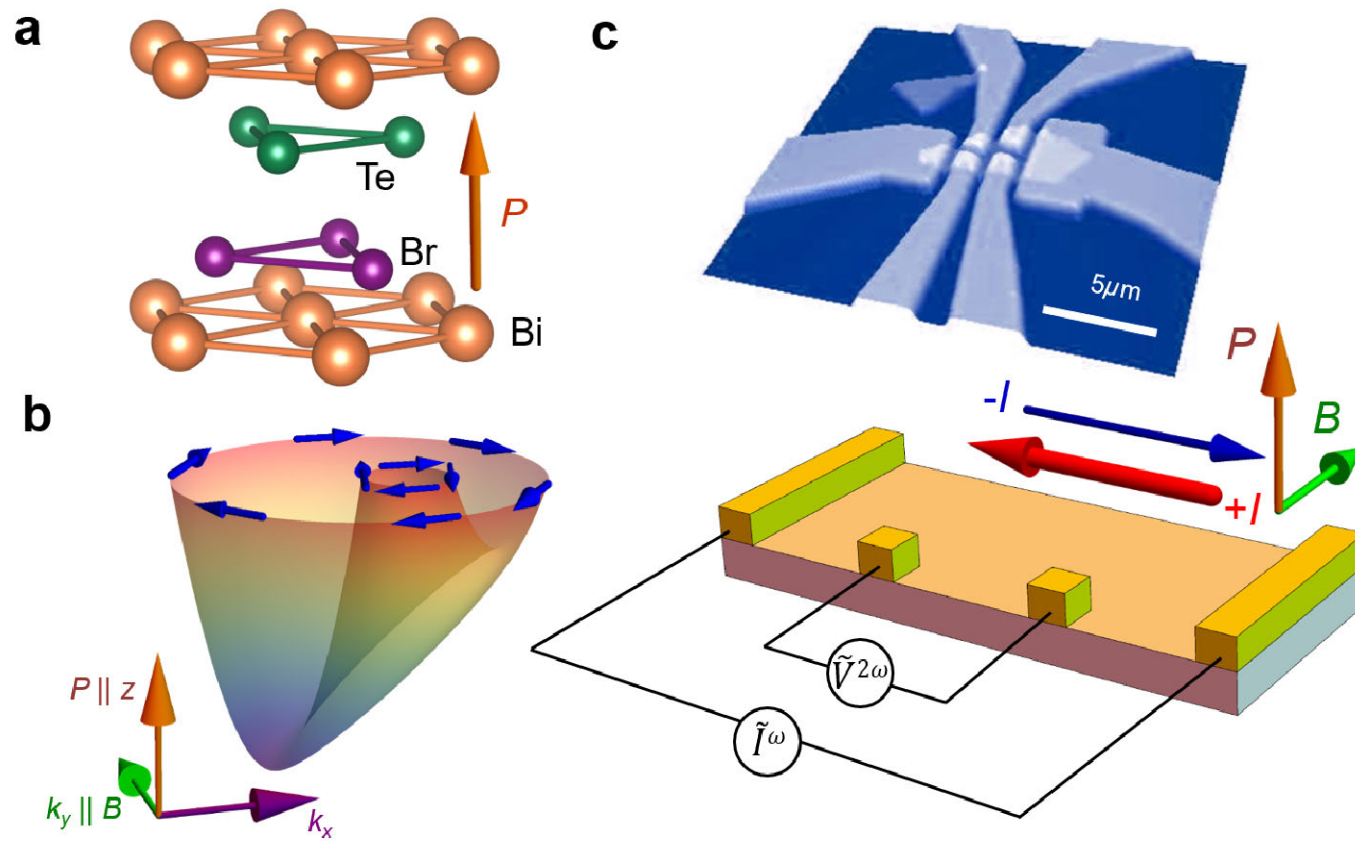
$$R = R_0 (1 + \beta B^2 + \gamma BI)$$



$$\mu_B B, \epsilon_{SOI} \ll \epsilon_F$$

Enhanced magnetochiral anisotropy in BiTeBr

Y.Iwasa *G*, Y.Tokura *G*, NN *G* Nature Phys. 2017



Magneto-chiral anisotropy in Rashba model

K. Hamamoto

$$H = \frac{k_z^2}{2m_{\parallel}} + \frac{k_x^2 + k_y^2}{2m_{\perp}} + \lambda(k_x\sigma_y - k_y\sigma_x) - B_y\sigma_y$$

Boltzmann equation

$$-e\mathbf{E} \cdot \frac{\partial f}{\partial \mathbf{k}} = -\frac{1}{\tau}(f - f_0)$$

