

# Supplementary material to: Thermally-assisted-occupation density functional theory with generalized-gradient approximations

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## TABLES

TABLE S1. Non-hydrogen transfer barrier heights (in kcal/mol) of the NHTBH38/04 set [1].

Reactions	$\Delta E_{ref}$	KS-DFT				TAO-DFT				
		LDA	PBE	BLYP	BLYP-D	LDA	PBE	BLYP	BLYP-D	
<b>Heavy-atom transfer reactions</b>										
H + N <sub>2</sub> O → OH + N <sub>2</sub>	$V^f$	18.14	2.69	9.97	8.54	8.19	2.63	9.92	8.48	8.13
	$V^r$	83.22	32.09	52.46	61.67	61.24	37.21	53.40	62.92	62.48
H + FH → HF + H	$V^f$	42.18	18.48	27.07	26.03	25.76	18.57	27.14	26.10	25.83
	$V^r$	42.18	18.48	27.07	26.03	25.76	18.57	27.14	26.10	25.83
H + ClH → HCl + H	$V^f$	18.00	2.27	9.64	9.80	9.74	2.14	9.51	9.66	9.60
	$V^r$	18.00	2.27	9.64	9.80	9.74	2.14	9.51	9.66	9.60
H + FCH <sub>3</sub> → HF + CH <sub>3</sub>	$V^f$	30.38	13.36	18.51	16.12	15.33	13.36	18.52	16.12	15.33
	$V^r$	57.02	31.72	41.00	42.27	41.33	31.62	40.88	42.14	41.21
H + F <sub>2</sub> → HF + F	$V^f$	2.27	-15.97	-9.86	-11.66	-11.78	-16.13	-9.98	-11.79	-11.91
	$V^r$	106.18	69.40	80.86	82.15	82.02	77.32	82.70	84.15	84.03
CH <sub>3</sub> + FCl → CH <sub>3</sub> F + Cl	$V^f$	7.43	-11.50	-6.48	-6.97	-8.45	-11.93	-6.78	-7.30	-8.78
	$V^r$	60.17	37.67	41.63	41.76	40.43	46.51	47.37	48.19	46.85
<b>Nucleophilic substitution reactions</b>										
F <sup>-</sup> + CH <sub>3</sub> F → FCH <sub>3</sub> + F <sup>-</sup>	$V^f$	-0.34	-12.18	-8.31	-7.90	-8.95	-12.39	-8.51	-8.10	-9.15
	$V^r$	-0.34	-12.18	-8.31	-7.90	-8.95	-12.39	-8.51	-8.10	-9.15
F <sup>-</sup> ...CH <sub>3</sub> F → FCH <sub>3</sub> ...F <sup>-</sup>	$V^f$	13.38	6.55	7.06	6.50	6.84	6.45	6.96	6.40	6.74
	$V^r$	13.38	6.55	7.06	6.50	6.84	6.45	6.96	6.40	6.74
Cl <sup>-</sup> + CH <sub>3</sub> Cl → ClCH <sub>3</sub> + Cl <sup>-</sup>	$V^f$	3.10	-6.74	-3.80	-3.95	-5.69	-7.07	-4.13	-4.30	-6.03
	$V^r$	3.10	-6.74	-3.80	-3.95	-5.69	-7.07	-4.13	-4.30	-6.03
