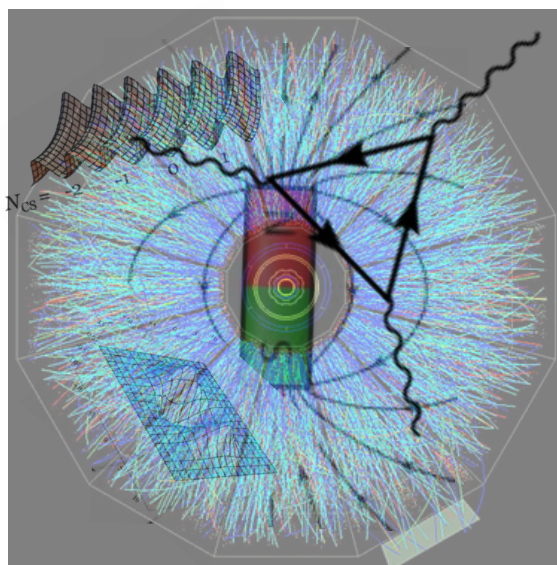


Novel Quantum Phenomena in the Subatomic Swirls



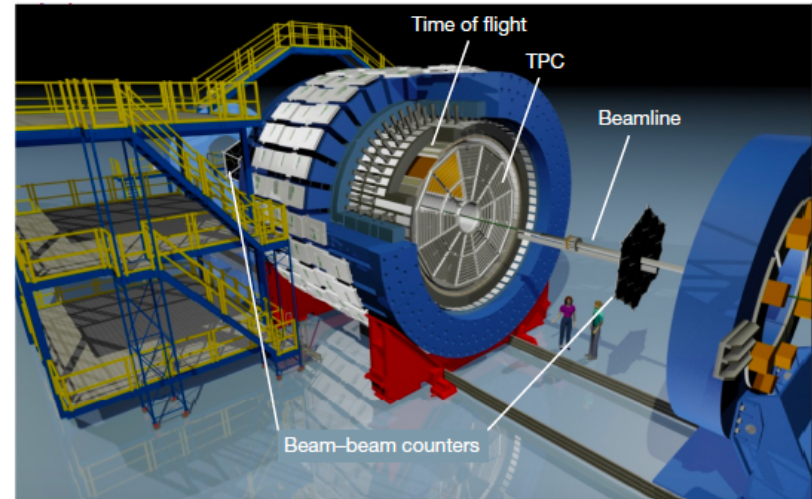
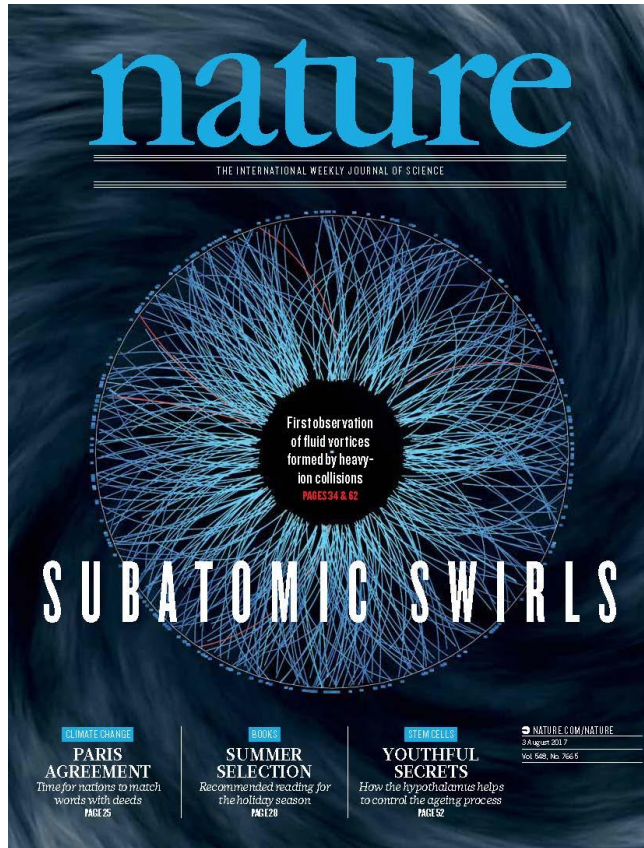
Jinfeng Liao

Indiana University, Physics Dept. & CEEM

Research Supported by NSF & DOE



The Subatomic Swirls



*An exciting discovery from
STAR Collaboration at RHIC:
The most vortical fluid!*

LETTER

doi:10.1038/nature23004

Global Λ hyperon polarization in nuclear collisions

The STAR Collaboration*

Introduction

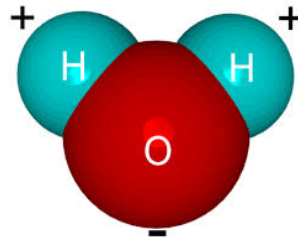
Nuclear Physics: Exploring the Heart of Matter

The physical world has a hierarchy of structures.

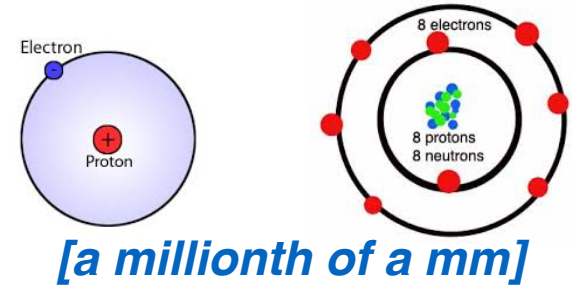
matter



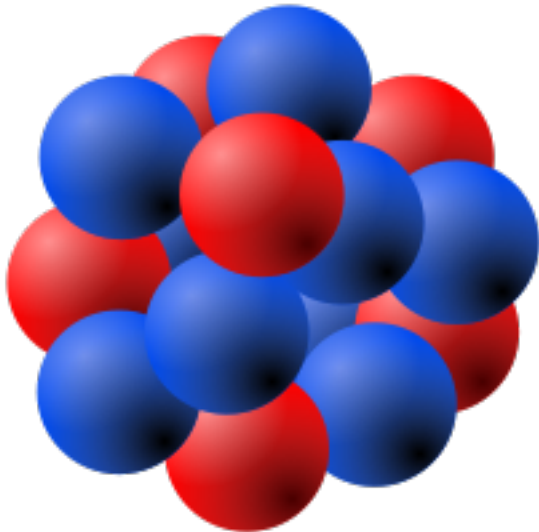
molecule



atoms

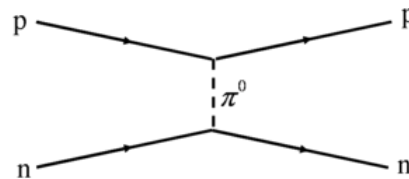
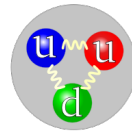


atomic nucleus

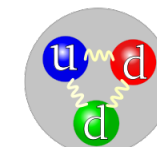


[a trillionth of a mm]

proton

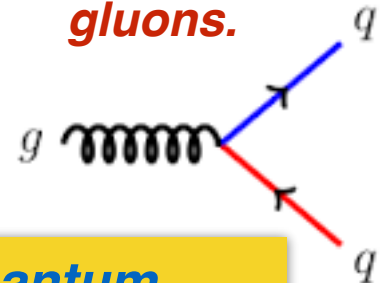


nuclear force



neutron

**Most basic entities:
quarks
and
gluons.**



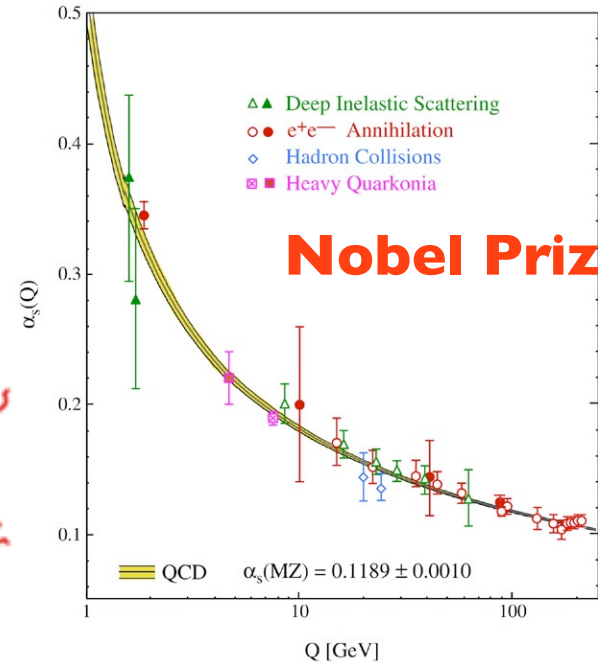
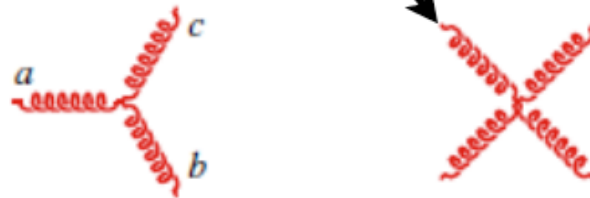
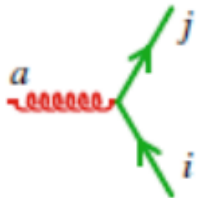
Quantum Chromodynamics (QCD)

Quantum Chromodynamics (QCD)

*The fundamental theory of strong nuclear force:
QCD, a non-Abelian gauge theory of quarks and gluons*

$$\mathcal{L} = \bar{\psi}(i\partial - M - g\mathcal{A}_a G^a)\psi - \frac{1}{4}F_a^{\mu\nu} F_{\mu\nu}^a$$

$$F_a^{\mu\nu} = \partial^\mu A_a^\nu - \partial^\nu A_a^\mu - g f_{abc} A_b^\mu A_c^\nu$$



*Asymptotic Freedom: coupling becomes large
at low energy or long distance scale.*

$$\Lambda_{QCD} \sim 200\text{MeV} \quad R \sim 1\text{ fm}$$

QCD Confinement: “The Missing Particles”

Free Quark Searches

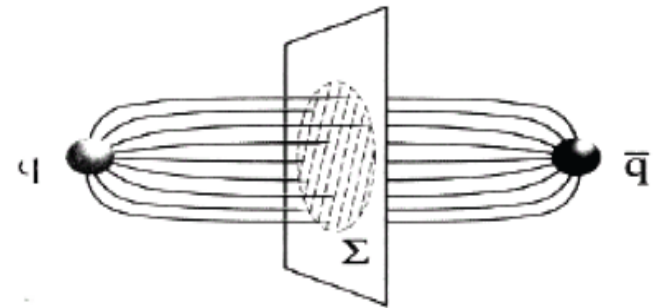
from Particle Data Group

All searches since 1977 have had negative results.

This null result is by itself a remarkable FACT of Nature.

Confinement problem:
Biggest challenge within Standard Model!

Mathematics: one of the seven
Millennium Problems!

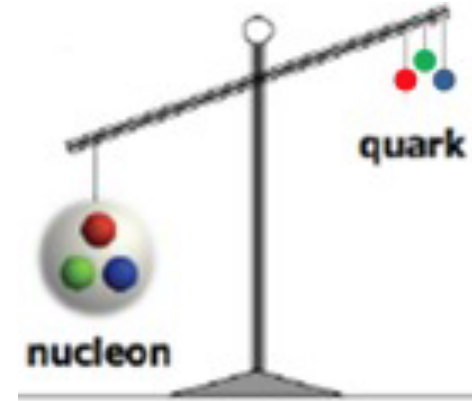
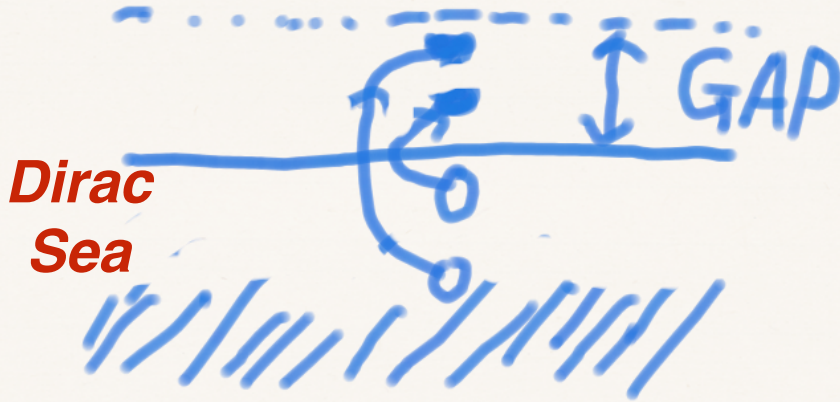


QCD dipole field

***QCD vacuum as “dual superconductor” with dual Meissner effect?
Color-magnetic topological condensate?***

Chiral Symmetry: Spontaneous Breaking

$$m_\pi \approx 140 \text{ MeV}, m_n \approx 940 \text{ MeV}$$



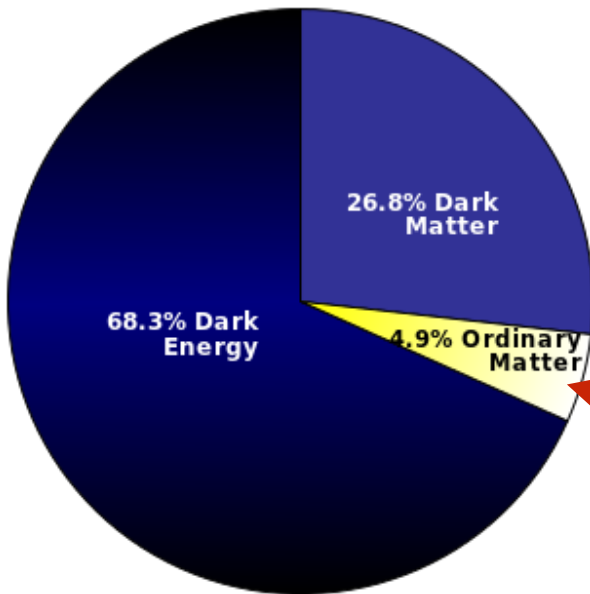
$$M = m - 2G \langle \bar{\psi}\psi \rangle$$

*Constituent
mass*

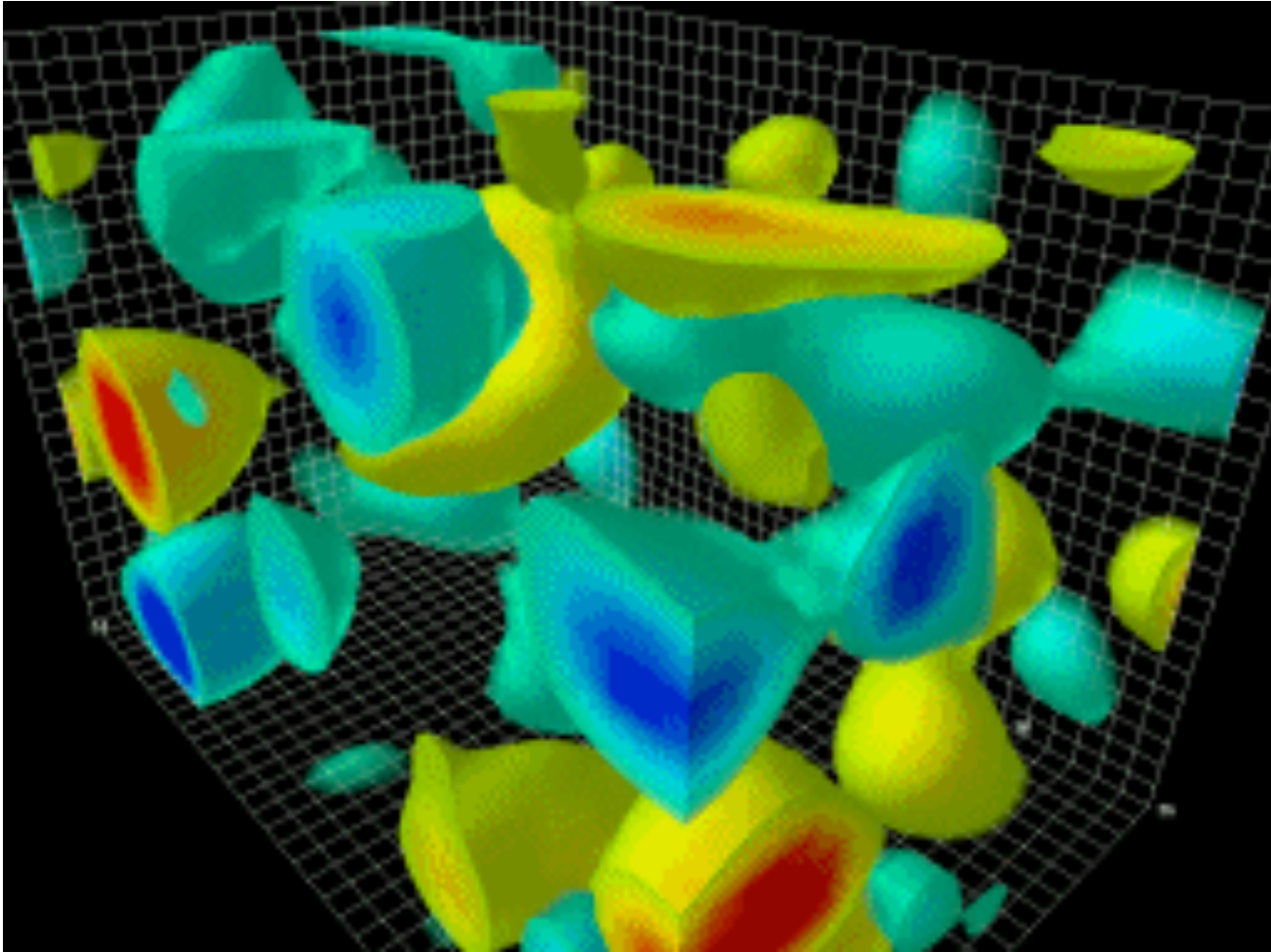
*Lagrangian
(SM) mass*

*Vacuum
condensate*

*It accounts for 99% of
the mass of our visible
matter in universe.*



QCD as Topological Material



Instantons $Q_w = \frac{1}{32\pi^2} \int d^4x (gG_a^{\mu\nu}) \cdot (g\tilde{G}_{\mu\nu}^a)$

Emergent Phenomena in QCD

F. Wilczek
@ QM2014



The study of the strong interactions is now a mature subject - we have a theory of the fundamentals* (QCD) that is correct* and complete*.

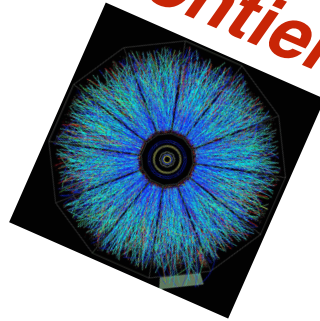
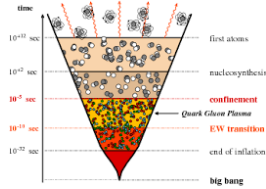
In that sense, it is akin to atomic physics, condensed matter physics, or chemistry. The important questions involve emergent phenomena and “applications”.