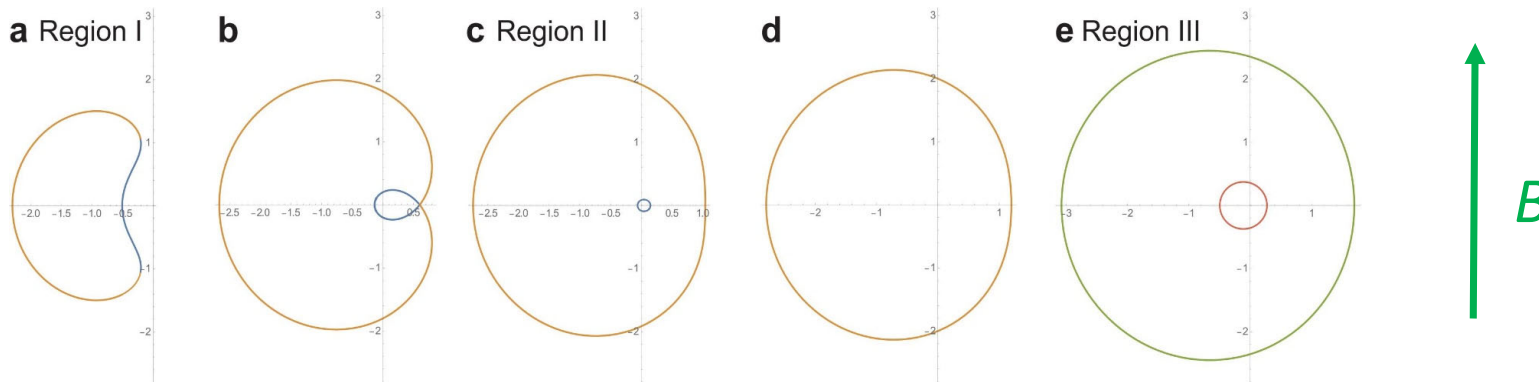
Expand in E

$$f = f_0 + f_1 + f_2 + \dots,$$

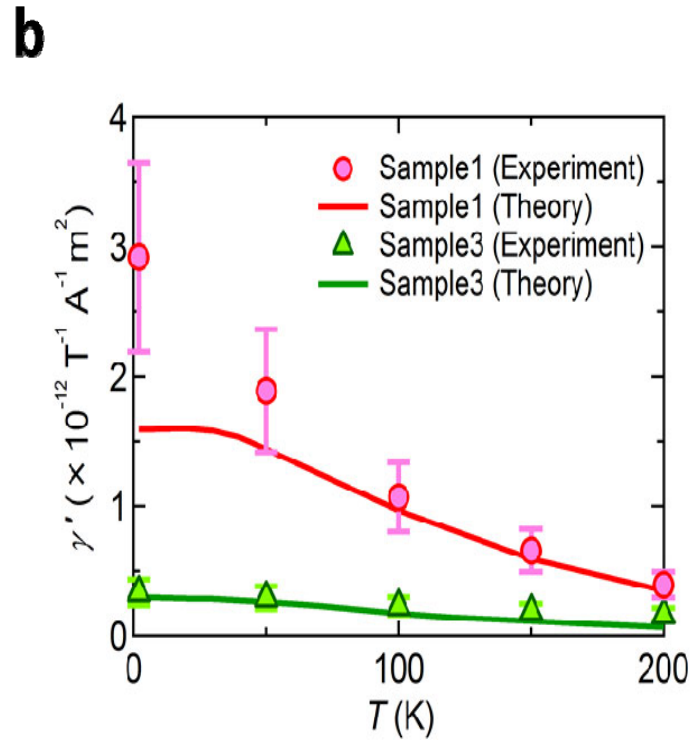
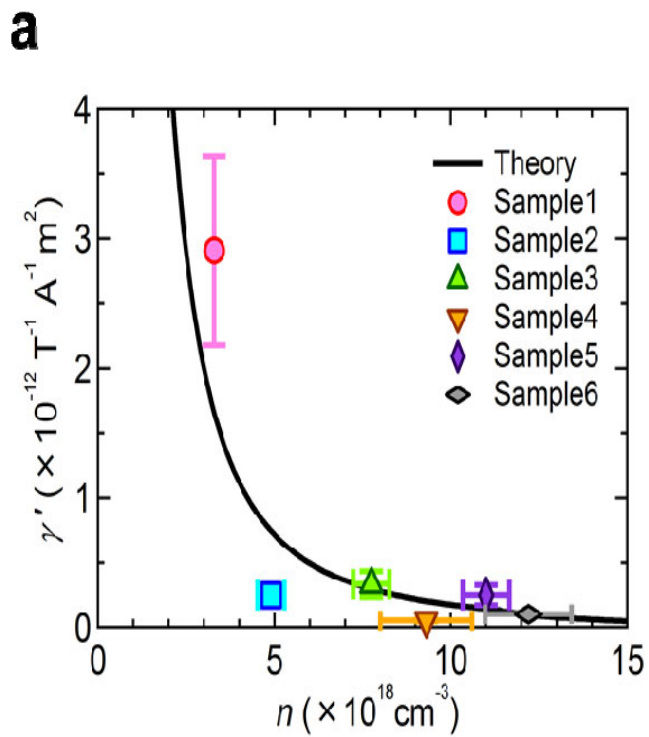
$$J_x = J_x^{(1)} + J_x^{(2)} = \sigma_1 E_x + \sigma_2 E_x^2$$

γ is independent of τ in the single relaxation time approx. like Hall coefficient

γ diverges as $n \rightarrow 0$ increasing Fermi energy γ is zero when two FSs coexist



No fitting parameters !



$$\gamma \sim 1T^{-1} A^{-1}$$

$$\gamma' = \gamma A \quad A \text{ cross section of the sample}$$

Chiral anomaly in Weyl semimetals

X. Huang et al., PRX 2015

$$\frac{dQ^5}{dt} = \frac{2\nu}{(2\pi)^2} \frac{e^2}{\hbar^2} \mathbf{E} \cdot \mathbf{B}$$

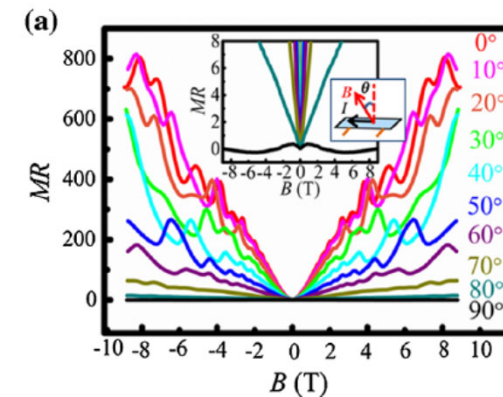
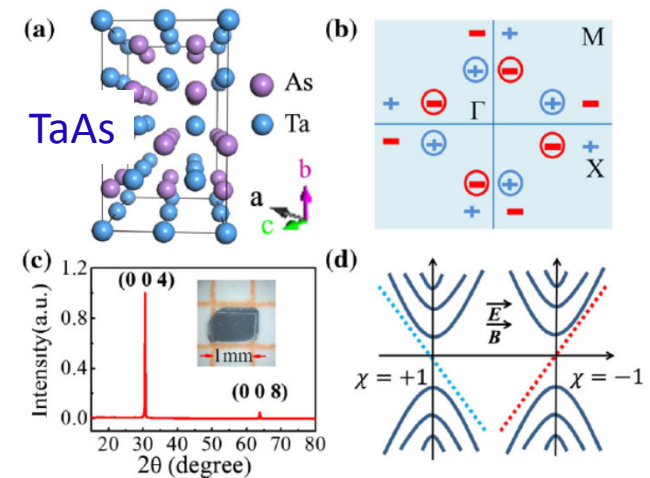
$$Q^5 = \frac{\nu e^2 \tau}{4\pi^2 \hbar^2} \mathbf{E} \cdot \mathbf{B}$$