Cl <sup>-</sup> ...CH <sub>3</sub> Cl → ClCH <sub>3</sub> ...Cl <sup>-</sup>	$V^f$	13.61	6.74	7.15	5.72	5.55	6.66	7.07	5.65	5.48
	$V^r$	13.61	6.74	7.15	5.72	5.55	6.66	7.07	5.65	5.48
F <sup>-</sup> + CH <sub>3</sub> Cl → FCH <sub>3</sub> + Cl <sup>-</sup>	$V^f$	-12.54	-23.45	-19.52	-19.35	-20.67	-23.59	-19.65	-19.47	-20.79
	$V^r$	20.11	10.10	12.31	13.03	11.62	9.68	11.90	12.61	11.19
F <sup>-</sup> ...CH <sub>3</sub> Cl → FCH <sub>3</sub> ...Cl <sup>-</sup>	$V^f$	2.89	-1.04	-0.67	-1.65	-1.54	-1.07	-0.70	-1.68	-1.57
	$V^r$	29.62	21.65	21.45	21.03	21.08	21.49	21.29	20.87	20.92
OH <sup>-</sup> + CH <sub>3</sub> F → HOCH <sub>3</sub> + F <sup>-</sup>	$V^f$	-2.78	-14.36	-10.59	-9.77	-11.56	-14.57	-10.74	-9.90	-11.69
	$V^r$	17.33	5.70	9.14	9.07	7.79	5.60	9.06	9.00	7.72
OH <sup>-</sup> ...CH <sub>3</sub> F → HOCH <sub>3</sub> ...F <sup>-</sup>	$V^f$	10.96	3.39	3.88	3.73	3.17	3.27	3.85	3.73	3.17
	$V^r$	47.20	47.53	43.21	40.24	39.70	47.58	43.28	40.31	39.77
<b>Unimolecular and association reactions</b>										
H + N <sub>2</sub> → HN <sub>2</sub>	$V^f$	14.69	-2.19	5.19	5.24	5.08	-2.35	5.04	5.09	4.92
	$V^r$	10.72	9.44	9.08	8.51	8.38	9.60	9.19	8.61	8.48
H + CO → HCO	$V^f$	3.17	-7.57	-1.69	-1.95	-2.25	-7.71	-1.83	-2.09	-2.39
	$V^r$	22.68	26.34	24.66	23.34	23.13	26.54	24.81	23.49	23.28
H + C <sub>2</sub> H <sub>4</sub> → CH <sub>3</sub> CH <sub>2</sub>	$V^f$	1.72	-5.34	-0.14	-0.69	-1.78	-5.46	-0.27	-0.81	-1.90
	$V^r$	41.75	39.21	40.20	38.11	37.63	39.37	40.35	38.27	37.78
CH <sub>3</sub> + C <sub>2</sub> H <sub>4</sub> → CH <sub>3</sub> CH <sub>2</sub> CH <sub>2</sub>	$V^f$	6.85	-5.81	1.50	4.72	1.48	-6.13	1.18	4.39	1.15
	$V^r$	32.97	32.95	29.76	24.88	24.13	33.08	29.90	25.02	24.27
HCN → HNC	$V^f$	48.16	44.83	45.60	46.76	46.94	44.89	45.66	46.81	46.99
	$V^r$	33.11	30.60	30.50	31.68	31.80	30.60	30.50	31.68	31.80
MSE			-12.41	-8.52	-8.69	-9.32	-11.93	-8.38	-8.52	-9.15
MAE			12.62	8.62	8.72	9.35	12.15	8.49	8.56	9.19
rms			16.13	10.61	10.27	10.83	15.09	10.28	9.90	10.46