It *embodies* many deep aspects of relativistic quantum field theory (confinement, asymptotic freedom, anomalies/instantons, spontaneous symmetry breaking ...)

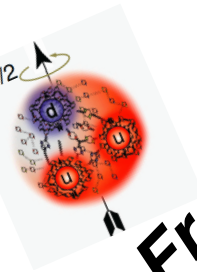
NP as Quantum Chromo Material Science

Temperature

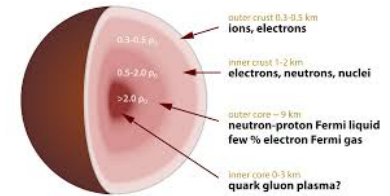
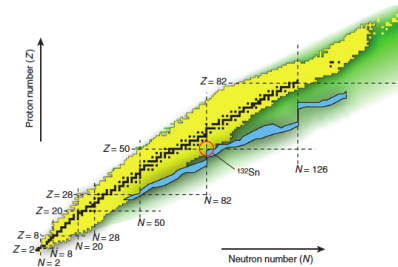
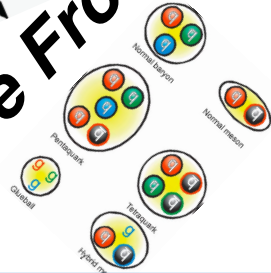
“Hot Frontier”



$s=1/2$



“Force Frontier”



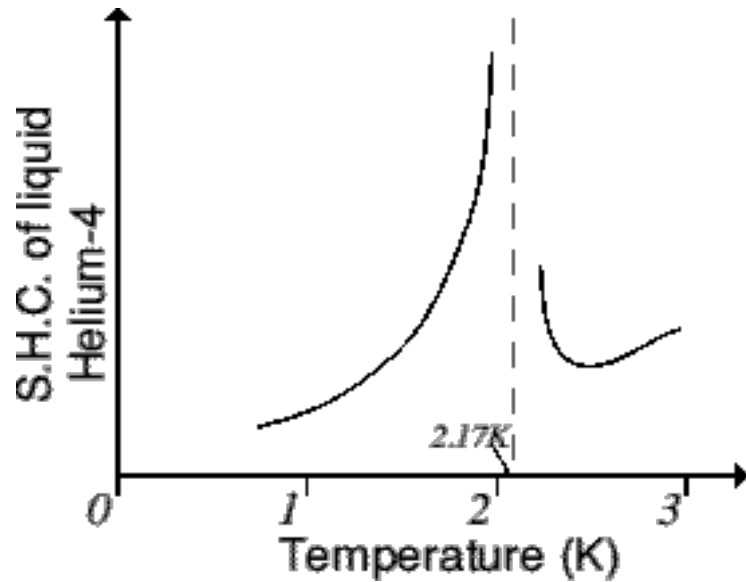
“Dense Frontier”

Baryon Density

This talk will focus on the “hot frontier”.

Quark-Gluon Plasma (QGP): A Subatomic Quantum Fluid

QCD in Hot Environment



The “super” side is hard, and let’s attack the lambda point from the “right side”, when the system is just about to condense!

Why don’t we do the same for QCD?!

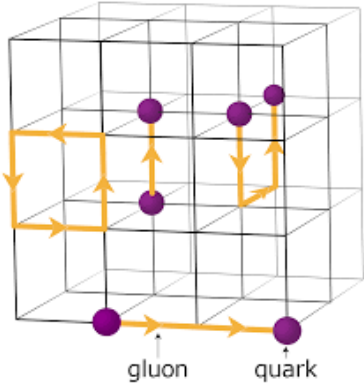
QCD at extreme temperatures:

At high enough $T \gg \Lambda_{\text{QCD}}$

A transition to a quark-gluon plasma (QGP) !

[mid ~ late 1970’s]

QGP: A New Phase of Matter



from Lattice QCD

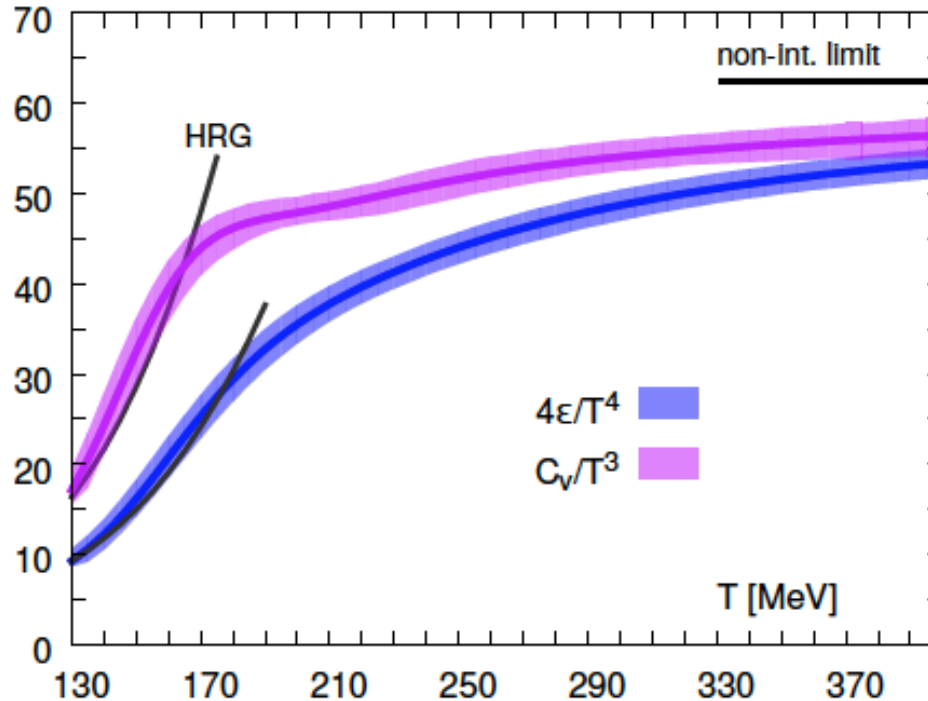
RHIC LHC

$$\epsilon = 47.5 \times \frac{\pi^2}{30} T^4$$

free QGP

a relativistic pion gas

$$\epsilon = 3 \times \frac{\pi^2}{30} T^4$$



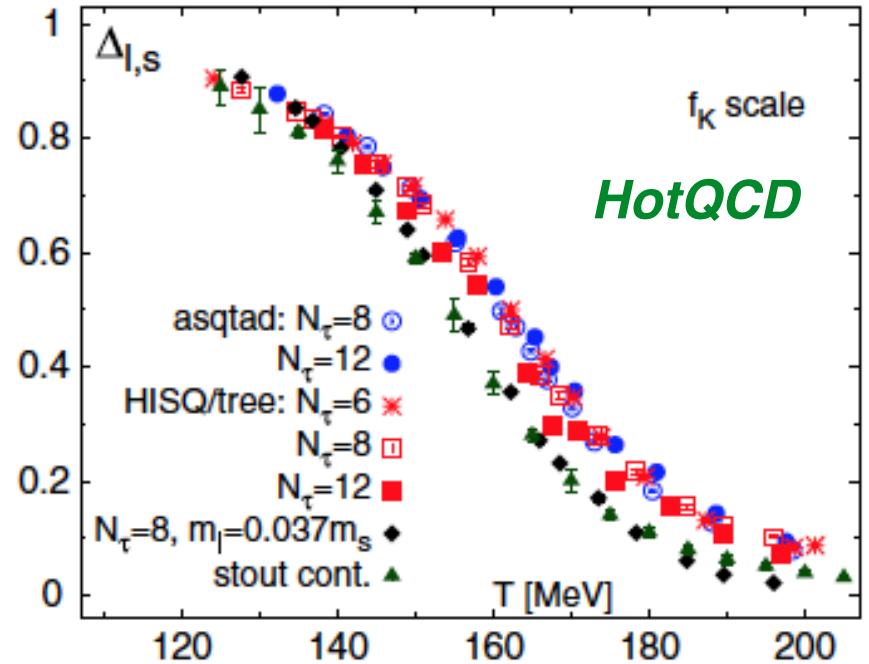
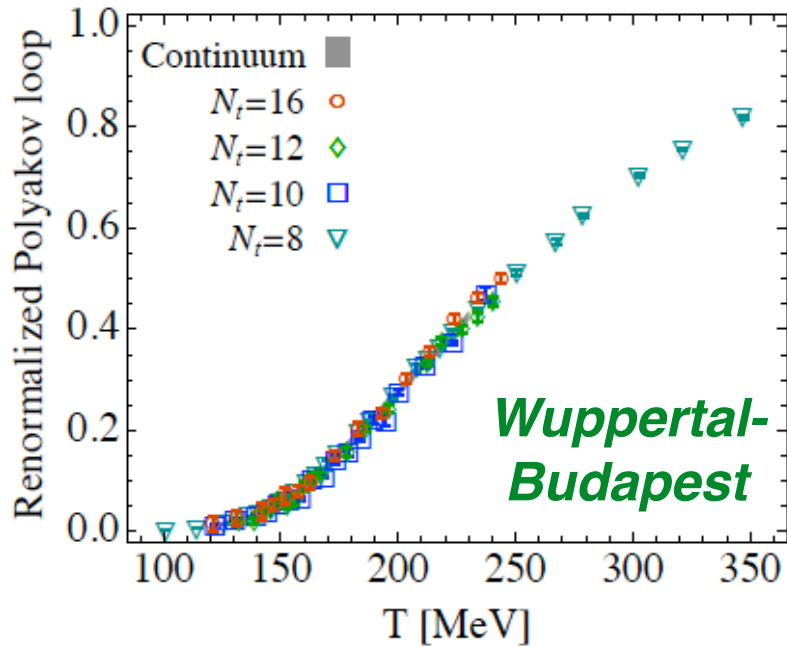
More precisely,
Hadron Resonance Gas

- * *Two benchmarks at low/high T*
- * *A transition regime in the middle*
- * *Crossover (instead of a phase transition)*

QGP: A New Phase of Matter

*The liberated
quarks & gluons*

*The restored
chiral symmetry*



$$|\langle P \rangle| = \left| \frac{1}{L_\sigma^3} \sum_x \langle P(x) \rangle \right| \rightarrow e^{-\beta F_s} \quad (L_\sigma \rightarrow \infty)$$

The high T phase of QCD matter (a few hundred MeV & up) is a distinctive new phase, the quark-gluon plasma (QGP).

Little Bangs in Heavy Ion Collisions (HIC)



***An artistic presentation:
“nuclei as heavy as bulls,
colliding into new phase of matter”***

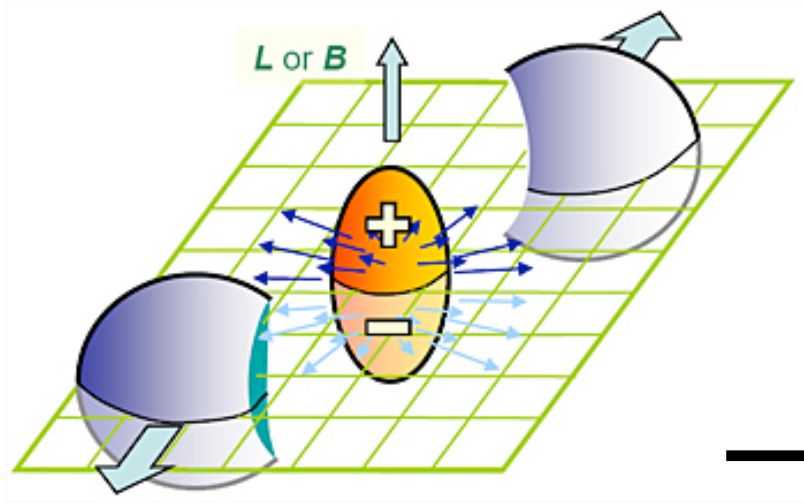


Relativistic Heavy Ion Collider

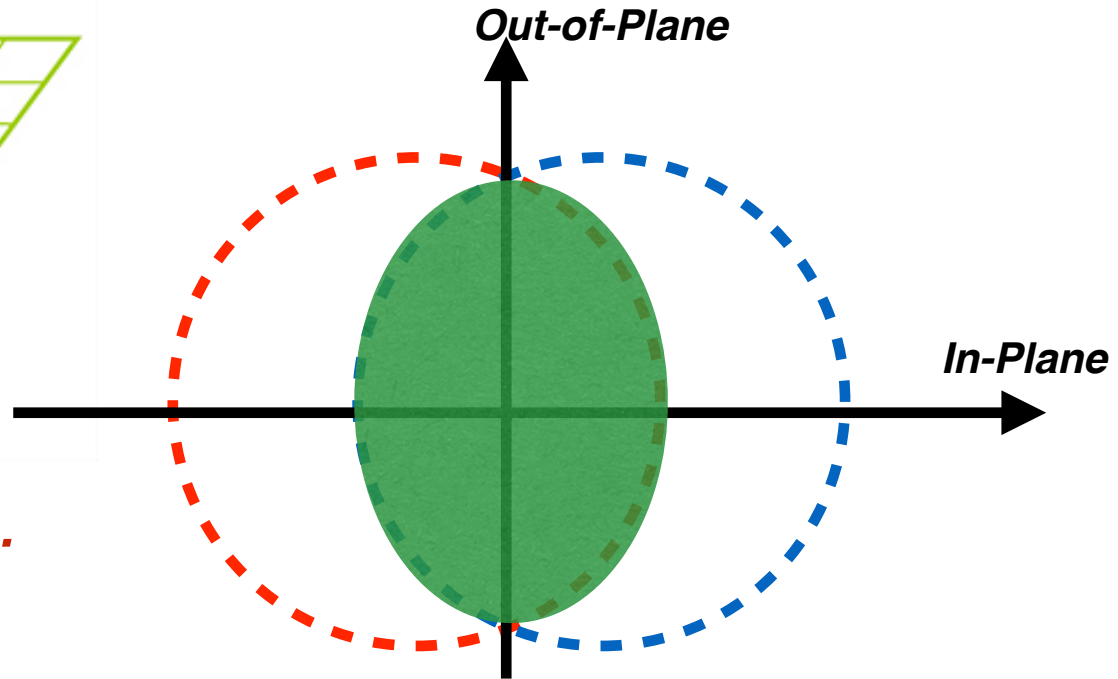
Large Hadron Collider



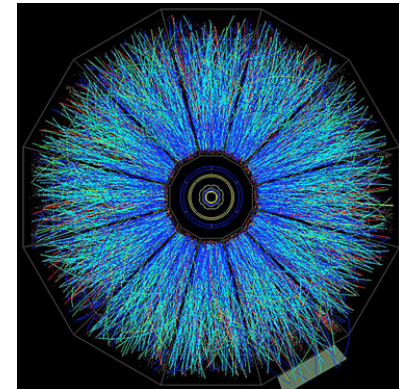
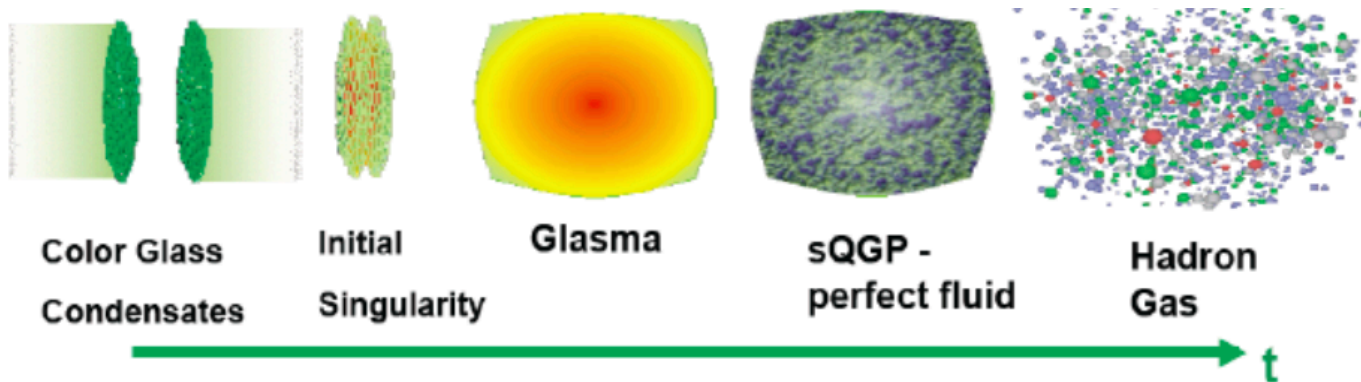
The Setup of Heavy Ion Collision



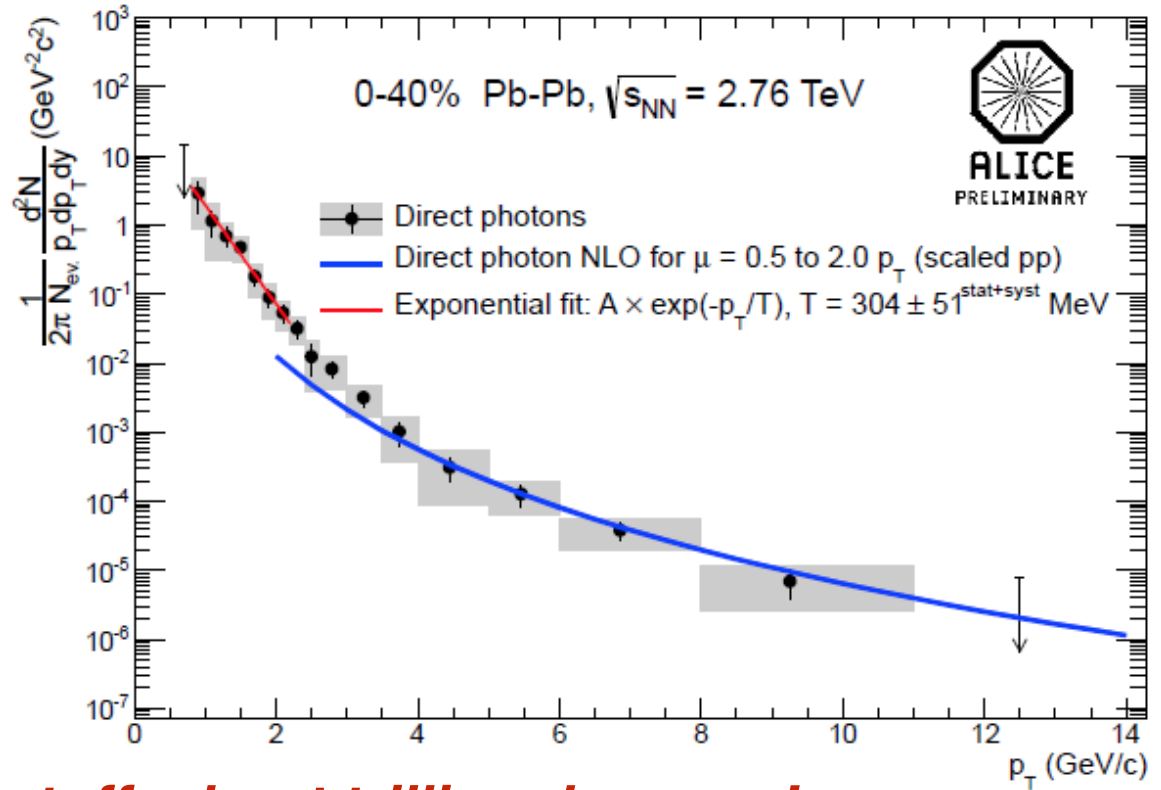
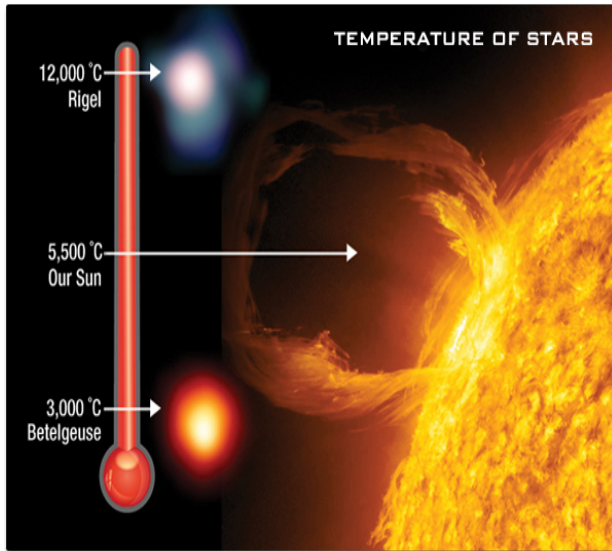
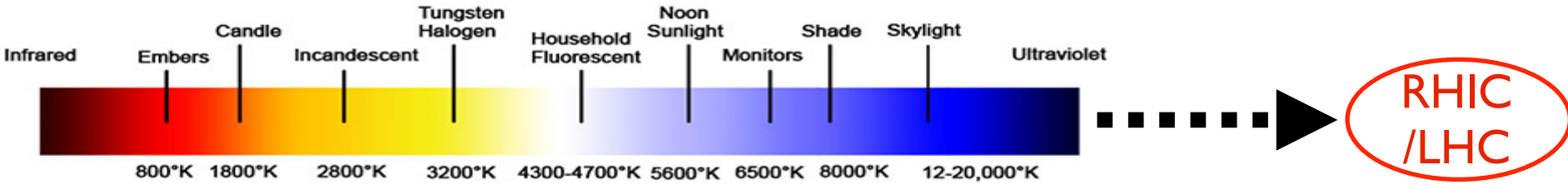
A typical off-central collision.