$$\mathbf{J} = -(e^2/h^2)\mu^5 \mathbf{B}$$

μ_5 chemical potential difference
in non-equilibrium steady state

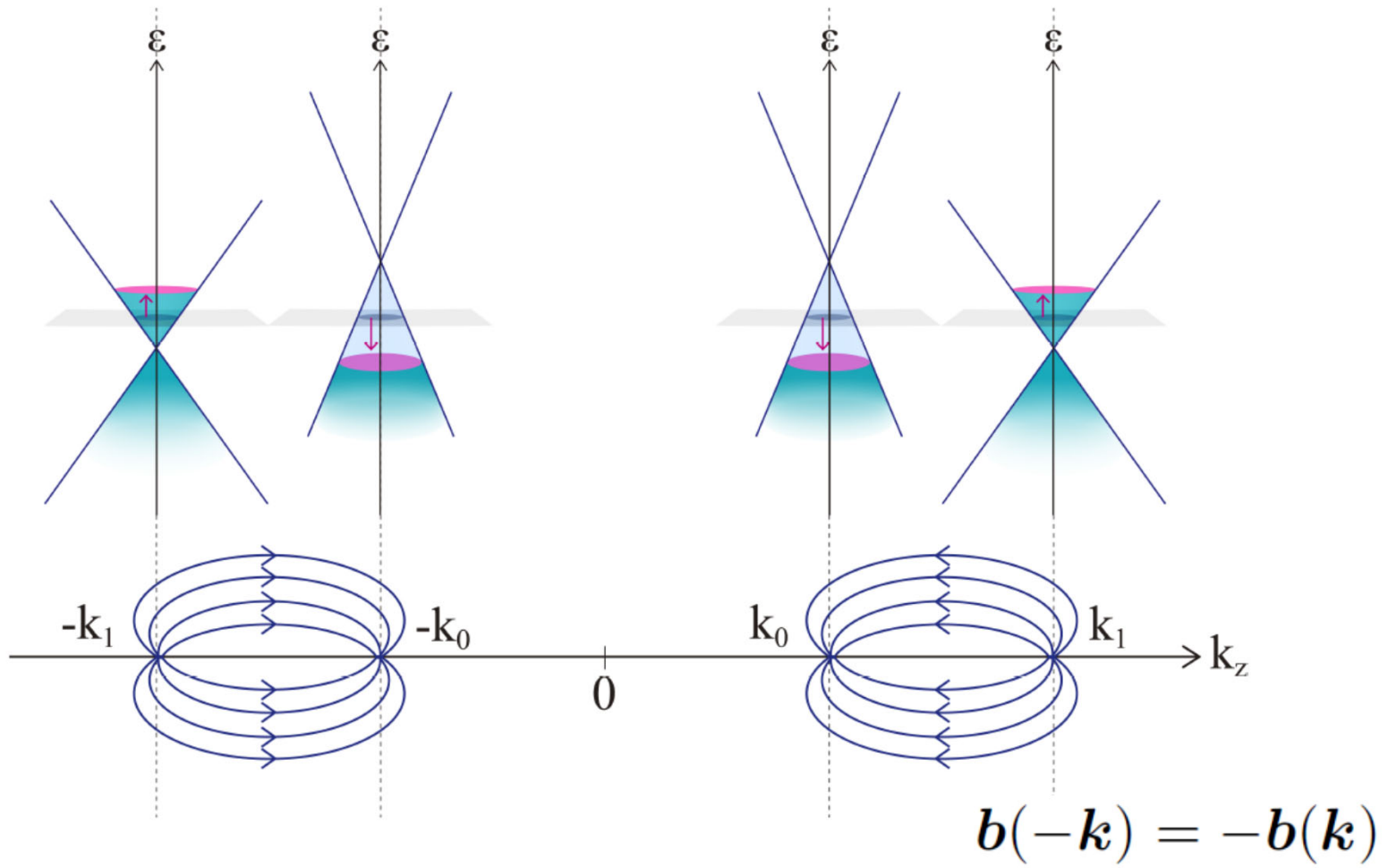
$$\Delta J \propto \tau(\mathbf{B} \cdot \mathbf{E})B$$

K. Fukushima, D. Kharzeev



negative magnetoresistance
due to chiral anomaly

Weyl fermions in noncentrosymmetric semimetals



Magneto-chiral anisotropy in noncentrosymmetric Weyl semimetals

T. Morimoto, NN PRL2016

$$\Delta\sigma_{\pm} = \frac{1}{3}e^2v_{\pm}^2\tau \frac{dD_{\pm}(\epsilon)}{d\epsilon} \Delta\epsilon_{\pm}$$

$$\Delta\sigma_{\pm} = \pm\nu \frac{e^4}{6\pi^2\hbar^2} \frac{v_{\pm}^2\tau^2}{\epsilon_{\pm}} \mathbf{E} \cdot \mathbf{B}.$$

$$\rho = \rho_0(1 + \gamma \mathbf{I} \cdot \mathbf{B})$$

$$\gamma' = -\frac{2\delta\sigma/(\mathbf{E} \cdot \mathbf{B})}{\sigma^2}$$

$$\gamma' = \gamma A$$

$$= -\frac{12\pi^2\hbar^4}{\nu} \left(\frac{v_+^2}{\epsilon_+} - \frac{v_-^2}{\epsilon_-} \right) \left(\frac{\epsilon_+^2}{v_+} + \frac{\epsilon_-^2}{v_-} \right)^{-2}$$