Max(-)	-51.13	-30.76	-24.03	-24.16	-46.01	-29.82	-22.03	-22.15
Max(+)	3.66	1.98	0.66	0.45	3.86	2.13	0.81	0.60

TABLE S2. Hydrogen transfer barrier heights (in kcal/mol) of the HTBH38/04 set [1].

Reactions	$\Delta E_{ref}$	KS-DFT				TAO-DFT				
		LDA	PBE	BLYP	BLYP-D	LDA	PBE	BLYP	BLYP-D	
H + HCl $\rightarrow$ H <sub>2</sub> + Cl	$V^f$	5.7	-3.14	0.56	-2.45	-2.58	-3.68	0.17	-2.89	-3.02
	$V^r$	8.7	-11.27	-1.95	1.84	1.71	-2.70	3.54	7.98	7.86
OH + H <sub>2</sub> $\rightarrow$ H + H <sub>2</sub> O	$V^f$	5.1	-18.39	-6.36	-3.49	-3.95	-13.65	-5.61	-2.43	-2.89
	$V^r$	21.2	11.33	13.69	10.39	9.96	10.88	13.44	10.13	9.70
CH <sub>3</sub> + H <sub>2</sub> $\rightarrow$ H + CH <sub>4</sub>	$V^f$	12.1	-5.35	3.82	7.14	5.96	-5.58	3.59	6.91	5.73
	$V^r$	15.3	4.94	9.32	7.65	6.61	4.87	9.24	7.58	6.54
OH + CH <sub>4</sub> $\rightarrow$ CH <sub>3</sub> + H <sub>2</sub> O	$V^f$	6.7	-17.22	-5.65	-2.75	-4.01	-12.41	-4.87	-1.64	-2.92
	$V^r$	19.6	2.21	8.91	10.63	9.24	1.68	8.52	10.24	8.86
H + H <sub>2</sub> $\rightarrow$ H <sub>2</sub> + H	$V^f$	9.6	-2.70	3.64	2.86	2.67	-2.80	3.53	2.76	2.57
	$V^r$	9.6	-2.70	3.64	2.86	2.67	-2.80	3.53	2.76	2.57
OH + NH <sub>3</sub> $\rightarrow$ H <sub>2</sub> O + NH <sub>2</sub>	$V^f$	3.2	-23.88	-11.94	-9.20	-10.46	-19.22	-11.26	-8.21	-9.47
	$V^r$	12.7	-10.71	-0.71	1.81	0.47	-11.30	-1.14	1.38	0.04
HCl + CH <sub>3</sub> $\rightarrow$ Cl + CH <sub>4</sub>	$V^f$	1.7	-13.74	-5.94	-3.51	-5.09	-14.16	-6.30	-3.88	-5.46
	$V^r$	7.9	-11.58	-2.95	1.29	-0.15	-2.73	2.73	7.66	6.22
OH + C <sub>2</sub> H <sub>6</sub> $\rightarrow$ H <sub>2</sub> O + C <sub>2</sub> H <sub>5</sub>	$V^f$	3.4	-20.98	-9.03	-6.12	-7.54	-16.17	-8.26	-5.02	-6.45
	$V^r$	19.9	4.79	10.76	12.36	10.26	4.26	10.37	11.97	9.87
F + H <sub>2</sub> $\rightarrow$ HF + H	$V^f$	1.8	-24.20	-12.97	-11.61	-11.86	-17.16	-11.52	-9.97	-10.22
	$V^r$	33.4	25.71	25.12	20.70	20.45	24.80	24.73	20.32	20.07
O + CH <sub>4</sub> $\rightarrow$ OH + CH <sub>3</sub>	$V^f$	13.7	-10.69	-0.79	1.44	0.52	-9.95	-1.14	1.20	-0.17