Quark-gluon plasma is created in such collisions!



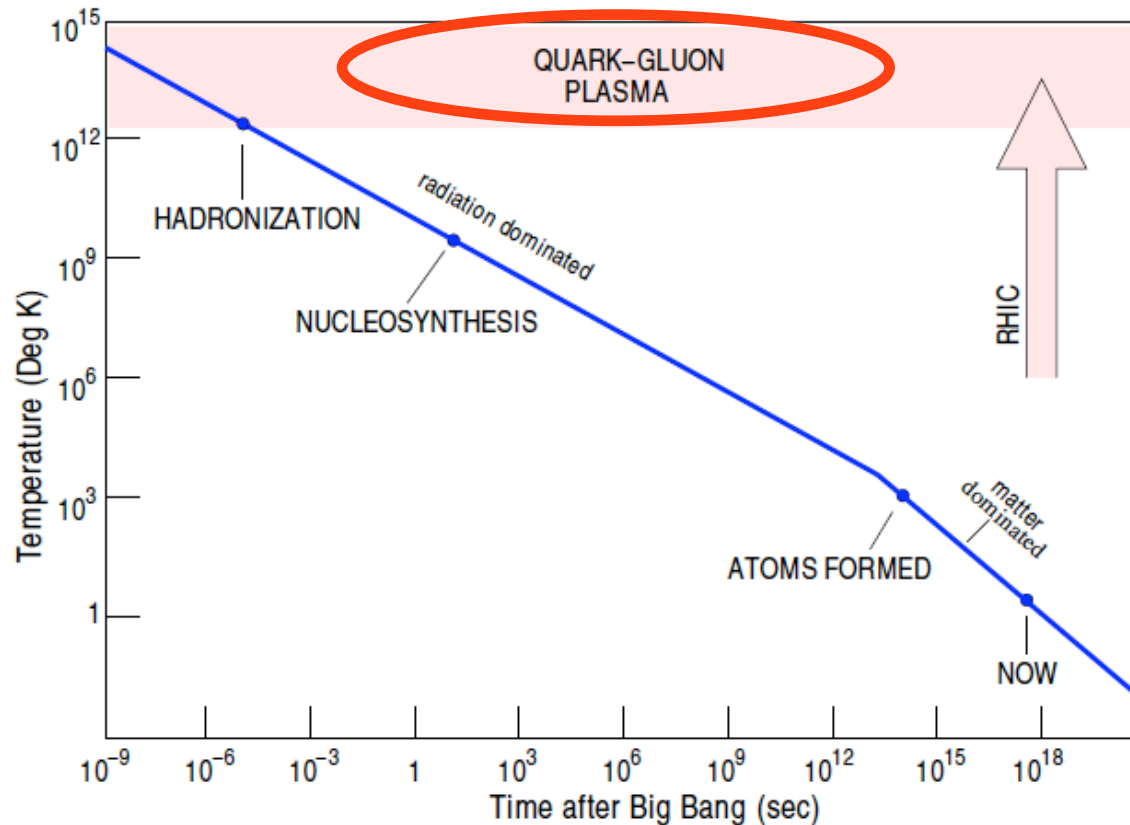
QGP Shining Brightly!



QGP is hot stuff: about trillion degrees !
Official Guinness World Record:
the highest man-made temperature!

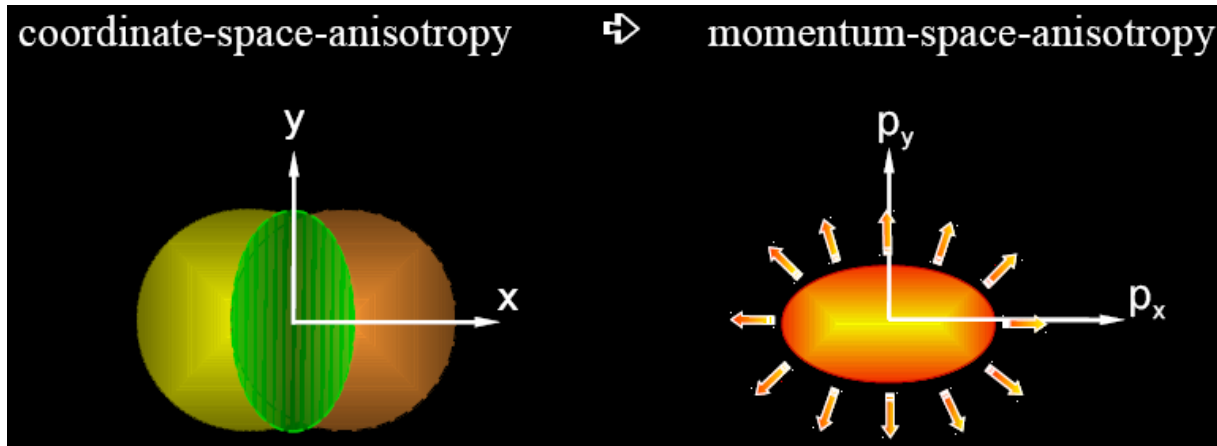
QGP: An Old Phase of Matter

*The highest ever temperature was in the beginning of universe.
The QGP temperature was available back then.*



The quark-gluon plasma is an old phase of matter!

Anisotropic Explosion: Elliptic Flow

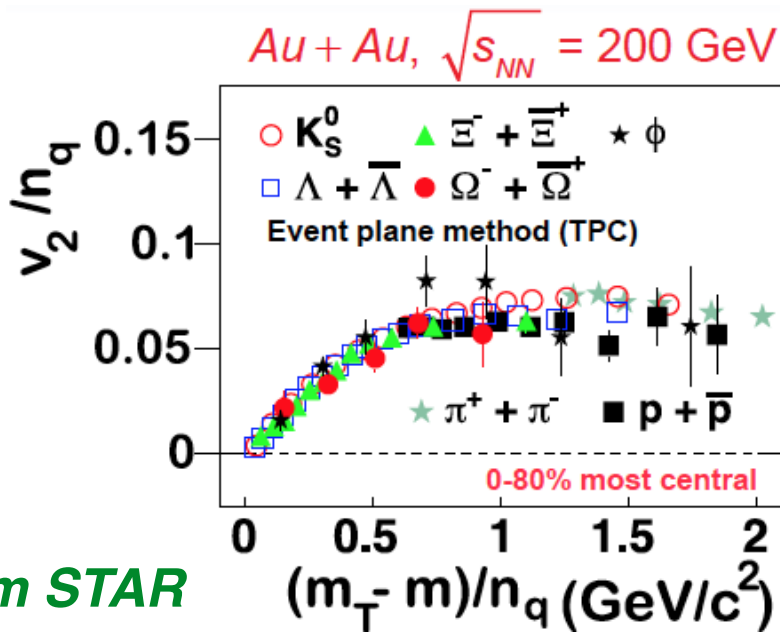


$$\frac{dN}{dP_t d\phi} = \frac{dN}{dP_t} [1 + 2v_2(P_t) \cos(2\phi) + \dots]$$

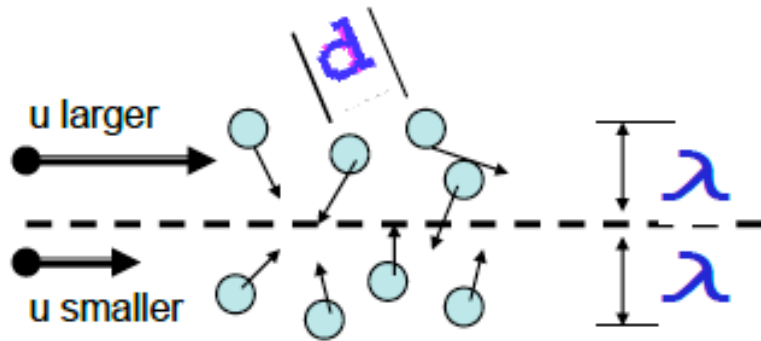
*relativistic hydrodynamics
@ 1~10 fm scale.*

*This response is very
sensitive to fluid dissipation*

$$1 \leq 4\pi(\eta/s)_{\text{QGP}} \leq 2.5$$



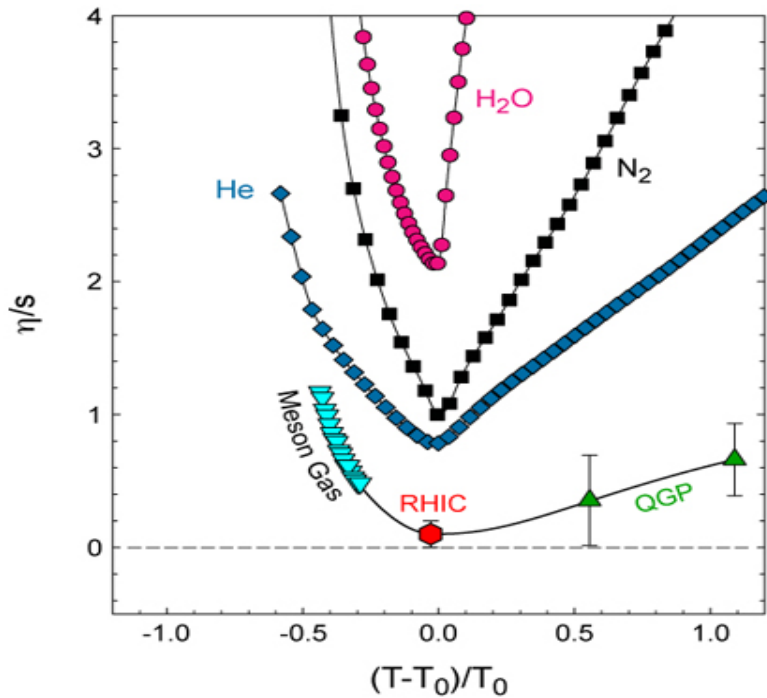
QGP: Nearly Perfect Quantum Liquid



$$\eta \sim \rho v_T \lambda \sim n p_T \lambda$$

$$s \sim n$$

$$\eta/s \sim p_T \lambda \sim \lambda/\lambda_{dB}$$



QGP is a quantum fluid:

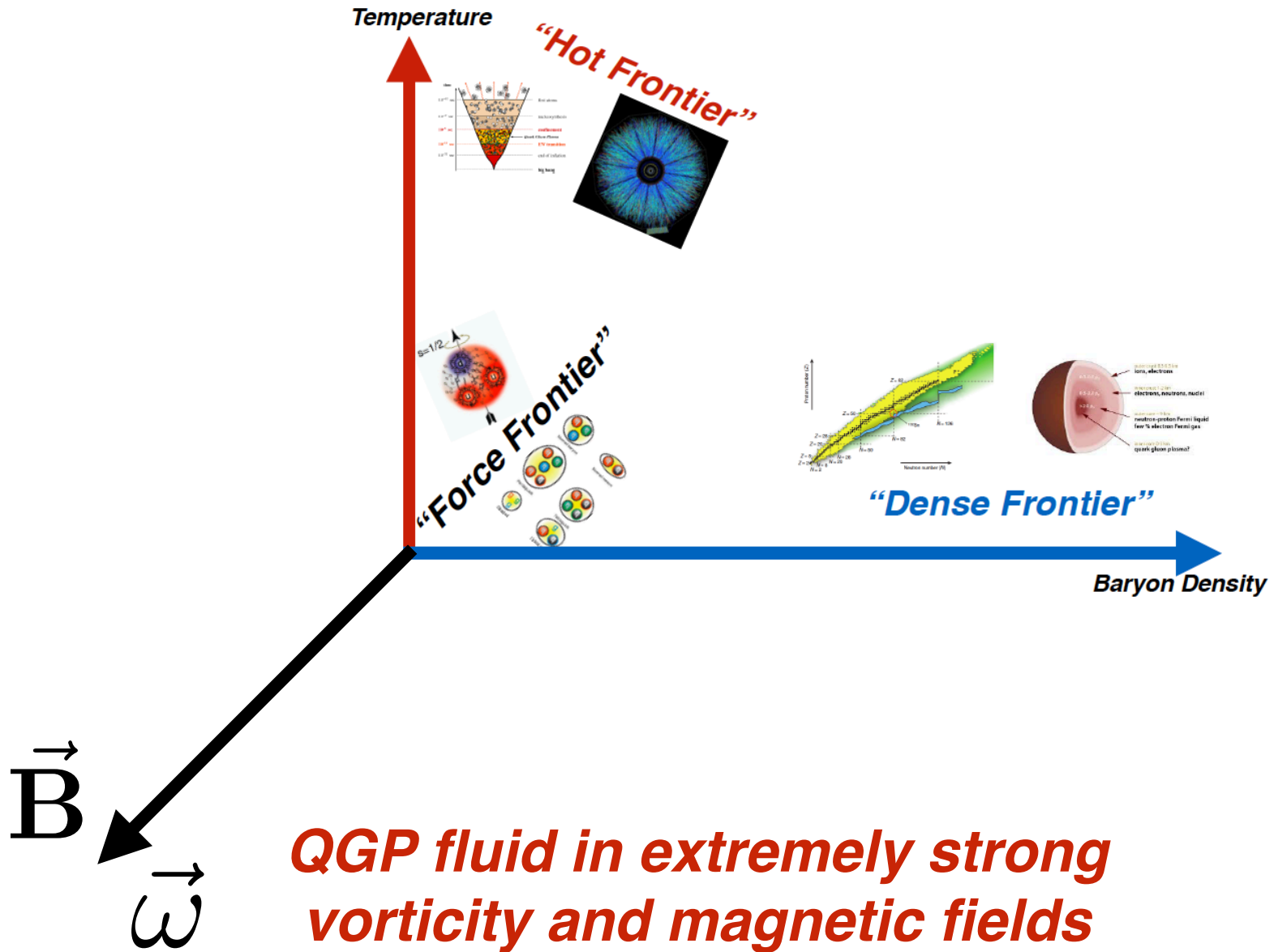
$$\lambda_{\text{M.F.P.}} \sim \lambda_{\text{de Broglie}}$$

[A recent ravel: cold atomic gas with infinite scattering length]

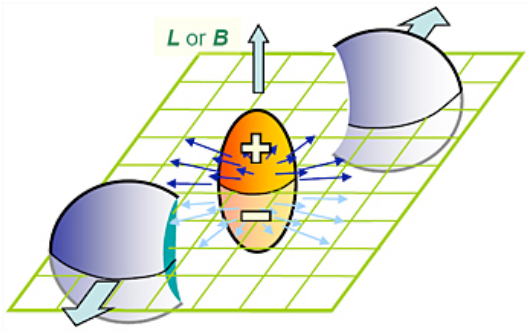
It has nearly perfect fluidity: less dissipative than known substance; very close to conjectured lower bound.