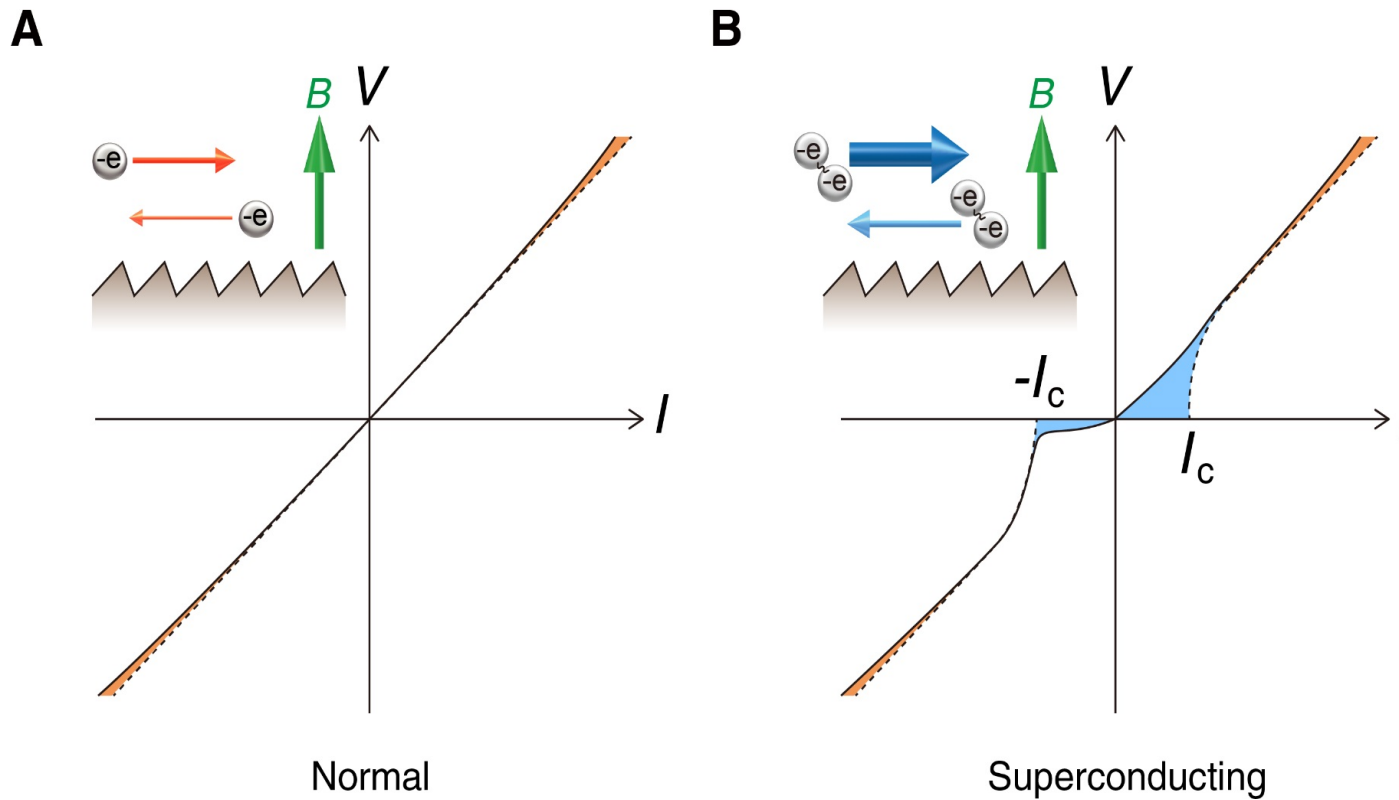
$$v \sim 4 \times 10^5 \text{ m/sec} \quad |\epsilon_{\pm}| \sim 10 \text{ meV} \quad \Rightarrow \quad \gamma' \simeq 3 \times 10^{-8} \times \text{m}^2 \text{T}^{-1} \text{A}^{-1}$$

$$\gamma \sim 10 \text{ T}^{-1} \text{A}^{-1} \quad \text{TaAs}$$

$$\gamma' \mathbf{J} \cdot \mathbf{B} \simeq 3 \times 10^{-4} \times (J/(1 \text{ A/cm}^2))(B/1 \text{ T})$$

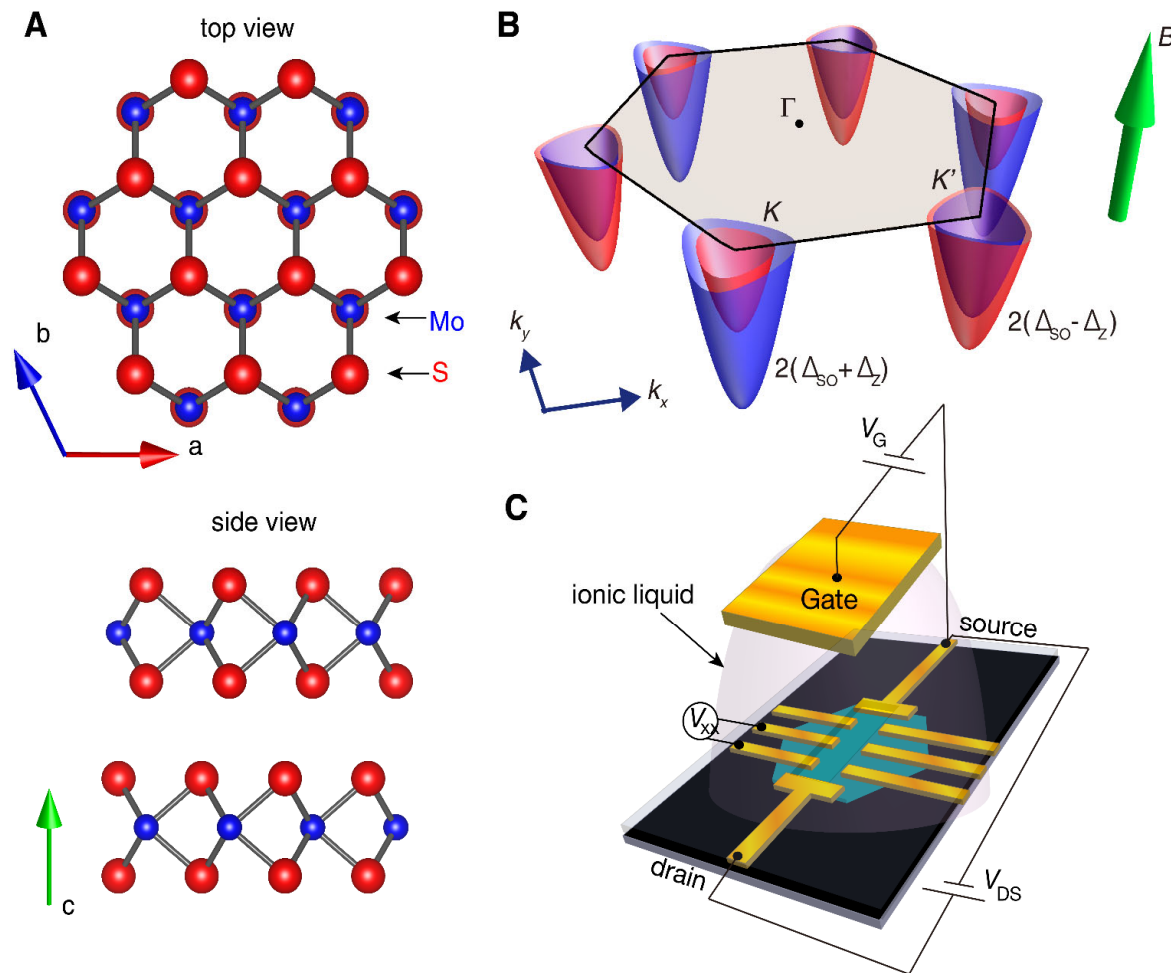
Giant enhancement of non-reciprocal response in superconductor