	$V^r$	8.1	-9.27	-0.57	1.68	0.61	-9.32	-0.68	1.50	0.46
H + PH <sub>3</sub> $\rightarrow$ PH <sub>2</sub> + H <sub>2</sub>	$V^f$	3.1	-7.35	-1.79	-2.63	-3.14	-7.46	-1.90	-2.73	-3.24
	$V^r$	23.2	9.24	17.91	21.58	20.38	9.02	17.68	21.34	20.15
H + HO $\rightarrow$ H <sub>2</sub> + O	$V^f$	10.7	-1.69	3.75	1.60	1.48	-1.55	3.84	1.66	1.58
	$V^r$	13.1	-13.40	-1.98	0.86	0.74	-12.63	-2.27	0.69	0.13
H + H <sub>2</sub> S $\rightarrow$ H <sub>2</sub> + HS	$V^f$	3.5	-6.73	-1.22	-2.20	-2.59	-7.03	-1.42	-2.48	-2.86
	$V^r$	17.3	-0.86	9.10	14.00	13.36	4.93	12.53	18.07	17.43
O + HCl $\rightarrow$ OH + Cl	$V^f$	9.8	-23.13	-10.54	-8.78	-8.86	-19.48	-10.85	-8.75	-9.32
	$V^r$	10.4	-19.55	-7.33	-3.75	-3.83	-7.42	-1.36	3.09	3.00
NH <sub>2</sub> + CH <sub>3</sub> $\rightarrow$ CH <sub>4</sub> + NH	$V^f$	8.0	-8.37	0.71	3.57	1.82	-8.62	0.43	3.28	1.53
	$V^r$	22.4	2.16	10.56	13.31	11.66	1.93	10.34	13.09	11.44
NH <sub>2</sub> + C <sub>2</sub> H <sub>5</sub> $\rightarrow$ C <sub>2</sub> H <sub>6</sub> + NH	$V^f$	7.5	-5.76	2.89	5.94	3.56	-6.02	2.60	5.64	3.26
	$V^r$	18.3	-1.57	7.51	10.59	8.87	-1.81	7.27	10.34	8.62
C <sub>2</sub> H <sub>6</sub> + NH <sub>2</sub> $\rightarrow$ NH <sub>3</sub> + C <sub>2</sub> H <sub>5</sub>	$V^f$	10.4	-9.69	1.44	5.25	3.08	-9.91	1.18	4.99	2.82
	$V^r$	17.4	2.91	9.99	12.72	9.94	2.60	9.68	12.40	9.62
NH <sub>2</sub> + CH <sub>4</sub> $\rightarrow$ CH <sub>3</sub> + NH <sub>3</sub>	$V^f$	14.5	-6.16	4.39	7.99	6.04	-6.37	4.15	7.75	5.80
	$V^r$	17.8	0.10	7.71	10.35	8.37	-0.20	7.41	10.05	8.06
<i>s-trans cis</i> -C <sub>5</sub> H <sub>8</sub> $\rightarrow$ <i>s-trans cis</i> -C <sub>5</sub> H <sub>8</sub>	$V^f$	38.4	24.99	31.19	35.82	34.69	24.88	31.08	35.70	34.58
	$V^r$	38.4	24.99	31.19	35.82	34.69	24.88	31.08	35.70	34.58
MSE		-17.90	-9.67	-7.84	-8.89	-16.34	-9.20	-7.25	-8.33	
MAE		17.90	9.67	7.84	8.89	16.34	9.20	7.29	8.34	
rms		18.92	10.37	8.66	9.52	17.06	9.87	8.24	9.17	
Max(-)		-32.93	-20.34	-18.58	-18.66	-29.28	-20.65	-18.55	-19.12	
Max(+)		-7.69	-4.61	-1.56	-2.82	-8.60	-4.77	0.77	0.13	