Vorticity & Magnetic Field

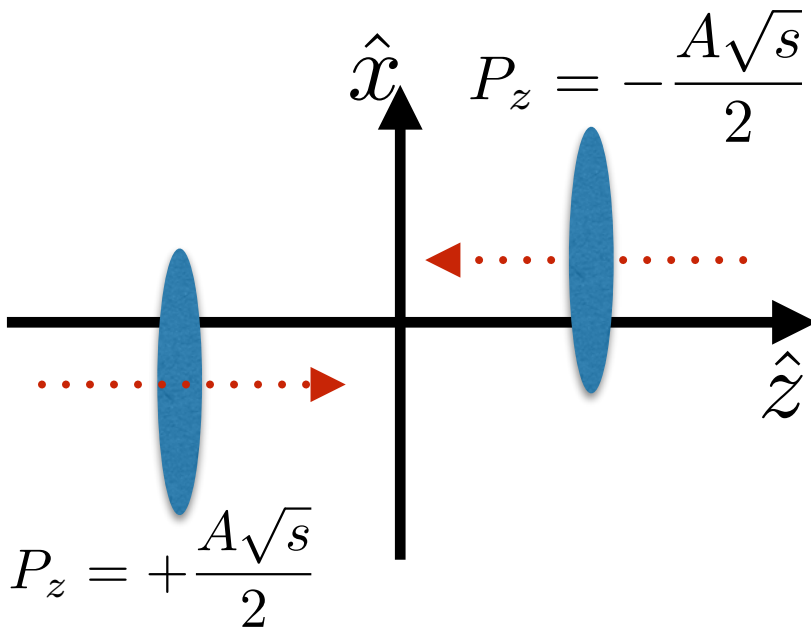
Fascinating New Frontiers



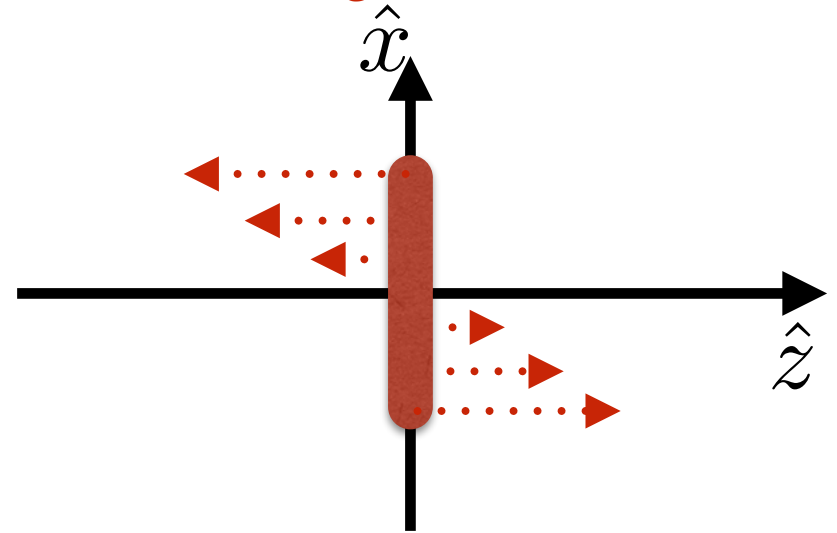
Rotating Quark-Gluon Plasma



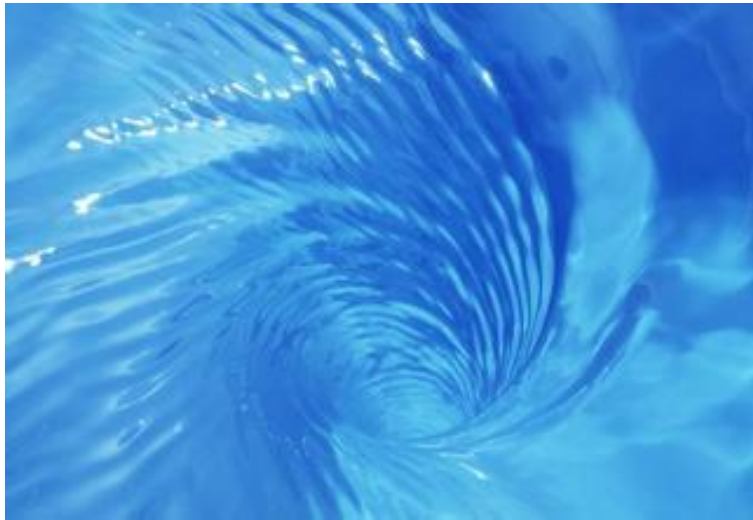
$$L_y = \frac{Ab\sqrt{s}}{2} \sim 10^{4\sim 5} \hbar$$



QGP's way of accommodating this angular momentum

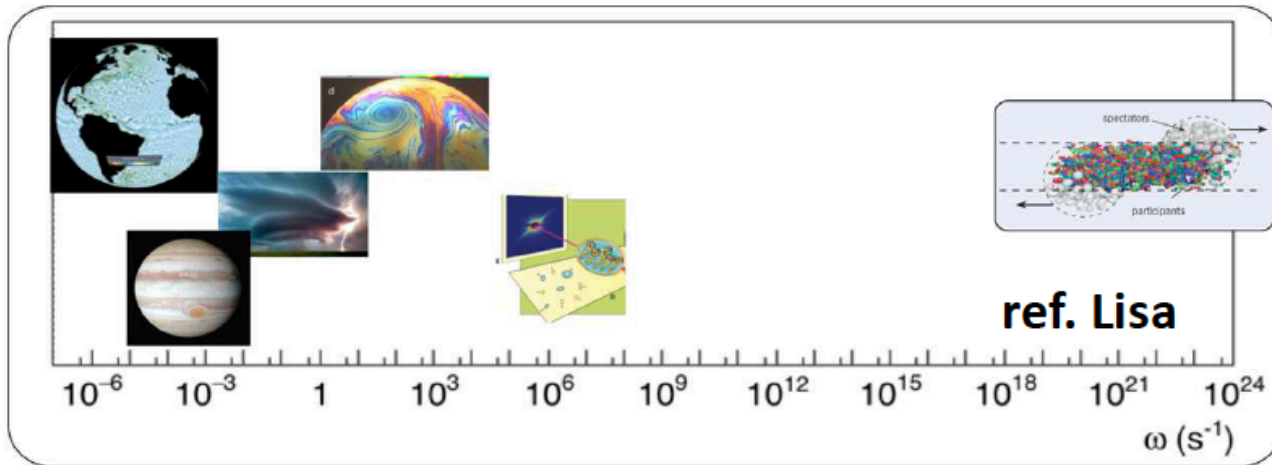


Quantifying Fluid Rotation



NR $\vec{\omega} = \frac{1}{2} \nabla \times \vec{v}$

UR $\Omega_{\mu\nu} = \frac{1}{2} (\partial_\nu u_\mu - \partial_\mu u_\nu)$



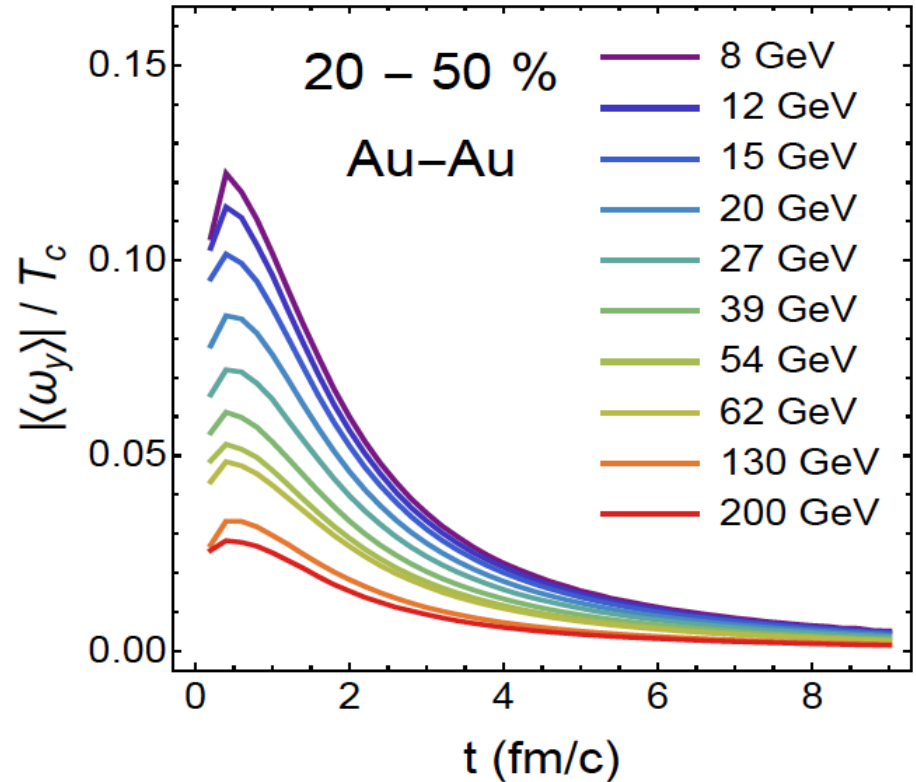
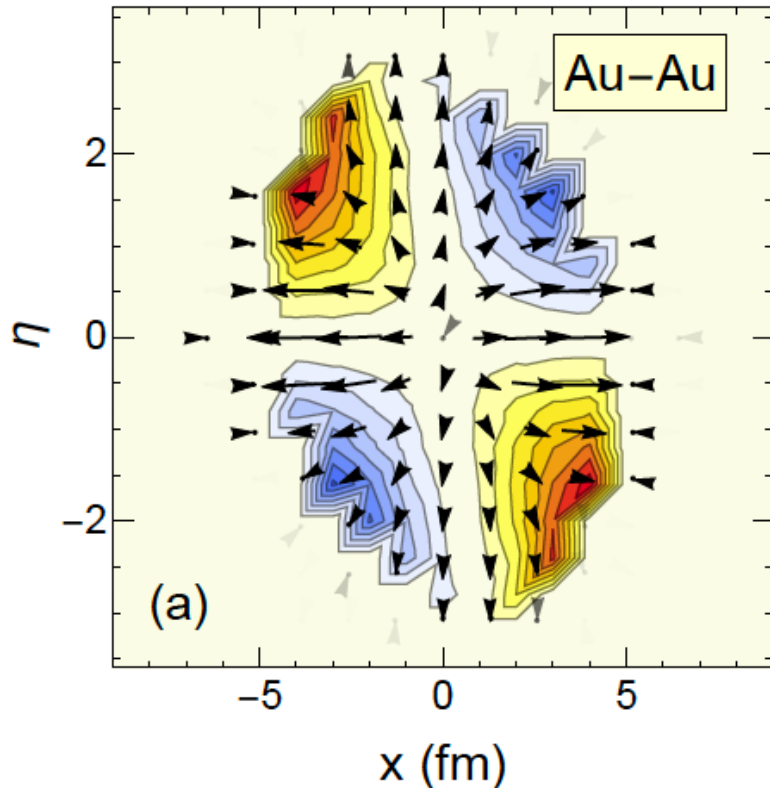
Heavy ion collisions:

$v \sim 0.1 c$

$\partial \sim \text{fm}^{-1}$

$\omega \sim 10^{22} \text{ s}^{-1}$

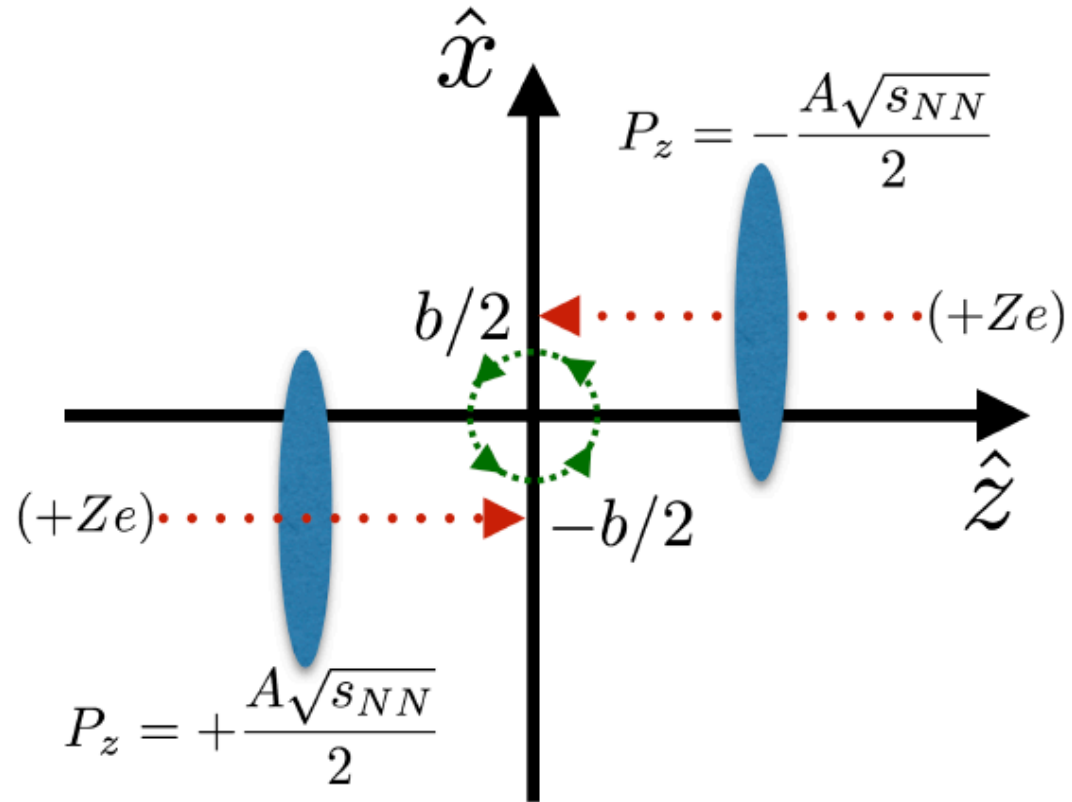
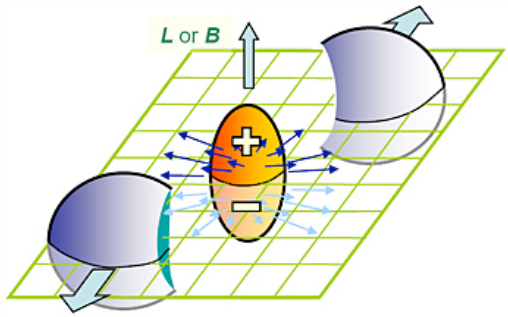
Rotating Quark-Gluon Plasma



The averaged vorticity strongly increases toward low beam energy!

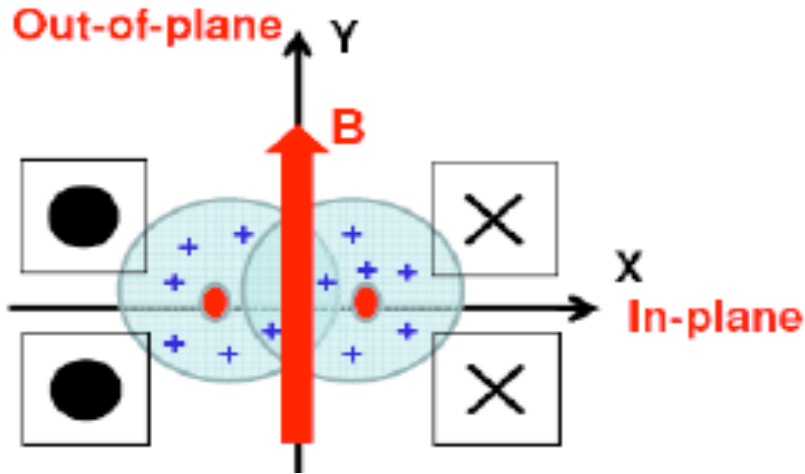
Jiang, Lin, JL, PRC2016; Deng & Huang, PRC2016;
Xia, Li, Wang, et al, PRC; Shi, Li, JL, PLB2018; ...

Strong Electromagnetic Fields

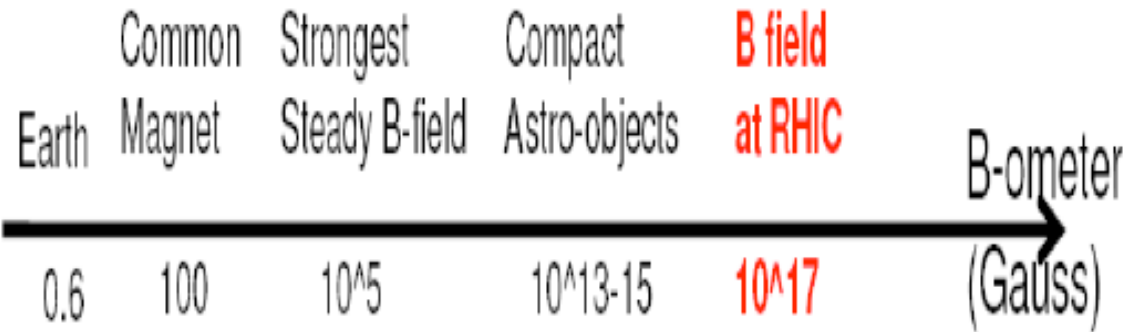


**The angular momentum together with large $(+Ze)$ nuclear charge
→ strong magnetic field!**

Strong Electromagnetic Fields

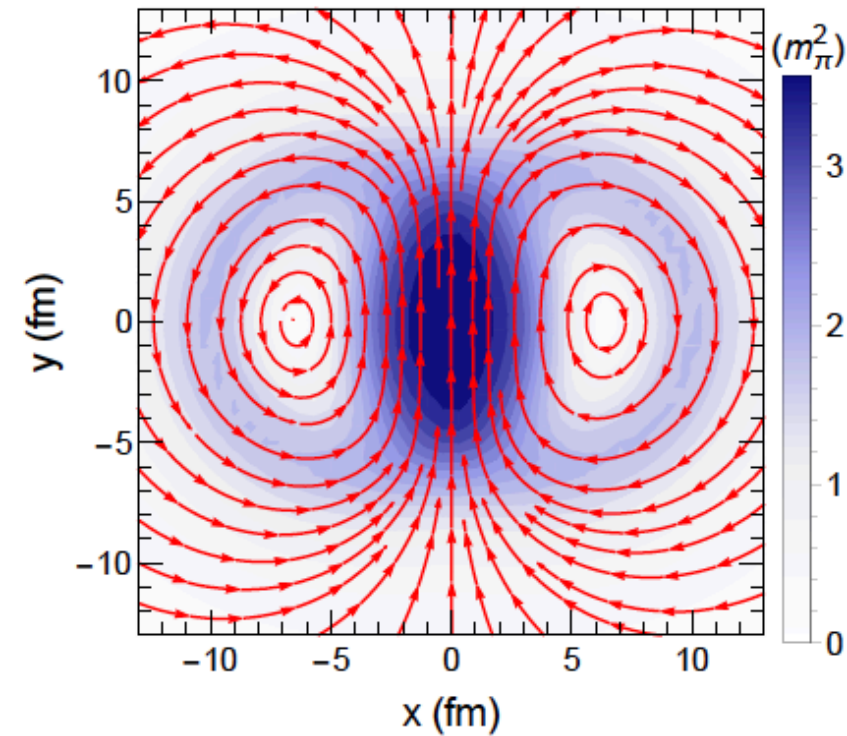


$$E, B \sim \gamma \frac{Z \alpha_{EM}}{R_A^2} \sim 3m_\pi^2$$

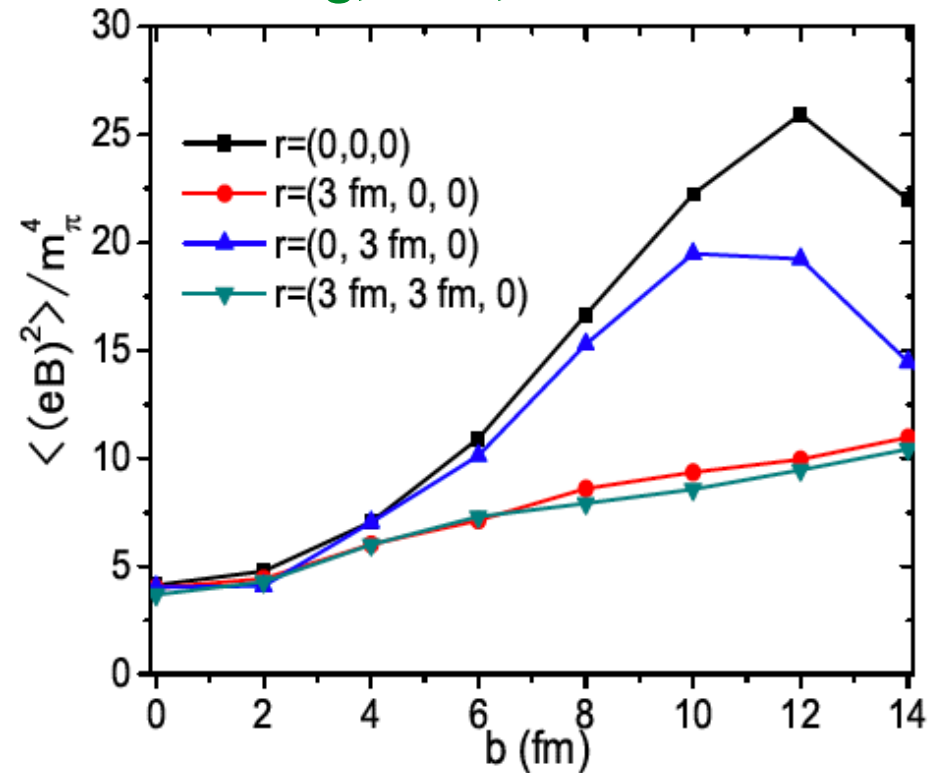


- **Strongest B field (and strong E field as well) naturally arises!**
[Kharzeev, McLerran, Warringa; Skokov, et al; Bzdak-Skokov; **Deng-Huang**; Skokov-McLerran; Tuchin; ...]
- “Out-of-plane” orientation (approximately)
[Bloczynski-Huang-Zhang-Liao]

Strong Electromagnetic Fields



Huang, Liao, et al PLB2012



Quantitative simulations confirm the existence of such extreme fields!