Wakatsuki, Saito et al. Science Adv. 2017



$$\Delta_{SC} \sim \mu_B B, \quad \epsilon_{SOI} \ll \epsilon_F$$

Band structure and spin splitting in MoS₂



Paraconductivity due to SC fluctuation in noncentrosymmetric MoS2

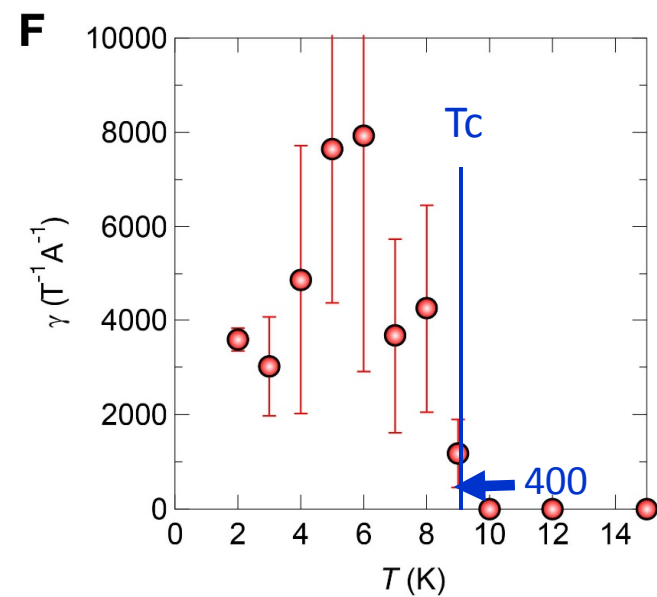
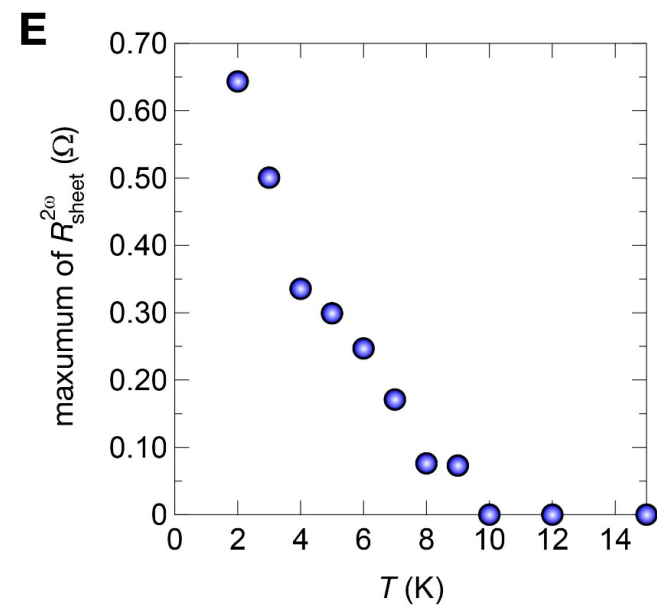
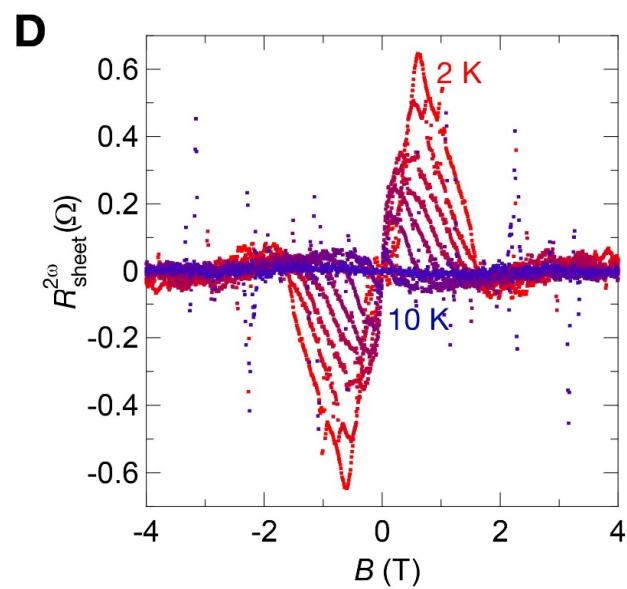
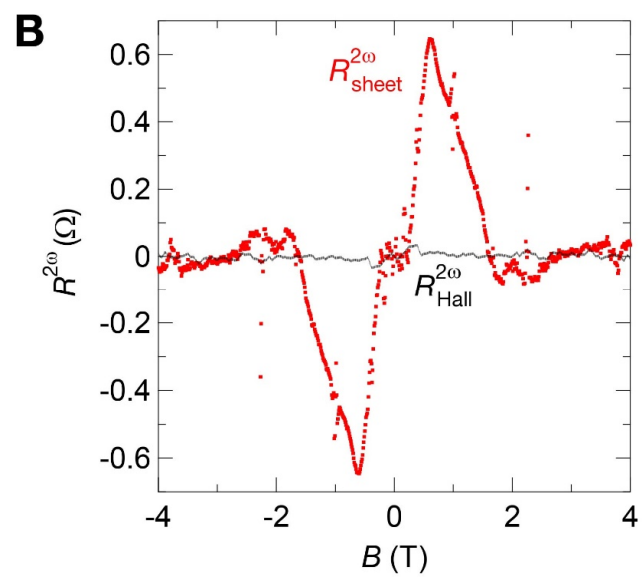
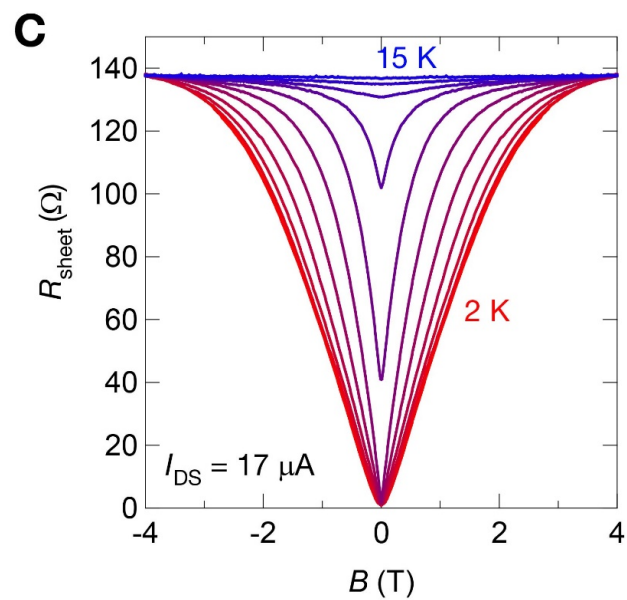
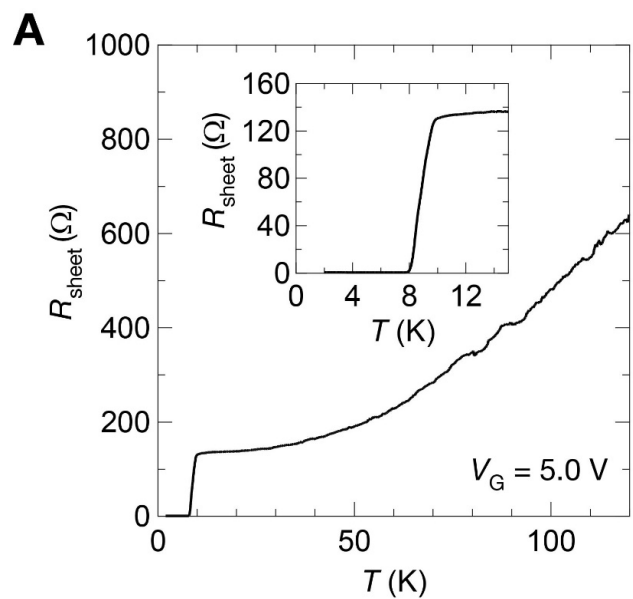
$$H_{k\sigma\tau} = \frac{\hbar^2 k^2}{2m} + \tau_z \lambda k_x (k_x^2 - 3k_y^2) - \Delta_Z \sigma_z - \Delta_{SO} \sigma_z \tau_z,$$