TABLE S3. Interaction energies (in kcal/mol) of the S22 set [2]. The counterpoise corrections are used to reduce the basis set superposition errors. Monomer deformation energies are not included.

Complex [Symmetry]	$\Delta E_{ref}$	KS-DFT				TAO-DFT			
		LDA	PBE	BLYP	BLYP-D	LDA	PBE	BLYP	BLYP-D
<b>Hydrogen bonded complexes</b>									
(NH <sub>3</sub> ) <sub>2</sub> [C <sub>2h</sub> ]	-3.17	-5.10	-2.83	-1.78	-3.44	-5.27	-3.00	-1.96	-3.63
(H <sub>2</sub> O) <sub>2</sub> [C <sub>s</sub> ]	-5.02	-7.78	-4.91	-3.99	-4.92	-7.95	-5.09	-4.18	-5.11
Formic acid dimer [C <sub>2h</sub> ]	-18.61	-26.82	-18.08	-15.48	-18.50	-27.22	-18.49	-15.89	-18.91
Formamide dimer [C <sub>2h</sub> ]	-15.96	-21.82	-14.69	-12.44	-15.63	-22.21	-15.08	-12.85	-16.03
Uracil dimer [C <sub>2h</sub> ]	-20.65	-26.15	-18.45	-16.21	-20.21	-26.51	-18.82	-16.59	-20.59
2-pyridoxine-2-aminopyridine [C <sub>1</sub> ]	-16.71	-22.77	-15.27	-12.51	-17.28	-23.18	-15.68	-12.94	-17.71
Adenine-thymine WC [C <sub>1</sub> ]	-16.37	-21.99	-14.28	-11.42	-16.50	-22.43	-14.73	-11.88	-16.96
MSE		-5.13	1.14	3.24	0.00	-5.47	0.80	2.89	-0.35
MAE		5.13	1.14	3.24	0.28	5.47	0.82	2.89	0.37
<b>Dispersion complexes</b>									
(CH <sub>4</sub> ) <sub>2</sub> [D <sub>3d</sub> ]	-0.53	-0.83	-0.08	0.68	-0.31	-0.95	-0.20	0.55	-0.44
(C <sub>2</sub> H <sub>4</sub> ) <sub>2</sub> [D <sub>2d</sub> ]	-1.51	-2.49	-0.31	1.12	-1.44	-2.71	-0.54	0.89	-1.68
Benzene-CH <sub>4</sub> [C <sub>3</sub> ]	-1.50	-2.01	-0.01	1.39	-1.23	-2.21	-0.22	1.17	-1.45
Benzene dimer [C <sub>2h</sub> ]	-2.73	-2.62	1.90	4.94	-1.93	-3.03	1.49	4.50	-2.36
Pyrazine dimer [C <sub>s</sub> ]	-4.42	-4.46	0.73	3.80	-3.65	-4.86	0.32	3.36	-4.09
Uracil dimer [C <sub>2</sub> ]	-10.12	-10.15	-2.69	1.13	-9.68	-10.66	-3.21	0.58	-10.24
Indole-benzene [C <sub>1</sub> ]	-5.22	-4.38	2.24	6.32	-3.92	-4.90	1.71	5.76	-4.47
Adenine-thymine stack [C <sub>1</sub> ]	-12.23	-11.96	-1.33	4.06	-11.81	-12.63	-2.01	3.35	-12.52
MSE		-0.08	4.84	7.71	0.54	-0.46	4.45	7.30	0.13
MAE		0.38	4.84	7.71	0.54	0.54	4.45	7.30	0.27
<b>Mixed complexes</b>									
Ethene-ethine [C <sub>2v</sub> ]	-1.53	-2.27	-1.16	-0.29	-1.49	-2.41	-1.30	-0.45	-1.64
Benzene-H <sub>2</sub> O [C <sub>s</sub> ]	-3.28	-4.44	-2.04	-0.49	-3.29	-4.67	-2.27	-0.74	-3.54
Benzene-NH <sub>3</sub> [C <sub>s</sub> ]	-2.35	-3.03	-0.92	0.55	-2.18	-3.24	-1.14	0.31	-2.42
Benzene-HCN [C <sub>s</sub> ]	-4.46	-5.85	-2.81	-0.94	-4.65	-6.09	-3.05	-1.19	-4.91
Benzene dimer [C <sub>2v</sub> ]	-2.74	-3.06	-0.10	1.86	-2.51	-3.33	-0.38	1.57	-2.81
Indole-benzene T-shape [C <sub>1</sub> ]	-5.73	-6.26	-2.02	0.69	-5.67	-6.63	-2.39	0.30	-6.05
Phenol dimer [C <sub>1</sub> ]	-7.05	-9.01	-3.86	-1.75	-6.65	-9.34	-4.20	-2.10	-7.00
MSE		-0.97	2.03	3.83	0.10	-1.22	1.77	3.55	-0.18
MAE		0.97	2.03	3.83	0.16	1.22	1.77	3.55	0.19
MSE		-1.97	2.77	5.05	0.23	-2.30	2.44	4.70	-0.12
MAE		2.08	2.77	5.05	0.33	2.33	2.44	4.70	0.28
rms		3.18	3.89	6.31	0.45	3.40	3.57	5.95	0.37
Max(-)		-8.21	0.11	1.03	-0.57	-8.61	-0.07	0.84	-1.00
Max(+)		0.84	10.90	16.29	1.30	0.32	10.22	15.58	0.75

TABLE S4. Comparison of errors (in kcal/mol) of the reaction energies (in kcal/mol) of the 30 chemical reactions in the NHTBH38/04 and HTBH38/04 sets [1].

Reactions	$\Delta E_{ref}$	KS-DFT				TAO-DFT			
		LDA	PBE	BLYP	BLYP-D	LDA	PBE	BLYP	BLYP-D
H + N <sub>2</sub> O → OH + N <sub>2</sub>	-65.08	35.68	22.59	11.96	12.03	30.50	21.60	10.65	10.73
H + FCH <sub>3</sub> → HF + CH <sub>3</sub>	-26.64	8.28	4.16	0.49	0.63	8.39	4.28	0.62	0.77
H + F <sub>2</sub> → HF + F	-103.91	18.54	13.19	10.10	10.10	10.46	11.23	7.97	7.97
CH <sub>3</sub> + FCl → CH <sub>3</sub> F + Cl	-52.74	3.57	4.64	4.01	3.86	-5.71	-1.41	-2.75	-2.89
F <sup>-</sup> + CH <sub>3</sub> Cl → FCH <sub>3</sub> + Cl <sup>-</sup>	-32.65	-0.90	0.82	0.27	0.37	-0.62	1.11	0.57	0.67