[STAR measurements of dielectron directly from such fields, PRL2018]

Spin & Rotational Polarization

Spin-Fluid Coupling

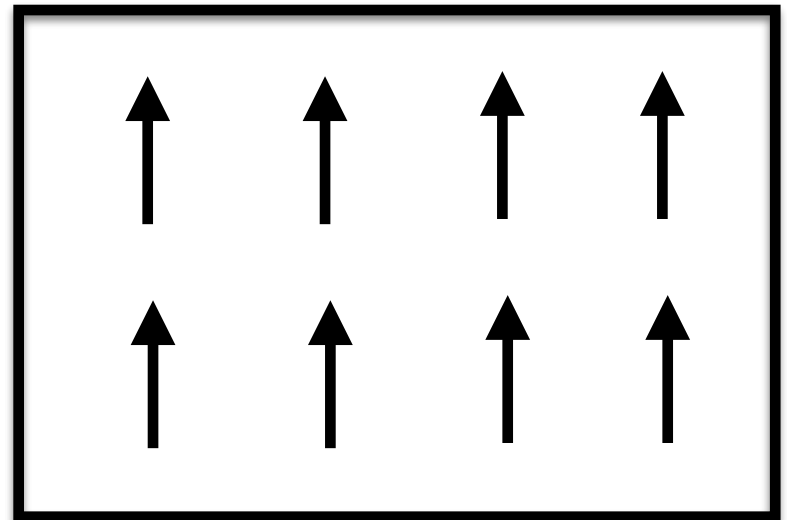
How does a many-body system cope with a sizable angular momentum?

*Orbital motion (vorticity);
Spin alignment (polarization).*



Fluid vorticity

Macroscopic



Individual spin

Microscopic, quantum

???



Spin & Rotational Polarization

Dirac Lagrangian in rotating frame:

$$g_{\mu\nu} = \begin{pmatrix} 1 - \vec{v}^2 & -v_1 & -v_2 & -v_3 \\ -v_1 & -1 & 0 & 0 \\ -v_2 & 0 & -1 & 0 \\ -v_3 & 0 & 0 & -1 \end{pmatrix}$$

$$\vec{v} = \vec{\omega} \times \vec{x}.$$

$$\bar{\gamma}^\mu = e_a^\mu \gamma^a$$

$$\Gamma_\mu = \frac{1}{4} \times \frac{1}{2} [\gamma^a, \gamma^b] \Gamma_{ab\mu}$$



$$\mathcal{L} = \bar{\psi} [i\bar{\gamma}^\mu (\partial_\mu + \Gamma_\mu) - m] \psi$$

Under slow rotation:

$$\mathcal{L} = \psi^\dagger \left[i\partial_0 + i\gamma^0 \vec{\gamma} \cdot \vec{\partial} + (\vec{\omega} \times \vec{x}) \cdot (-i\vec{\partial}) + \vec{\omega} \cdot \vec{S}_{4 \times 4} \right] \psi$$

$$\hat{H} = \gamma^0 (\vec{\gamma} \cdot \vec{p} + m) - \vec{\omega} \cdot (\vec{x} \times \vec{p} + \vec{S}_{4 \times 4}) = \hat{H}_0 - \vec{\omega} \cdot \hat{\vec{J}}$$

**Rotational
polarization effect!**

Rotational Polarization

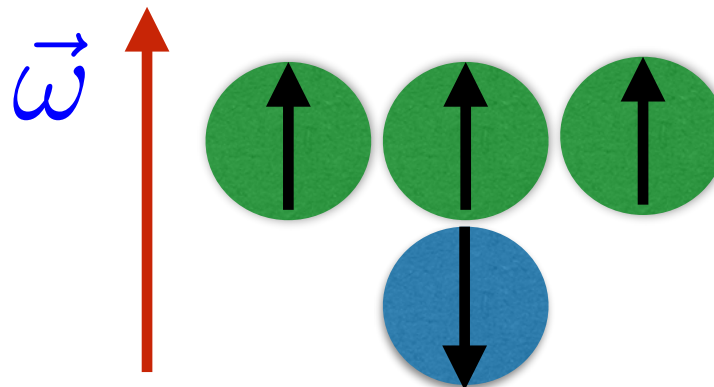
$$\hat{H} = \gamma^0(\vec{\gamma} \cdot \vec{p} + m) - \vec{\omega} \cdot (\vec{x} \times \vec{p} + \vec{S}_{4 \times 4}) = \hat{H}_0 - \vec{\omega} \cdot \hat{J}$$

**Rotational
polarization effect!**



**For thermally produced particles:
“equal-partition” of angular momentum**

$$dN \propto e^{\frac{\vec{\omega} \cdot \vec{J}}{T}}$$

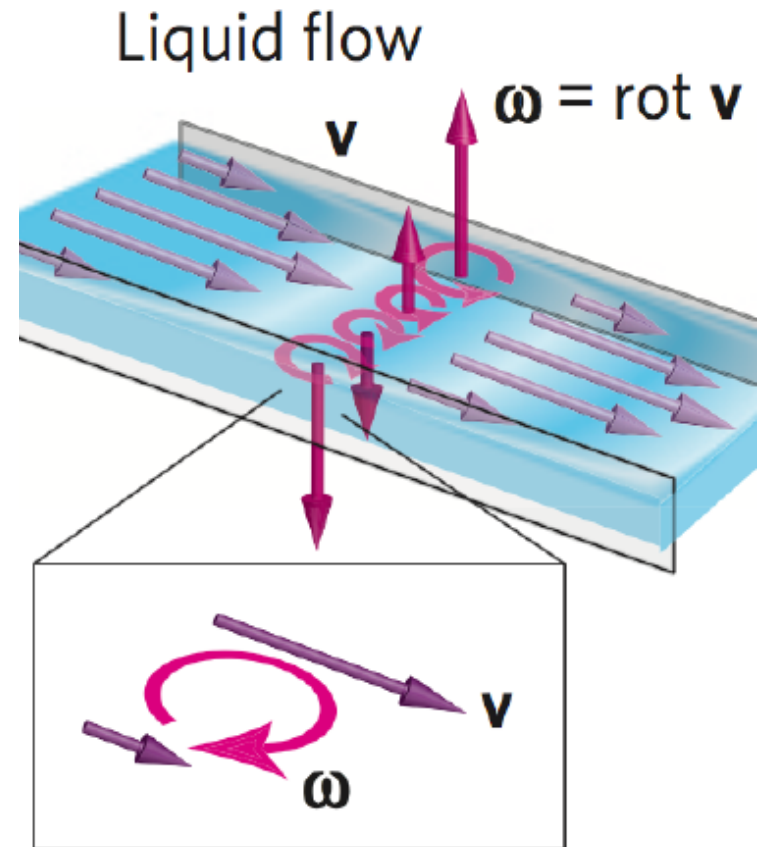


From Vorticity to Spin Polarization

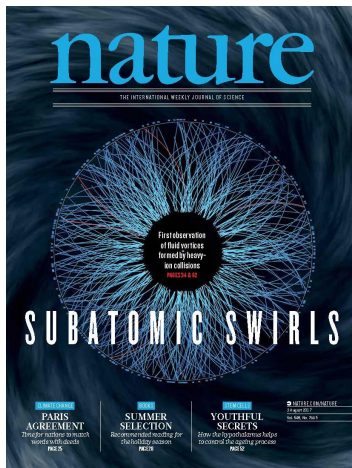
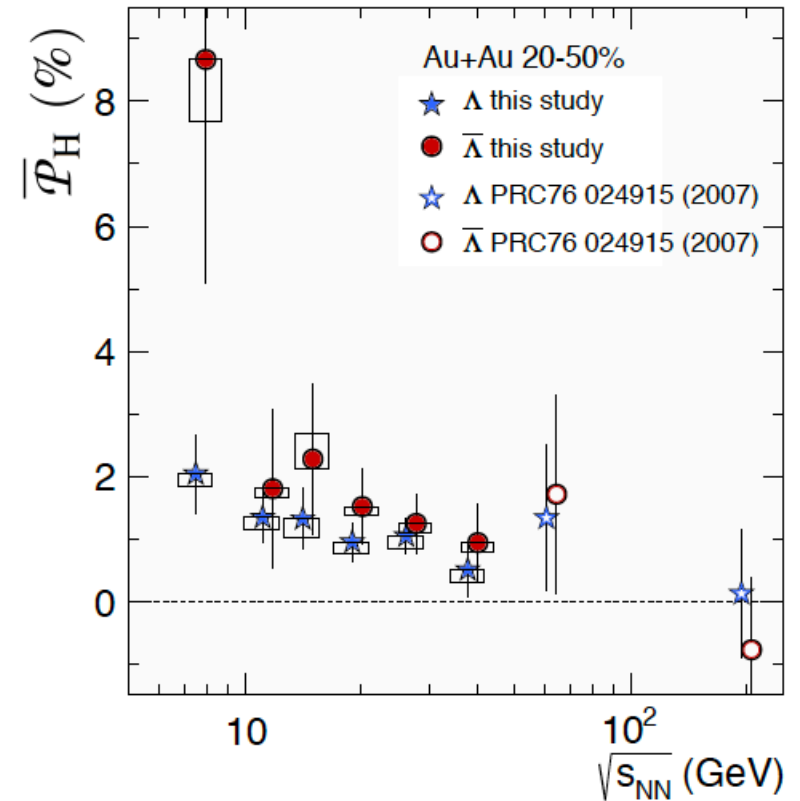
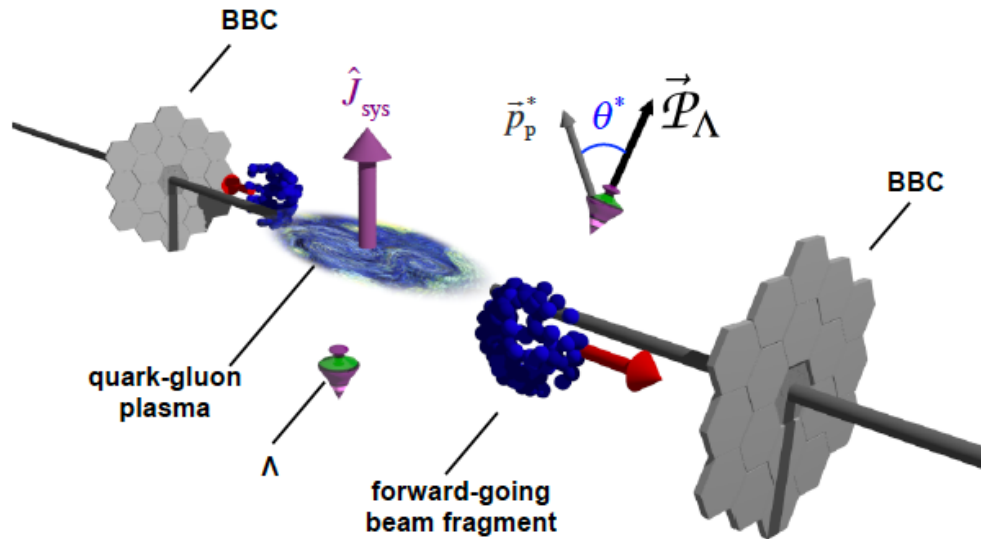
“Spin hydrodynamic generation”
Takahashi, *et al.* Nat. Phys. (2016)

Viscous fluid flow
—> vorticity
—> spin polarization

“Fluid Spintronics”

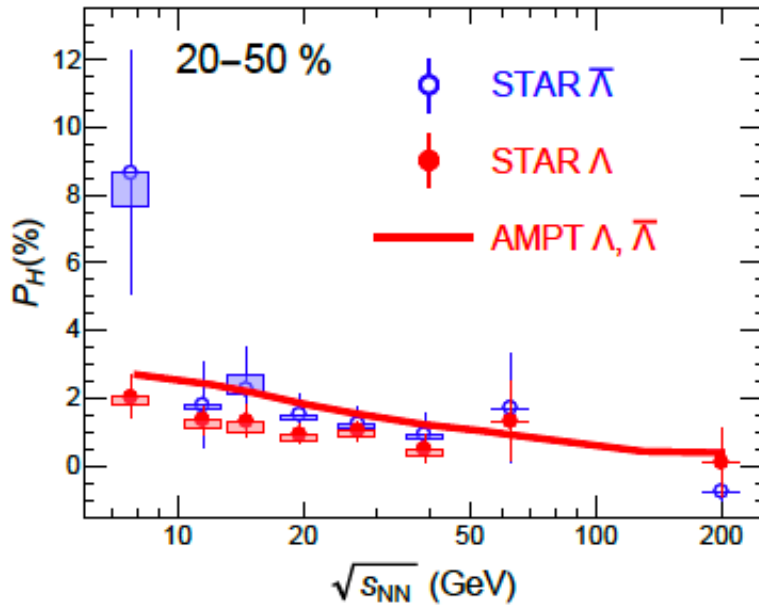


Fluid Spintronics in the Subatomic Swirls



STAR Collaboration, Nature 2017

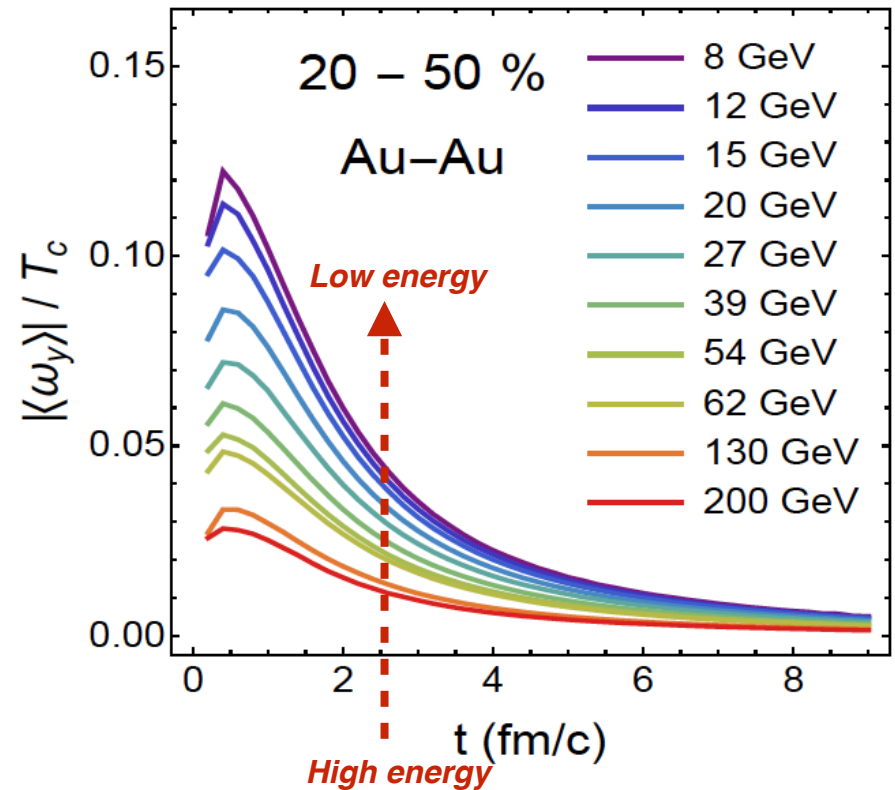
Fluid Spintronics in the Subatomic Swirls



$$\omega \approx (9 \pm 1) \times 10^{21} \text{ s}^{-1}$$

The most vortical fluid!

Jiang, Lin, JL, PRC2016



STAR Collaboration, Nature 2017

Rotational Suppression of Fermion Pairing

Let us consider pairing phenomenon in fermion systems.

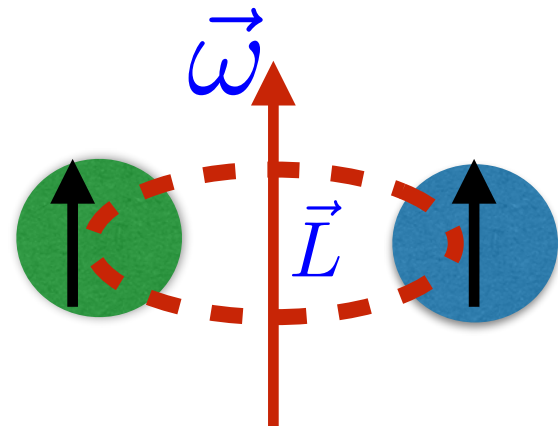
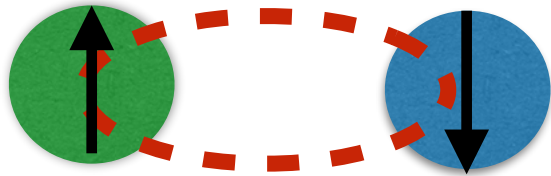
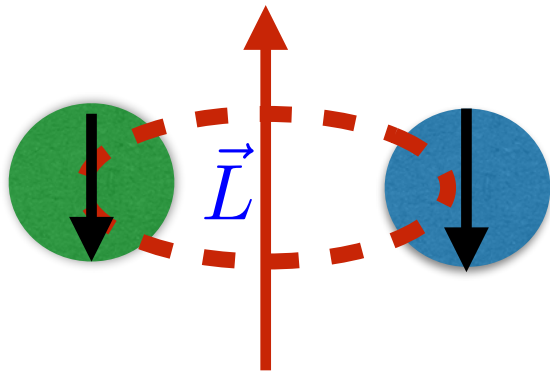
There are many examples:

superconductivity, superfluidity, chiral condensate, diquark, ...

We consider scalar pairing state, with $J=0$.

$$\vec{S} = \vec{s}_1 + \vec{s}_2 \quad \vec{J} = \vec{L} + \vec{S}$$

Rotation tends to polarize ALL angular momentum, both L and S, thus suppressing scalar pairing.