$$F = \int d\mathbf{r} \Psi^* \left[a + \frac{\mathbf{p}^2}{4m} + \frac{\Lambda B}{\hbar^3} (p_x^3 - 3p_x p_y^2) \right] \Psi + \frac{b}{2} \int d\mathbf{r} |\Psi(\mathbf{r})|^4,$$

$$\Lambda = \frac{93\zeta(5) g \mu_B \Delta_{SO} \lambda}{28\zeta(3) (\pi k_B T_c)^2}$$

$$\mathbf{j} = \frac{e^2}{16\hbar} \epsilon^{-1} \mathbf{E} - \frac{\pi e^3 m \Lambda B}{64 \hbar^3 k_B T_c} \epsilon^{-2} \mathbf{F}(\mathbf{E}) \quad \longrightarrow \quad \frac{\gamma_S}{\gamma_N} \sim \left(\frac{\epsilon_F}{k_B T_c} \right)^3$$

$$\epsilon = \frac{T - T_c}{T_c} \quad \mathbf{F}(\mathbf{E}) = (E_x^2 - E_y^2, -2E_x E_y)$$



		Rashba SC ($B \perp \hat{z}$)	TI surface + SC ($B \perp \hat{z}$)	TMD ($B \parallel \hat{z}$)
Symmetry		C_∞		Hexagonal
		$V = a_1 I(1 + \gamma_N BI)$		
$T > T_0$	Normal	[Sec. II A] $\gamma_N = 0$ ($E_F > 0$) $\gamma_N \sim \frac{\alpha}{e(m\alpha^2 E_{FR})^{3/2}}$ ($E_F < 0$)	[Sec. II B 1] $\gamma_N \sim \frac{\text{sgn } E_F}{emv_F E_F^2}$	[Sec. II B 2] $\gamma_N \sim \frac{ E_F \lambda}{ev_F^5}$
	Paraconductivity	Parity mixing ($E_F > 0$) $\gamma_S \sim \frac{r_{t,s} E_F \alpha}{eT_0^3 E_{FR} \ln(E_c/T_0)}$ q -cubic term ($E_F < 0$) $\gamma_S \sim \frac{1}{em\alpha E_{FR} T_0}$	$\gamma_S \sim \frac{1}{emv_F E_F T_0}$	$\gamma_S \sim \frac{E_F^2 \lambda}{ev_F^5 T_0}$
		$V = a_1 I(1 + \gamma_S BI)$		
$T < T_0$	KT transition		No KT transition	
	$T_{KT} < T < T_0$	[Sec. III A] $V = a_1 I(1 + \gamma_S BI)$ $\gamma_S \sim (T_0 - T)^{-1}$ ($T \rightarrow T_0$) $\gamma_S \sim (T - T_{KT})^{-3/2}$ ($T \rightarrow T_{KT}$)	Viscous vortex flow [Sec. III A,B] $V = a'_1 BI(1 + \gamma_S BI)$ $\gamma_S \sim \frac{m\Delta_{SO}\lambda}{eT_0 E_F (T_0 - T)}$	
	$T < T_{KT}$	$V = a_3 I^3 + a'_4 BI^4$		Ratchet mechanism [Sec. III C] $V = a'_1 BI(1 + \gamma'_S I)$

S. Hoshino et al. 2018

$\frac{1}{emv_F E_F T_0}$	$\gamma_S \sim \frac{E_F^2 \lambda}{ev_F^5 T_0}$	$\gamma_S \sim \frac{m\Delta_{SO}\lambda}{eT_0^3}$
on	No KT transition	
[Sec. III A] $a_1 I(1 + \gamma_S BI)$ $(T \rightarrow T_0)^{-1}$ $(T \rightarrow T_{KT})^{-3/2}$	<i>Viscous vortex flow</i> [Sec. III A,B] $V = a'_1 BI(1 + \gamma_S BI)$ $\gamma_S \sim \frac{m\Delta_{SO}\lambda}{eT_0 E_F (T_0 - T)}$	
$a_3 I^3 + a'_4 BI^4$	<i>Ratchet mechanism</i> [Sec. III C] $V = a'_1 BI(1 + \gamma'_S I)$	

S. Hoshino et al. 2018

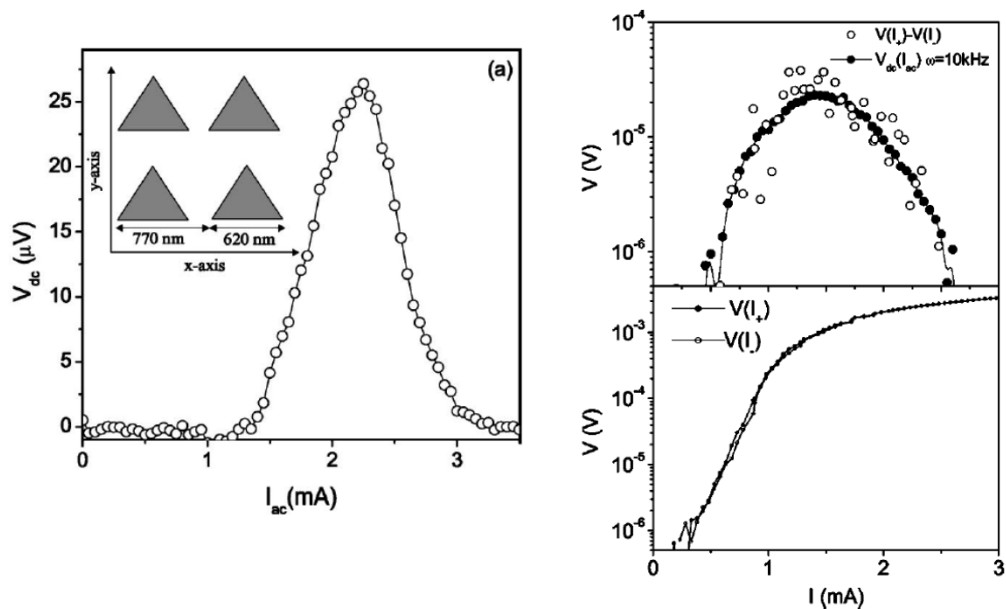
Number of vortices
Dissipative dynamics
of vortices