[Yin Jiang, JL, PRL2016]


[Rotational Inhabitation: Chen, Fukushima, Huang, Mameda, PRD2016]

Chiral Magnetic Effect in the Subatomic Chiral Matter

Exciting Progress: See Recent Reviews


Progress in Particle and Nuclear Physics 88 (2016) 1–28

Contents lists available at [ScienceDirect](#)

 **ELSEVIER**

Progress in Particle and Nuclear Physics

journal homepage: www.elsevier.com/locate/ppnp




Review

Chiral magnetic and vortical effects in high-energy nuclear collisions—A status report

D.E. Kharzeev^{a,b}, J. Liao^{c,d,*}, S.A. Voloshin^e, G. Wang^f

^a Department of Physics and Astronomy, Stony Brook University, Stony Brook, NY 11794-3800, USA
^b Department of Physics and RIKEN-BNL Research Center, Brookhaven National Laboratory, Upton, NY 11973-5000, USA
^c Physics Department and Center for Exploration of Energy and Matter, Indiana University, 727 E Third Street, Bloomington, IN 47405, USA
^d RIKEN BNL Research Center, Bldg. 510A, Brookhaven National Laboratory, Upton, NY 11973, USA
^e Department of Physics and Astronomy, Wayne State University, 666 W. Hancock, Detroit, MI 48201, USA
^f Department of Physics and Astronomy, University of California, Los Angeles, CA 90095, USA

 CrossMark

Prog. Part. Nucl. Phys. 88, 1 (2016)[arXiv:1511.04050 [hep-ph]].

J. Liao, Pramana 84, no. 5, 901 (2015) [arXiv:1401.2500 [hep-ph]].

X.G. Huang, ROPP2016; Hattori, Huang, 2017.

Chiral Anomaly

Chiral anomaly is a fundamental aspect of QFT with chiral fermions.

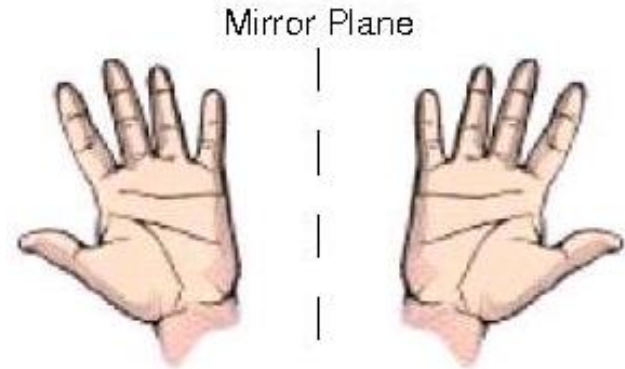
Classical symmetry:

$$\mathcal{L} = i\bar{\Psi}\gamma^\mu\partial_\mu\Psi$$

$$\mathcal{L} \rightarrow i\bar{\Psi}_L\gamma^\mu\partial_\mu\Psi_L + i\bar{\Psi}_R\gamma^\mu\partial_\mu\Psi_R$$

$$\Lambda_A : \Psi \rightarrow e^{i\gamma_5\theta}\Psi$$

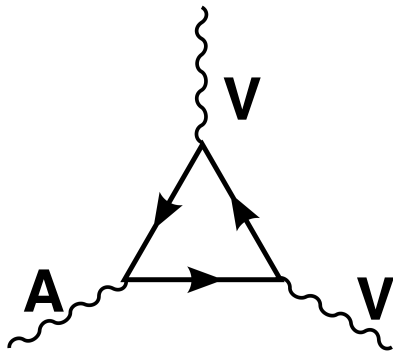
$$\partial_\mu J_5^\mu = 0$$



Broken at QM level:

$$\partial_\mu J_5^\mu = C_A \vec{E} \cdot \vec{B}$$

$$dQ_5/dt = \int_{\vec{x}} C_A \vec{E} \cdot \vec{B}$$

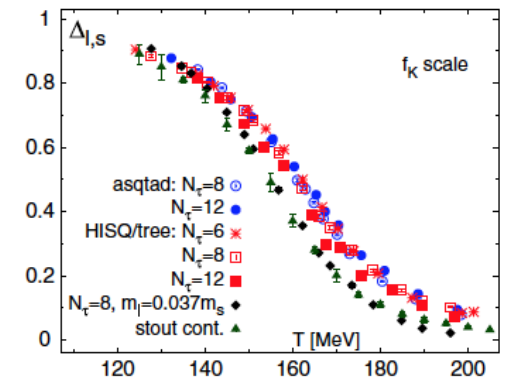
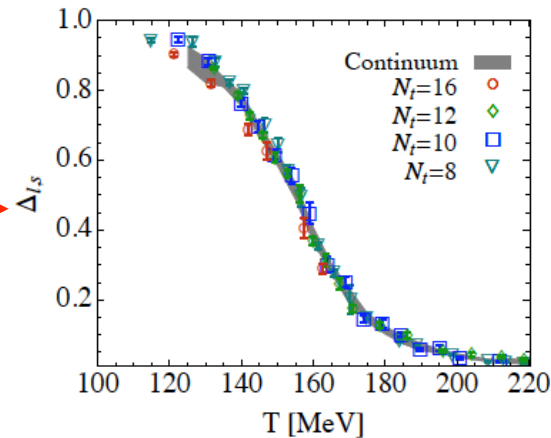
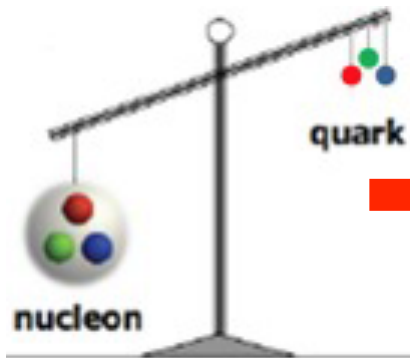


[e.g. $\pi^0 \rightarrow 2 \text{ gamma}$]

- * C_A is universal anomaly coefficient
- * Anomaly is intrinsically QUANTUM effect

Chiral Restoration in QGP

** Spontaneously broken chiral symmetry in the vacuum is a fundamental property of QCD.*

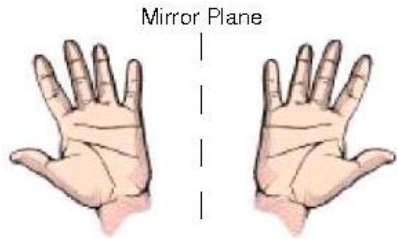
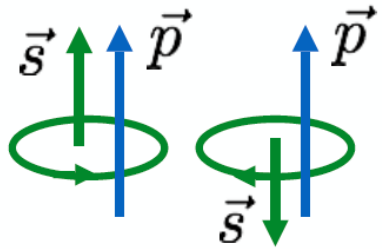


** A chirally symmetric quark-gluon plasma at high temperature is also a fundamental property of QCD!*

Can we see direct experimental evidence for that?

Chiral Restoration via Chiral Anomaly

$$J_5^\mu = J_R^\mu - J_L^\mu$$



$$\partial_\mu J_5^\mu = 2iM\bar{\Psi}\gamma^5\Psi + C_A\vec{E}\cdot\vec{B}$$

Low T
Strong spon. breaking



High T
Quantum Anomaly

Look for pure quantum anomaly effect in hot QGP with chiral symmetry restoration!

The Chiral Magnetic Effect (CME)

Chirality & Anomaly & Topology

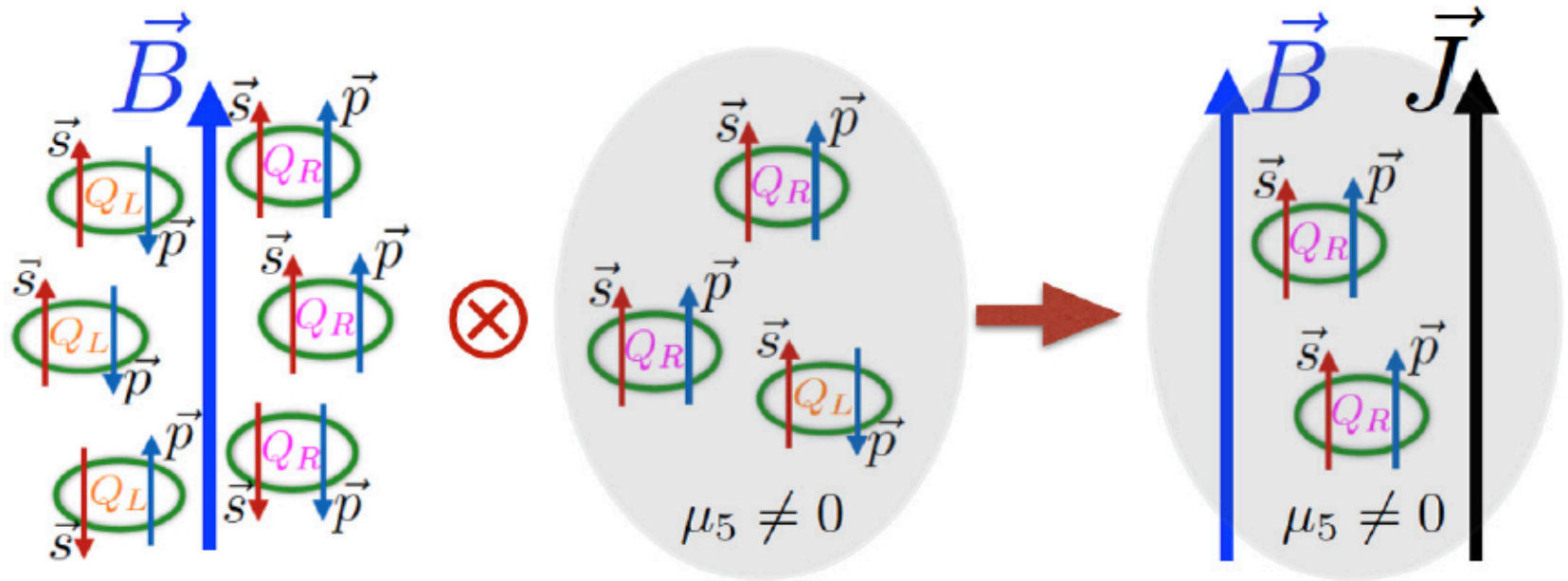
$$\vec{J} = \frac{Q^2}{2\pi^2} \mu_5 \vec{B}$$

Electric
Current

Magnetic
Field

Q.M. Transport

Intuitive Picture of CME



Intuitive understanding of CME:

Magnetic polarization \rightarrow
correlation between micro.
SPIN & EXTERNAL FORCE



Chiral imbalance \rightarrow
correlation between directions of
SPIN & MOMENTUM



Transport current along magnetic field

$$\vec{J} = \frac{Q^2}{2\pi^2} \mu_5 \vec{B}$$

From Micro. Laws To Macro. Phenomena

Micro. Laws:

*Symmetry;
Lagrangian;
Conservation laws;*

.....

Macro. Phenomena:

*Thermodynamics;
Transport;
Fluid Dynamics;*

.....



WHAT ABOUT the “SEMI”-SYMMETRY???
i..e ANOMALY?!

– classical symmetry that is broken in quantum theory

CME = Macroscopic Chiral Anomaly

$$\text{Anomaly --> } \partial^\mu j_\mu^5 = \frac{q^2}{2\pi^2} \mathbf{E} \cdot \mathbf{B} \quad \frac{dN_5}{dt d^3x} = \frac{q^2}{2\pi^2} \mathbf{E} \cdot \mathbf{B}$$

$$\text{Chirality --> } \int d^3x j_{el} \cdot \mathbf{E} = \mu_5 \frac{dN_5}{dt} = \frac{q^2 \mu_5}{2\pi^2} \int d^3x \mathbf{B} \cdot \mathbf{E}$$

$$\mathbf{E} \rightarrow 0 \quad \mathbf{j}_{el} = \left(q^2 \mu_5 / 2\pi^2 \right) \mathbf{B}$$

- * This is a **non-dissipative** current!
- * Indeed the chiral magnetic conductivity is **P-odd** but **T-even**!
(In contrast the Ohmic conductivity is **T-odd** and dissipative.)

**CME is a quantum/anomalous transport current
as macroscopic manifestation of microscopic quantum anomaly.**

Fluid Dynamics That Knows Left & Right

conservation
law:

$$\partial_\mu J^\mu = 0 \longrightarrow \partial_\mu J^\mu = C E^\mu B_\mu$$

constituent
relation:

$$J^\mu = n u^\mu + \nu^\mu$$

$$\partial_\mu s^\mu \geq 0$$

$$\nu^\mu = -\sigma T P^{\mu\nu} \partial_\nu \left(\frac{\mu}{T} \right) + \sigma E^\mu + \xi \omega^\mu + \xi_B B^\mu$$

[Son, Surowka, 2009;...]

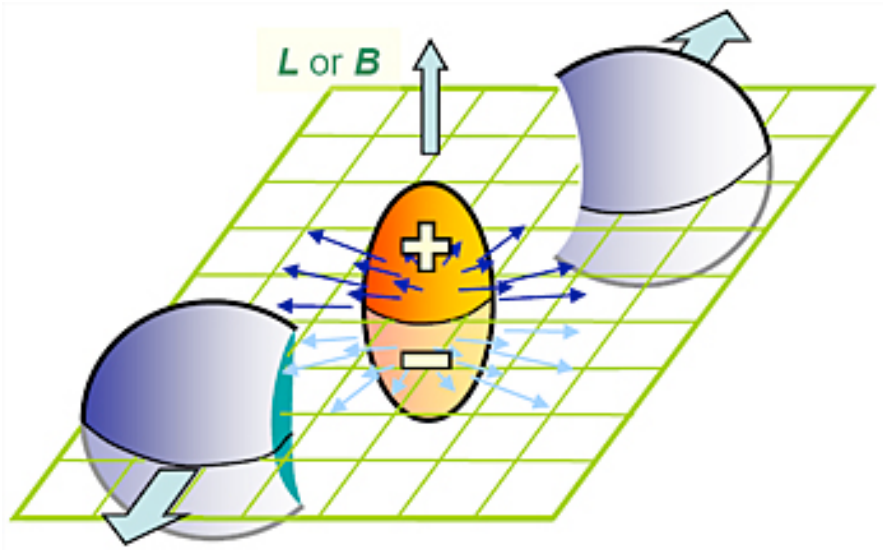
CVE

CME

**Microscopic quantum anomaly emerges as
macroscopic anomalous hydrodynamic currents!**

*It would be remarkable to actually “see” this new
hydrodynamics at work in real world materials!*

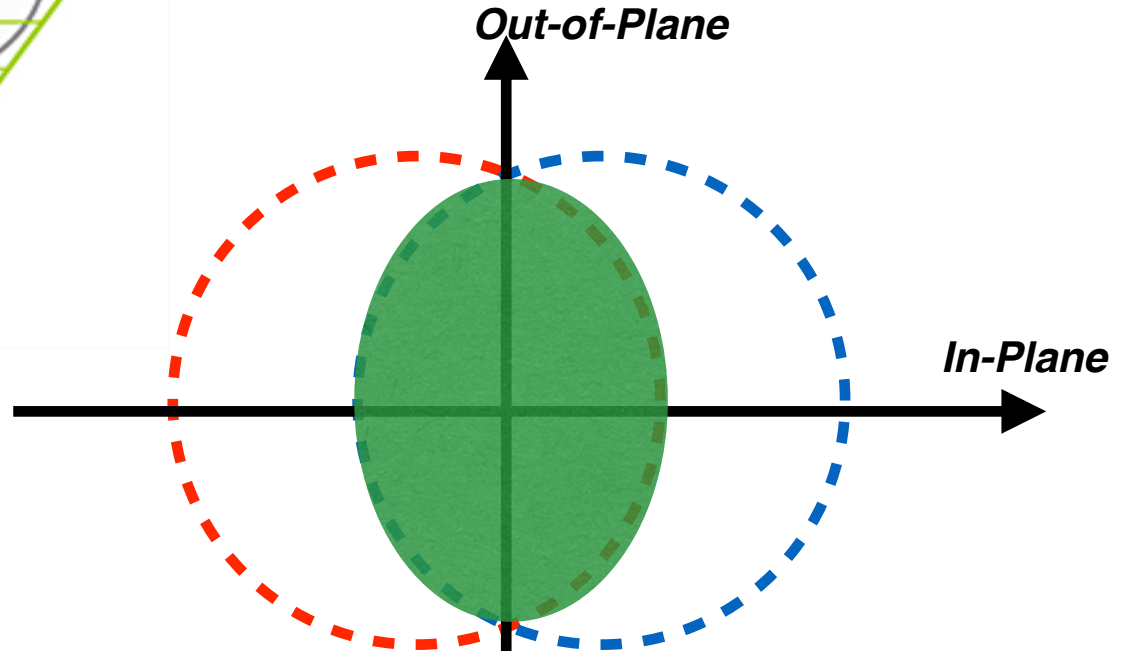
Looking for CME in Heavy Ion Collisions



The quark-gluon plasma is a subatomic CHIRAL MATTER.

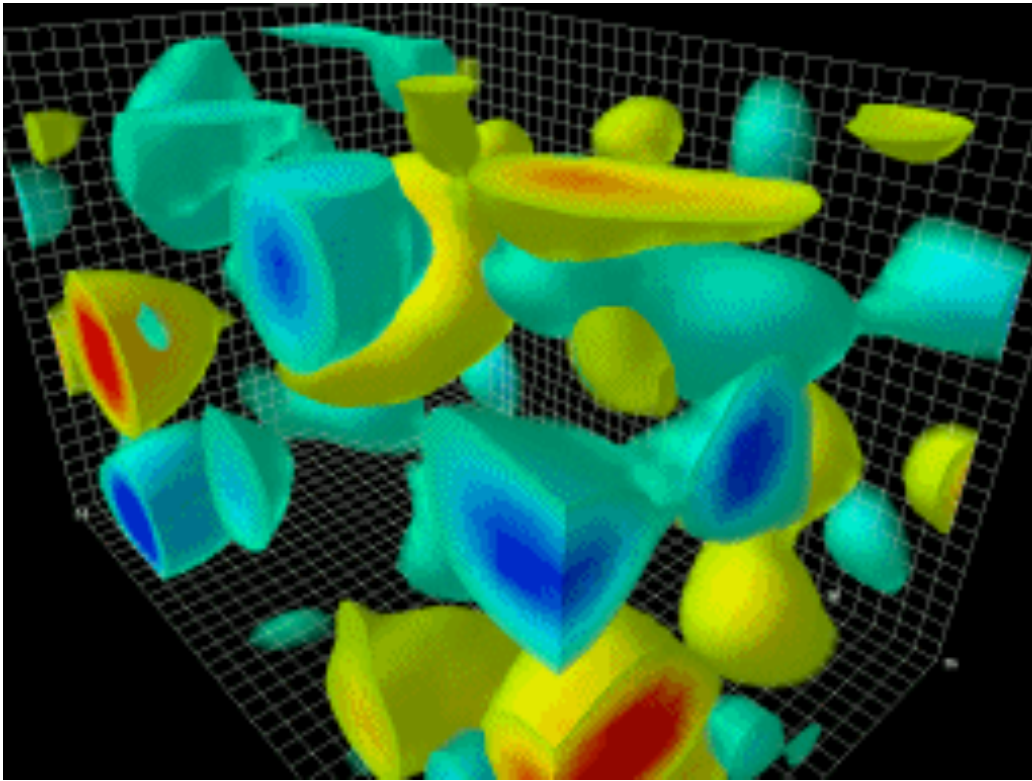
Can we observe CME in heavy ion collisions??

$$\vec{J} = \sigma_5 \mu_5 \vec{B}$$



- 1) (nearly) chiral quarks
- 2) chirality imbalance
- 3) strong magnetic field

From Gluon Topology to Quark Chirality



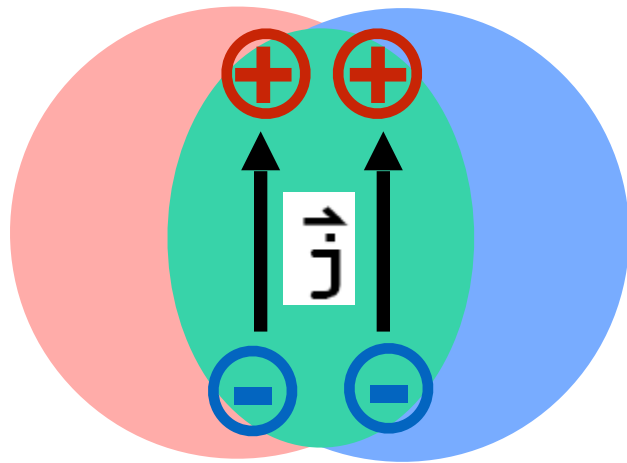
$$Q_w = \frac{1}{32\pi^2} \int d^4x (gG_a^{\mu\nu}) \cdot (g\tilde{G}_{\mu\nu}^a)$$

$$N_5(t \rightarrow +\infty) - N_5(t \rightarrow -\infty) = \frac{g^2}{16\pi^2} \int dt d^3\mathbf{r} G_a^{\mu\nu} \tilde{G}_{\mu\nu}^a$$

QCD anomaly: gluon topology \rightarrow chirality imbalance

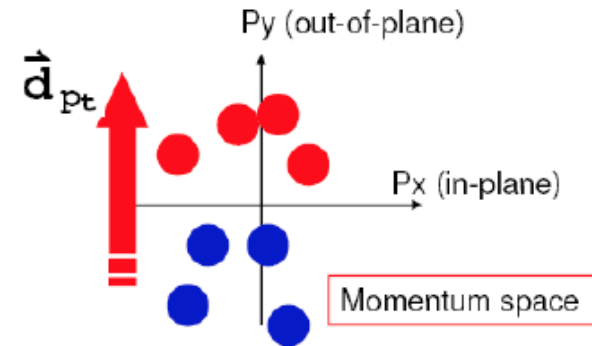
$$N_R - N_L = N_5 = 2Q_w$$

From CME Current to Charge Separation



$$\vec{J} = \sigma_5 \mu_5 \vec{B}$$

**strong radial blast:
position \rightarrow momentum**



**Charge Separation or
Electric Dipole in Pt Space
(along out-of-plane)**

[Kharzeev 2004; Kharzeev, McLerran, Warringa, 2008; ...]

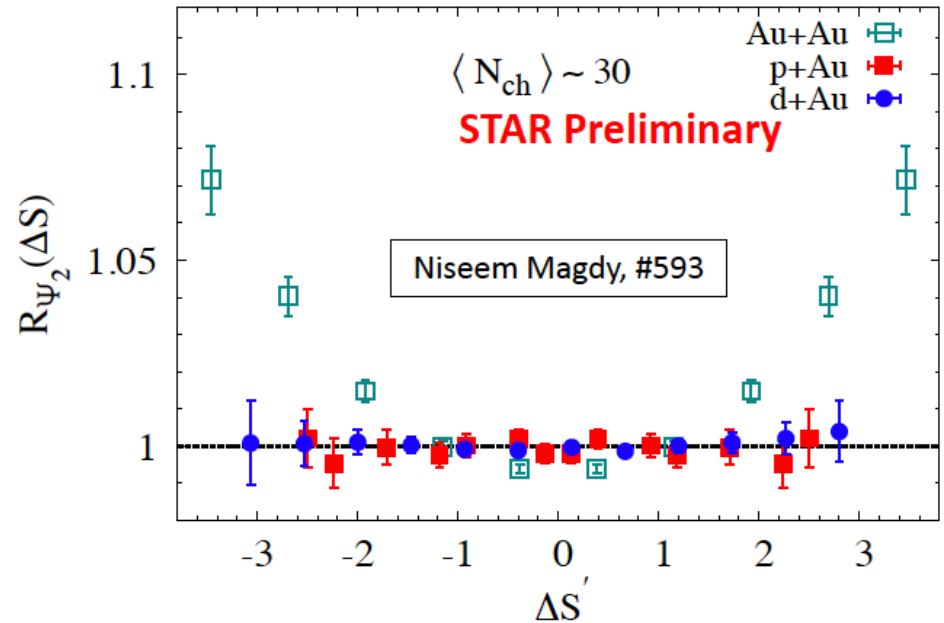
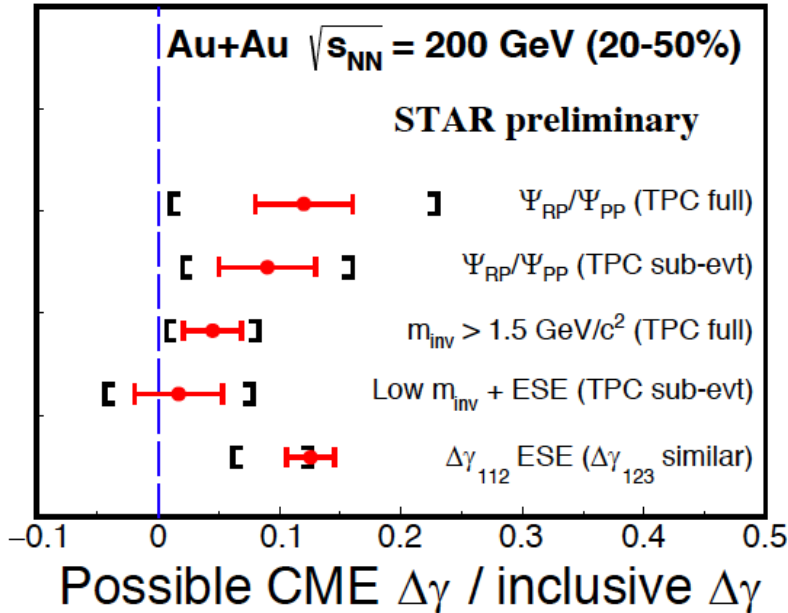
$$\frac{dN_{\pm}}{d\phi} \propto \dots + a_{\pm} \sin(\phi - \Psi_{RP})$$

$$\langle a_{\pm} \rangle \sim \pm \langle \mu_5 \rangle B$$

Very difficult measurement:

- * Zero average, only nonzero variance;
- * Correlation measurement with significant backgrounds;
- * Signal likely small

Latest Exp. Search Status



[From Z. Ye, STAR Summary Talk @ QM2018]

STAR @ RHIC 200GeV: “

naive” statistical interpretation: (8.5 +/- 1.2) %

ALICE @ LHC 2.76TeV: signal level possibly about 8~10%
(upper limit ~30%)

CMS @ LHC 5.02TeV: signal level no more than 7%

The trend with beam energy seems in line with expectation!

[arXiv:1611.04586](https://arxiv.org/abs/1611.04586)

Quantifying the chiral magnetic effect from anomalous-viscous fluid dynamics^{*}

Yin Jiang(姜寅)¹ Shuzhe Shi(施舒哲)² Yi Yin(尹伊)³ Jinfeng Liao(廖劲峰)^{2,4;1}

¹ School of Physics and Nuclear Energy Engineering, Beihang University, Beijing 100191, China

² Physics Department and Center for Exploration of Energy and Matter, Indiana University, 2401 N Milo B. Sampson Lane, Bloomington, IN 47408, USA

³ Center for Theoretical Physics, Massachusetts Institute of Technology, Cambridge, MA 02139, USA

⁴ Institute of Particle Physics and Key Laboratory of Quark & Lepton Physics (MOE), Central China Normal University, Wuhan 430079, China

Annals of Physics 394 (2018) 50–72

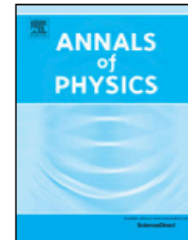
Contents lists available at ScienceDirect

Annals of Physics

journal homepage: www.elsevier.com/locate/aop



ELSEVIER



Anomalous chiral transport in heavy ion collisions from Anomalous-Viscous Fluid Dynamics



Shuzhe Shi^{a,*}, Yin Jiang^{b,c}, Elias Lilleskov^{d,a}, Jinfeng Liao^{a,e,*}

***Badly needed:
Quantitative
predictions for
CME signal in
heavy ion
collisions!***

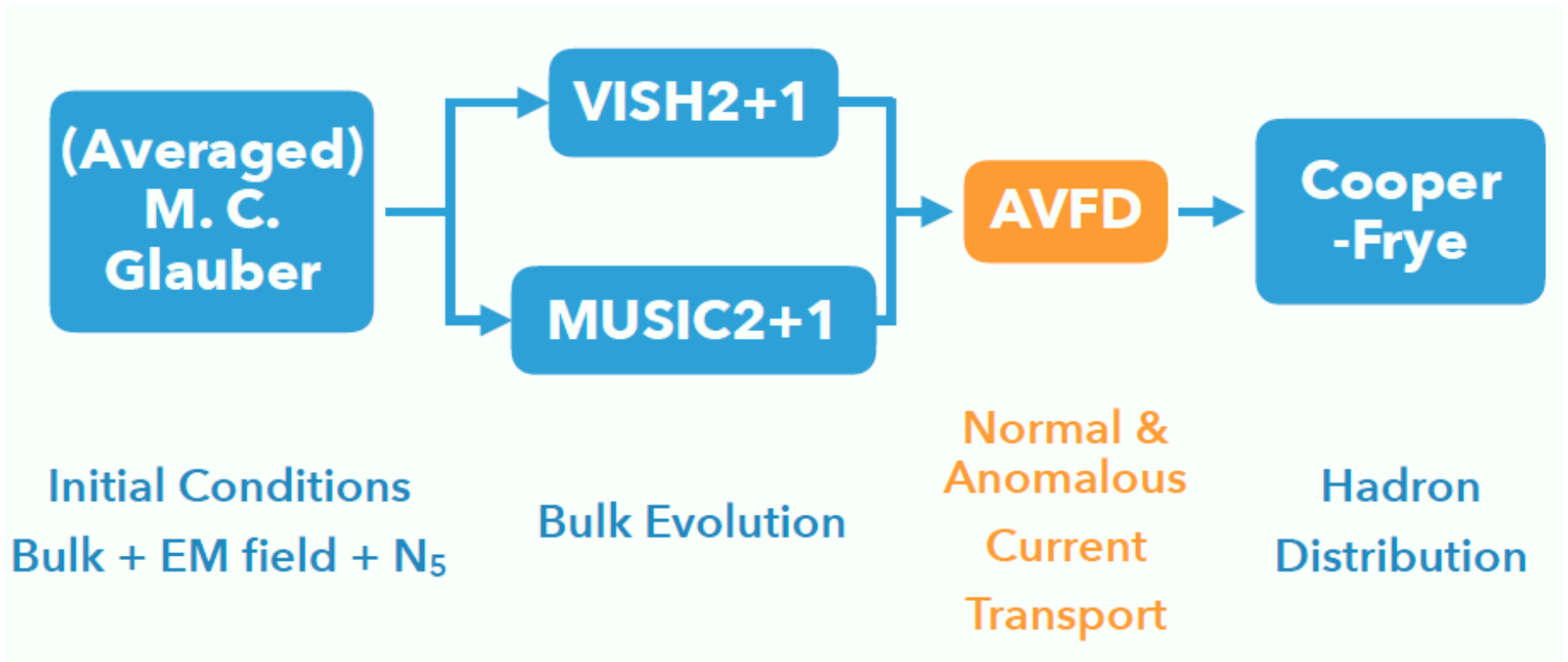
[arXiv:1711.02496](https://arxiv.org/abs/1711.02496)

Anomalous Viscous Fluid Dynamics (AVFD)



**AVFD:
Anomalous-Viscous Fluid Dynamics**

The AVFD Framework



We now have a versatile tool to quantitatively understand and answer many important questions about CME in heavy ion collisions!

arXiv:1611.04586

arXiv:1711.02496

The AVFD Framework

Anomalous-Viscous Fluid Dynamics

$$D_\mu J_R^\mu = + \frac{N_c q^2}{4\pi^2} E_\mu B^\mu \quad D_\mu J_L^\mu = - \frac{N_c q^2}{4\pi^2} E_\mu B^\mu$$

$$J_R^\mu = n_R u^\mu + v_R^\mu + \frac{N_c q}{4\pi^2} \mu_R B^\mu \quad \text{CME}$$

$$J_L^\mu = n_L u^\mu + v_L^\mu - \frac{N_c q}{4\pi^2} \mu_L B^\mu$$

Viscous Effect

$$\Delta^{\mu\nu} d v_{R,L}^\nu = - \frac{1}{\tau_{\text{rlx}}} (v_{R,L}^\mu - v_{\text{NS}}^\mu)$$

$$v_{\text{NS}}^\mu = \frac{\sigma}{2} T \Delta^{\mu\nu} \partial_\nu \frac{\mu}{T} + \frac{\sigma}{2} q E^\mu$$

on top of VISH2+1D -- OSU Group

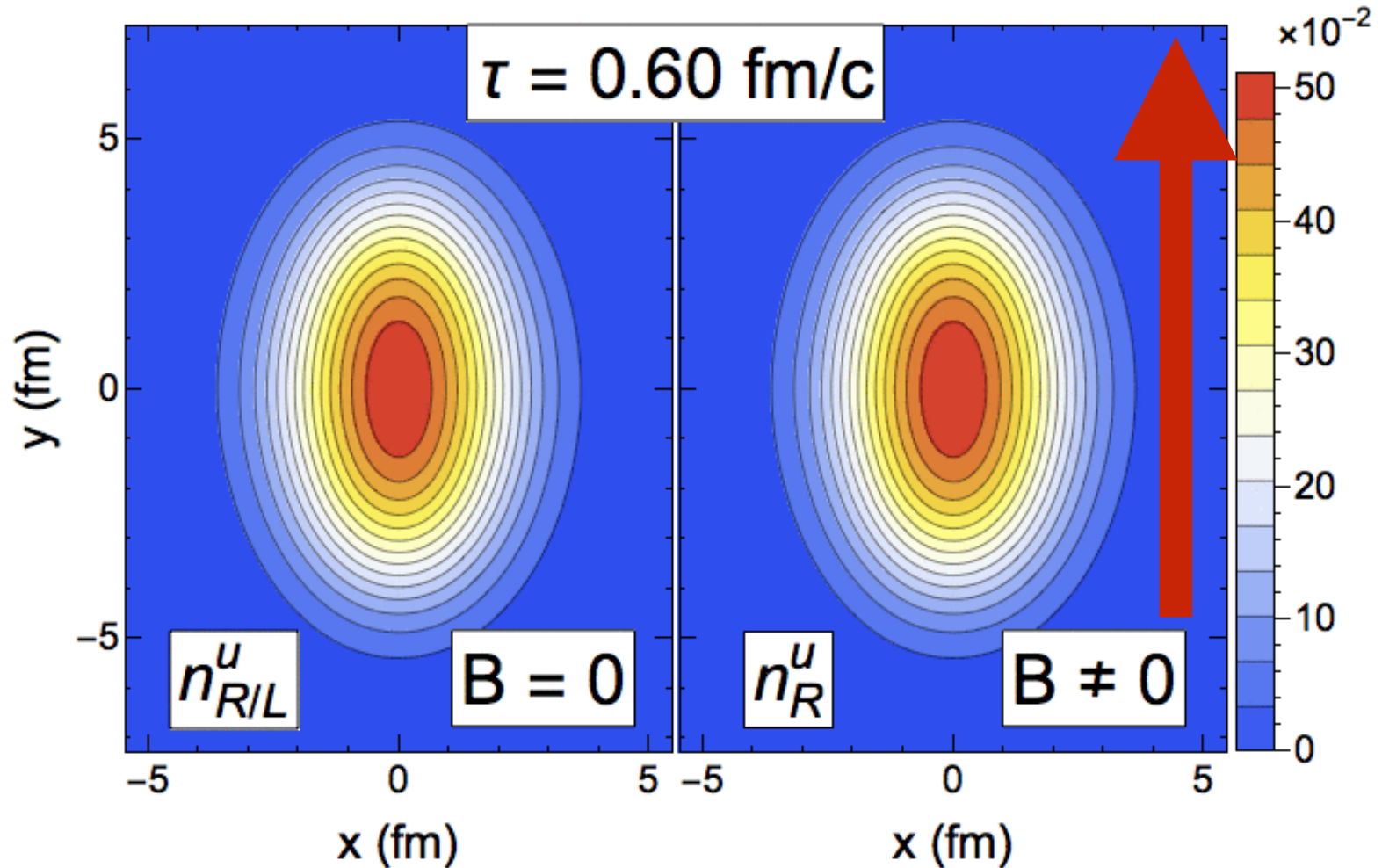
[We now also have MUSIC-AVFD!]