Ratchet motion of vortex and nonreciprocal transport

PHYSICAL REVIEW B 71, 024519 (2005)

Experimental ratchet effect in superconducting films with periodic arrays of asymmetric potentials

J. E. Villegas,¹ E. M. Gonzalez,¹ M. P. Gonzalez,¹ J. V. Anguita,² and J. L. Vicent¹



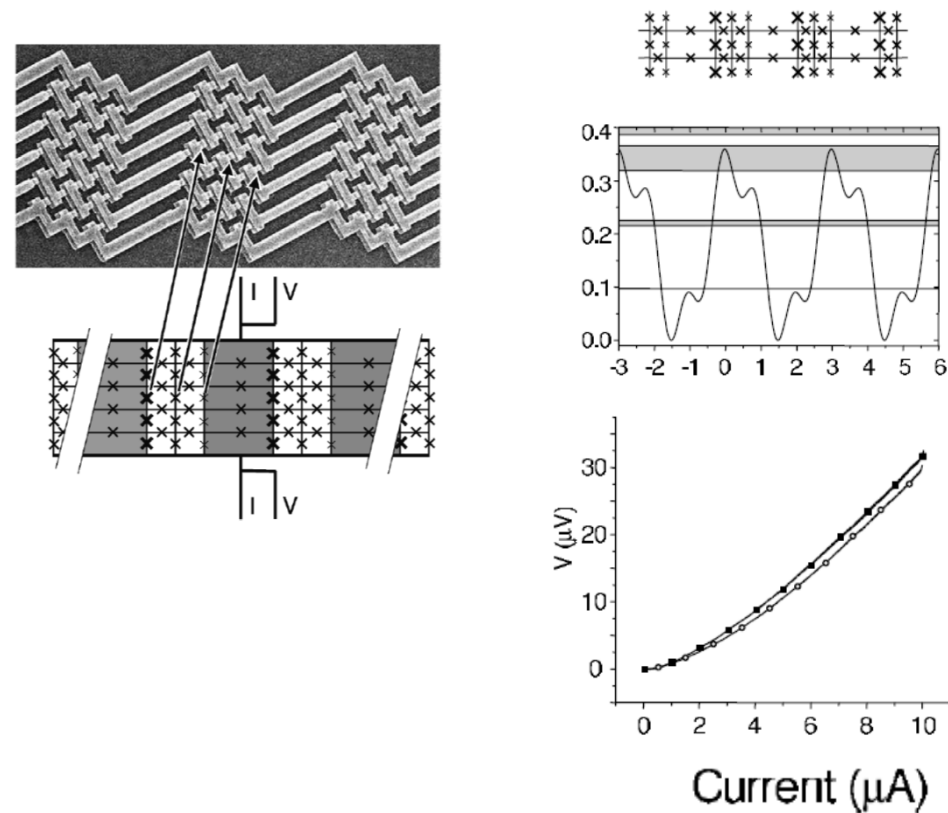
VOLUME 90, NUMBER 5

PHYSICAL REVIEW LETTERS

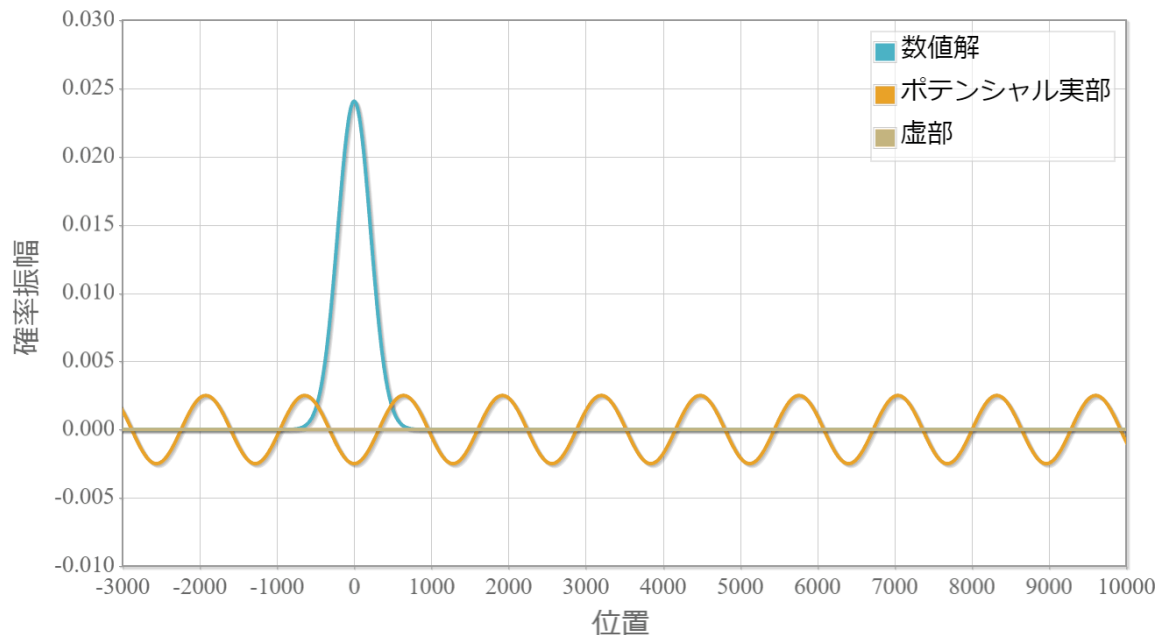
week ending
7 FEBRUARY 2003

Quantum Ratchet Effect for Vortices

J. B. Majer, J. Peguiron, M. Grifoni, M. Tussveld, and J. E. Mooij



A quantum particle in periodic potential



Quantum dissipation
by coupling to heat bath

$$\hat{\mathcal{H}} = \frac{P^2}{2M} + V(q) + \sum_{\alpha} \frac{P_{\alpha}^2}{2m_{\alpha}} + \frac{1}{2} \sum_{\alpha} m_{\alpha} \omega_{\alpha}^2 (x_{\alpha} + q \lambda_{\alpha} / m_{\alpha} \omega_{\alpha}^2)^2$$

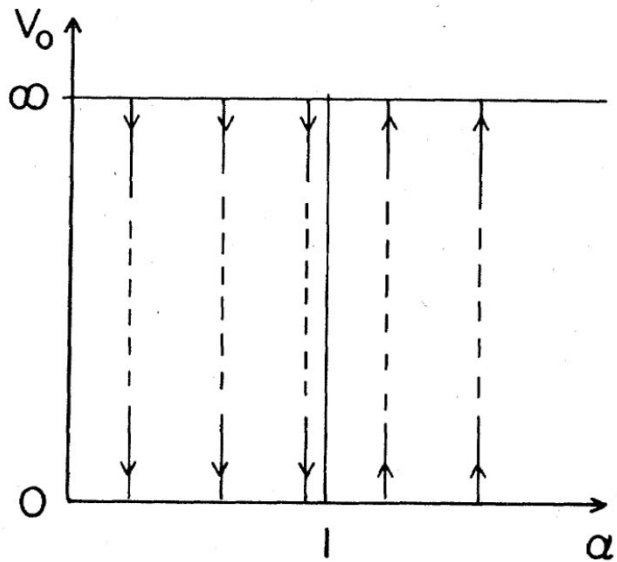
$$V(q) = -V \cos(2\pi q / q_0) - Fq$$

<http://www.natural-science.or.jp/article/20180529143612.php>

RG study

$$H = \frac{1}{2} \int \frac{d\omega}{2\pi} S_{\Lambda}(\omega) |\phi(\omega)|^2 - V_0 \Lambda \int d\tau \cos\phi(\tau)$$

$$S_{\Lambda}(\omega) = \frac{\alpha}{2\pi} |\omega| + \frac{\omega^2}{\Lambda} \quad \alpha \text{ dimensionless dissipation strength}$$



$$\frac{\partial V_0}{\partial l} = - \left[\frac{1}{\alpha} - 1 \right] V_0(l) + O(V_0^3)$$

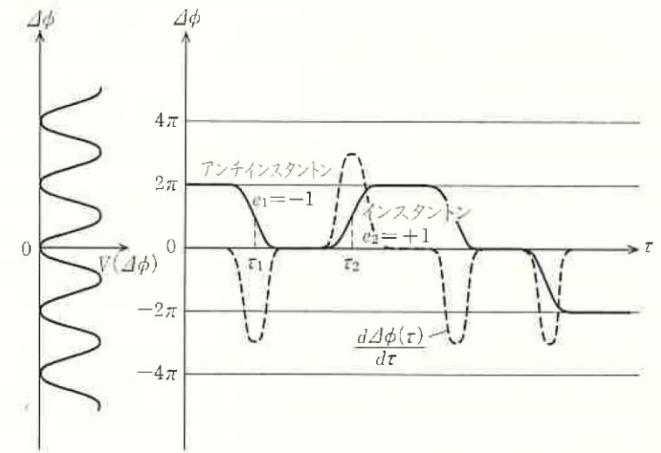
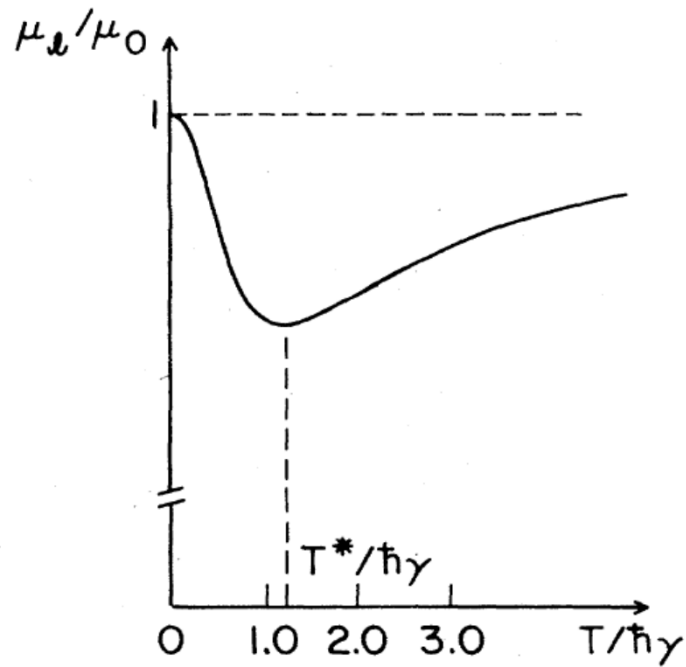


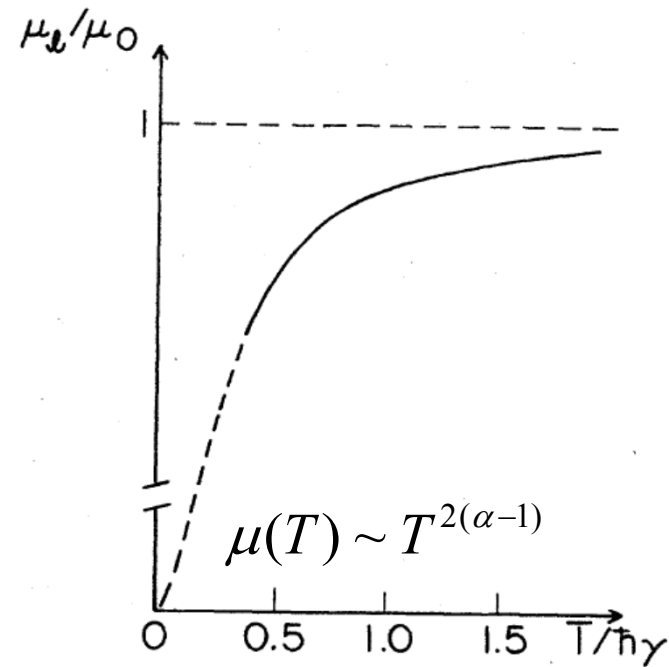
図5-4 インスタントン, アンチインスタントンを含んだ配置

duality $\alpha \rightarrow 1/\alpha$

Linear Mobility



$\alpha < 1$



$\alpha > 1$

Fisher-Zwerger PRB1985
Furusaki-Nagaosa PRB1993
Kane-Fisher PRB1992

Summary

- Non-linear and non-reciprocal responses in nontrosymmetric systems contain rich physics
- Time-reversal symmetry breaking plays an important role
- Magneto-chiral anisotropy
 - dissipation
 - quantum-classical crossover
 - duality between bosons and vortices

Symmetry Quantum Geometry Electron Correlation Irreversibility

For a review see [Y.Tokura, N.Nagaosa, Nature Communications 2018](#)