The AVFD At Work

[arXiv:1611.04586; arXiv:1711.02496]

Zero B Field

Nonzero B Field

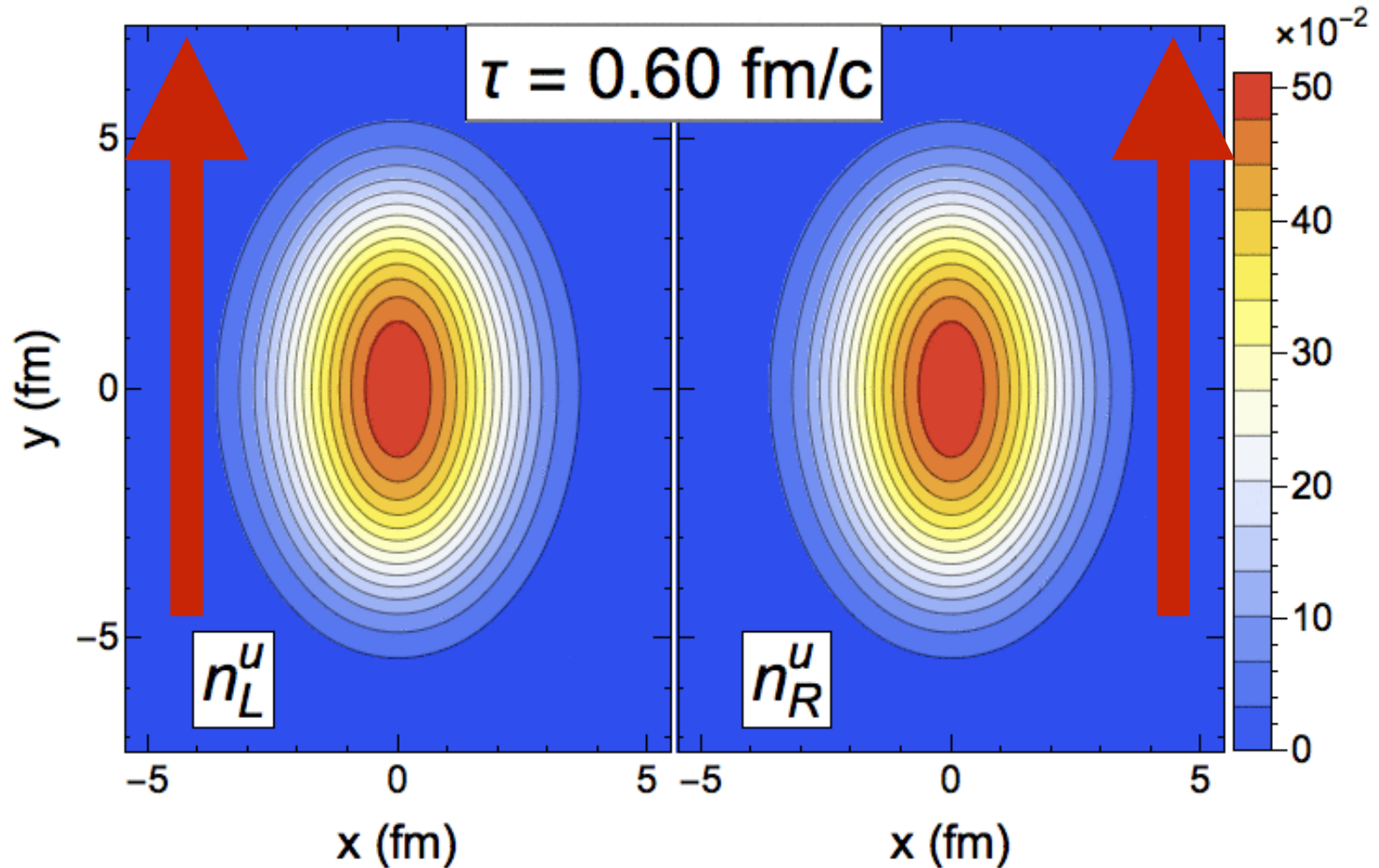


The AVFD At Work

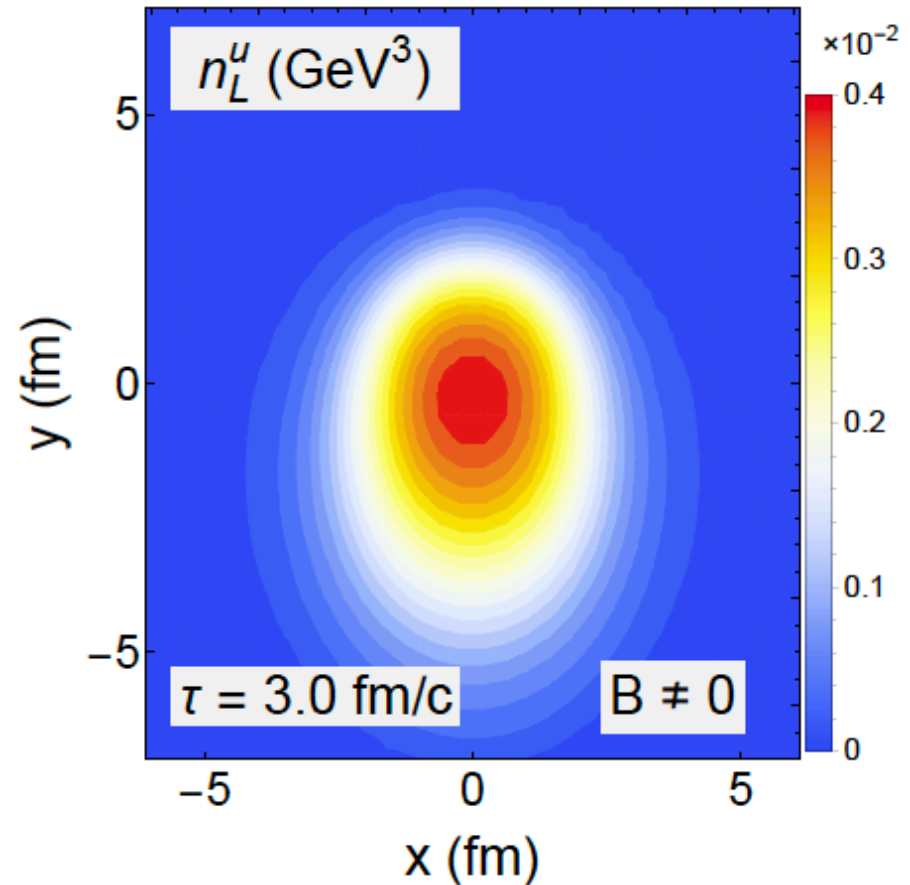
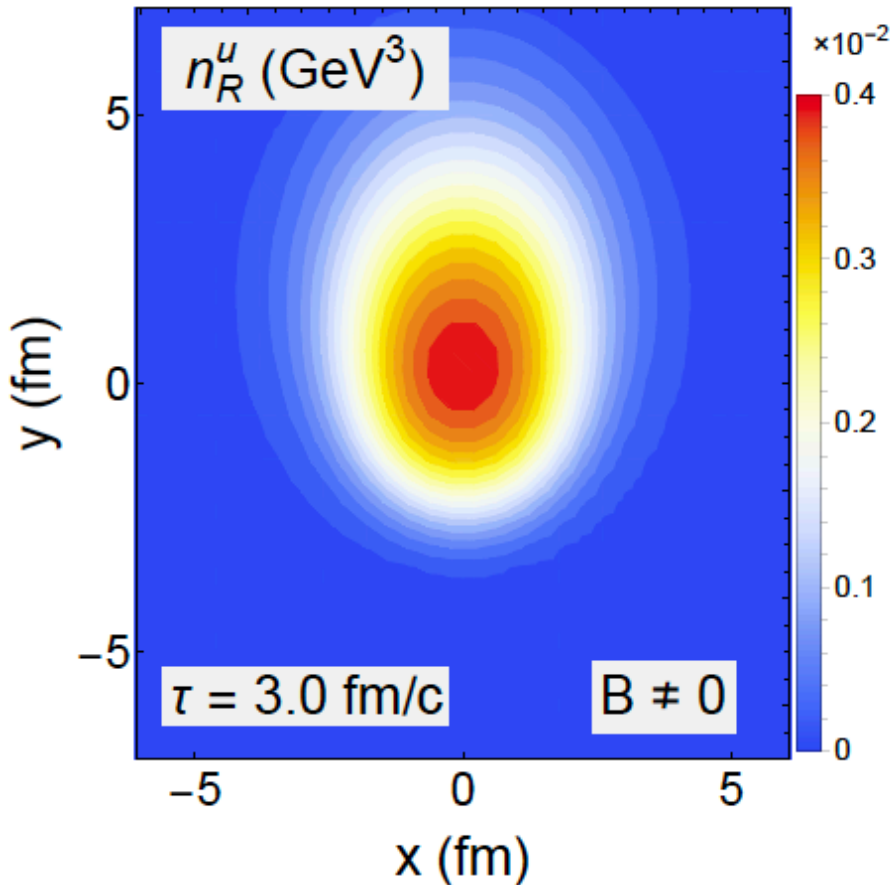
[arXiv:1611.04586; arXiv:1711.02496]

Left-handed

Right-handed



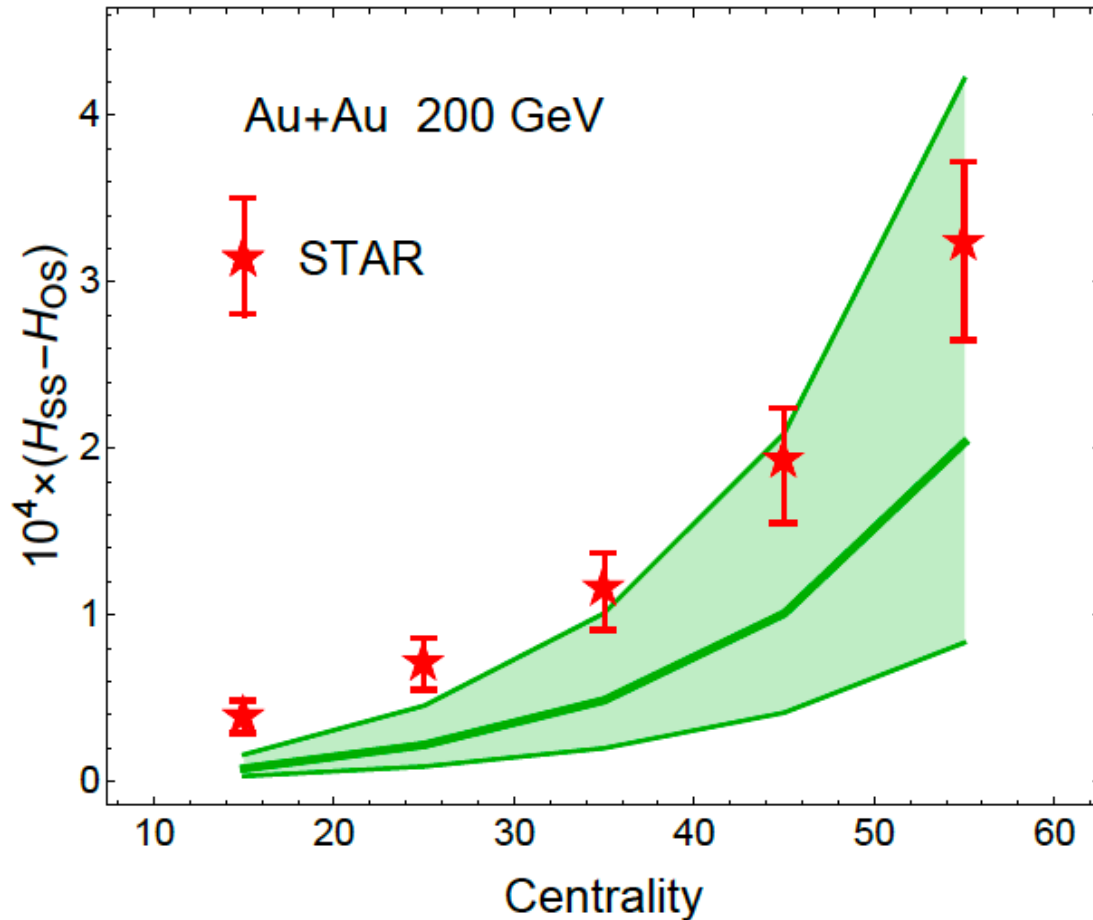
The Charge Separation from AVFD



B field $\otimes \mu_5 \Rightarrow$ current \Rightarrow dipole (charge separation)

$$dN_{\pm}/d\phi \propto 1 + 2 a_{1\pm} \sin(\phi - \psi_{RP}) + \dots$$

AVFD Predictions v.s Experimental Data



$$B(\tau) = \frac{B_0}{1 + (\tau/\tau_B)^2}$$

$$\tau_B = 0.6 \text{ fm}/c$$

$$\sqrt{\langle n_5^2 \rangle} \simeq \frac{Q_s^4 (\pi \rho_{tube}^2 \tau_0) \sqrt{N_{coll.}}}{16\pi^2 A_{overlap}}$$

Excellent agreement!

Shi, Jiang, JL, et al: arXiv:1611.04586 [CPC];
arXiv:1711.02496 [Annals of Physics]

Chiral Magnetic Wave (CMW)

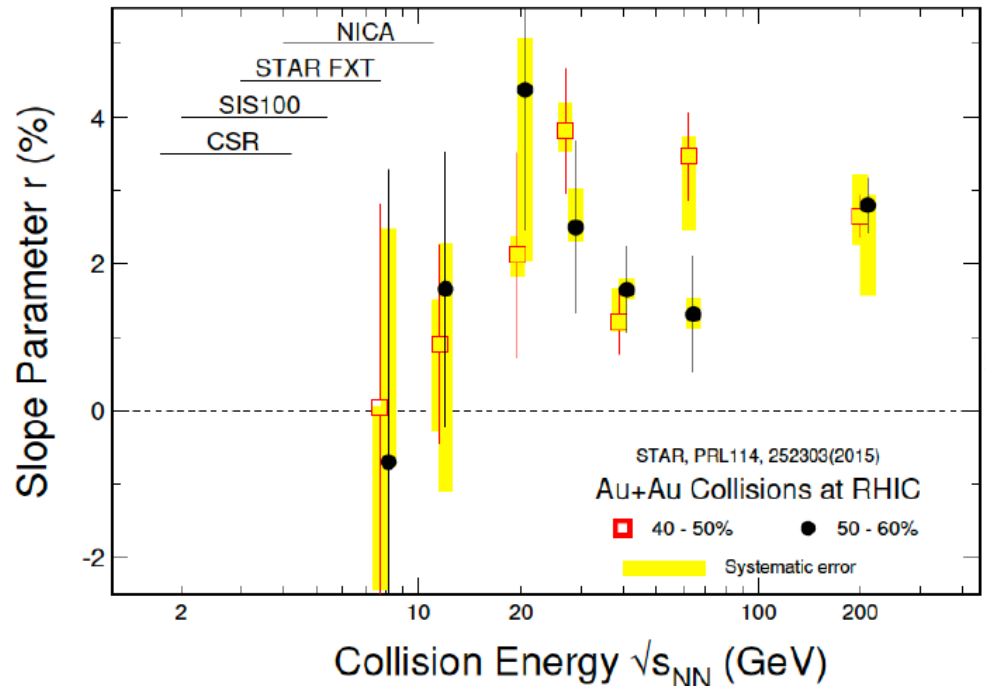
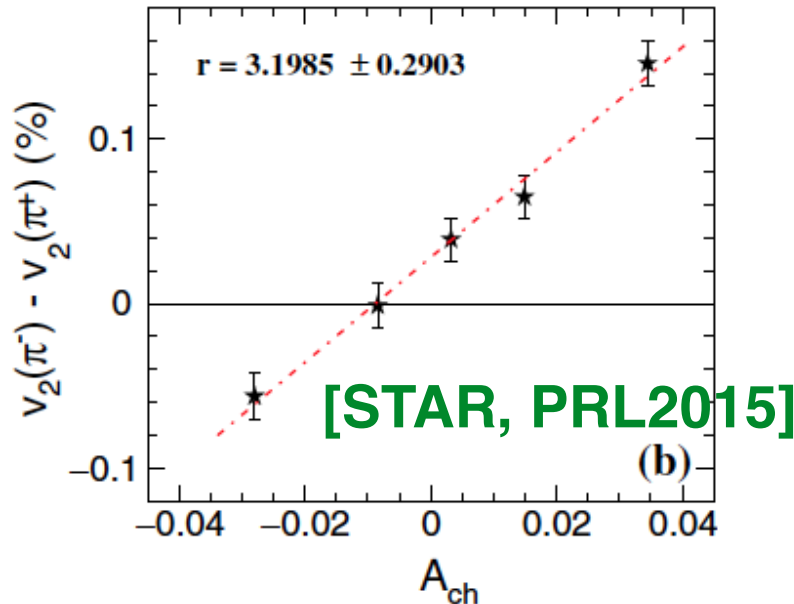
CMW: gapless collective excitation in chiral fluid

→ charge quadrupole of QGP → elliptic flow splitting

[Burnier, Kharzeev, JL, Yee, PRL2011;
& arXiv: 1208.2537]

$$v_2^- - v_2^+ = r_e A$$

**charge quadrupole
due to CMW transport**



[STAR@RHIC]

[Also seen by ALICE@LHC]

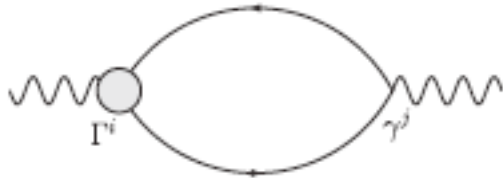
There Are Electric Fields Too!

Chiral matter in strong electric field:

Chiral Electric Separation Effect (CESE)

[Huang, JL, PRL2013; Jiang, Huang, Liao, PRD2014]

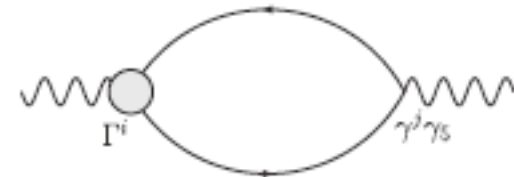
$$\mathbf{j}_A = \chi_e \mu_V \mu_A \mathbf{E},$$



$$\sigma_e = \chi_e \mu_V \mu_A$$

QED plasma

$$\sigma_e \approx \frac{T}{e^4 \ln(1/e)} \left(20.5 \frac{\mu_V \mu_A}{T^2} \right)$$



QCD plasma

$$\sigma_e \approx \frac{N_c N_f T}{g^4 \ln(1/g)} \left(4.83 \frac{\mu_V \mu_A}{T^2} \right)$$

Summary & Outlook

Summary: the Subatomic Swirls

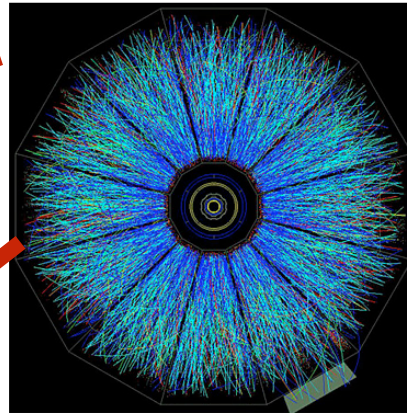
Quark-Gluon Plasma: A Subatomic Chiral Fluid

The new,
5th state of
matter

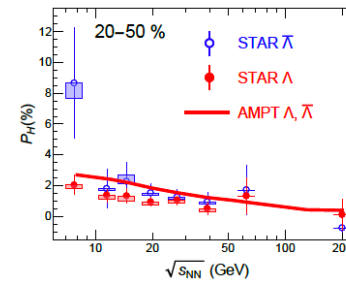
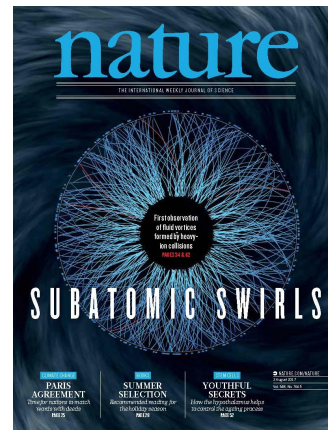
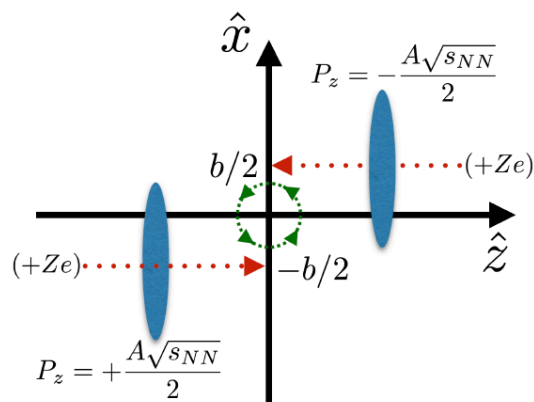
The oldest
state of matter:
early cosmos

The hottest
material

The most
perfect fluid



Subatomic swirls as
the most vortical fluid
with the strongest B field



Spin
Polarization