$F^- \cdots CH_3Cl \rightarrow FCH_3 \cdots Cl^-$	-26.73	4.05	4.61	4.05	4.11	4.18	4.73	4.17	4.24
$OH^- + CH_3F \rightarrow HOCH_3 + F^-$	-20.11	0.05	0.38	1.27	0.75	-0.07	0.30	1.21	0.70
$OH^- \cdots CH_3F \rightarrow HOCH_3 \cdots F^-$	-36.24	-7.90	-3.09	-0.27	-0.29	-8.07	-3.19	-0.34	-0.36
$H + N_2 \rightarrow HN_2$	3.97	-15.60	-7.86	-7.24	-7.28	-15.92	-8.12	-7.49	-7.53
$H + CO \rightarrow HCO$	-19.51	-14.40	-6.84	-5.78	-5.87	-14.74	-7.13	-6.07	-6.16
$H + C_2H_4 \rightarrow CH_3CH_2$	-40.03	-4.52	-0.31	1.22	0.62	-4.79	-0.59	0.95	0.34
$CH_3 + C_2H_4 \rightarrow CH_3CH_2CH_2$	-26.12	-12.64	-2.14	5.96	3.47	-13.09	-2.60	5.49	2.99
$HCN \rightarrow HNC$	15.05	-0.83	0.06	0.02	0.09	-0.77	0.12	0.08	0.14
$H + HCl \rightarrow H_2 + Cl$	-3.0	11.13	5.51	-1.29	-1.29	2.01	-0.37	-7.87	-7.87
$OH + H_2 \rightarrow H + H_2O$	-16.1	-13.62	-3.95	2.22	2.19	-8.43	-2.95	3.55	3.51
$CH_3 + H_2 \rightarrow H + CH_4$	-3.2	-7.09	-2.30	2.70	2.55	-7.25	-2.45	2.53	2.39
$OH + CH_4 \rightarrow CH_3 + H_2O$	-12.9	-6.53	-1.65	-0.48	-0.36	-1.19	-0.49	1.02	1.13
$OH + NH_3 \rightarrow H_2O + NH_2$	-9.5	-3.67	-1.73	-1.51	-1.43	1.58	-0.63	-0.08	-0.01
$HCl + CH_3 \rightarrow Cl + CH_4$	-6.2	4.04	3.21	1.41	1.26	-5.23	-2.83	-5.34	-5.48
$OH + C_2H_6 \rightarrow H_2O + C_2H_5$	-16.5	-9.27	-3.29	-1.97	-1.30	-3.93	-2.13	-0.49	0.19
$F + H_2 \rightarrow HF + H$	-31.6	-18.31	-6.49	-0.72	-0.72	-10.36	-4.65	1.30	1.30
$O + CH_4 \rightarrow OH + CH_3$	5.6	-7.02	-5.83	-5.84	-5.69	-6.23	-6.06	-5.90	-6.23
$H + PH_3 \rightarrow PH_2 + H_2$	-20.1	3.51	0.40	-4.10	-3.42	3.63	0.52	-3.98	-3.29
$H + HO \rightarrow H_2 + O$	-2.4	14.11	8.12	3.14	3.14	13.48	8.52	3.37	3.84
$H + H_2S \rightarrow H_2 + HS$	-13.8	7.93	3.48	-2.41	-2.15	1.84	-0.15	-6.74	-6.49
$O + HCl \rightarrow OH + Cl$	-0.6	-2.98	-2.61	-4.43	-4.43	-11.46	-8.89	-11.24	-11.71
$NH_2 + CH_3 \rightarrow CH_4 + NH$	-14.4	3.87	4.55	4.66	4.56	3.85	4.49	4.59	4.49
$NH_2 + C_2H_5 \rightarrow C_2H_6 + NH$	-10.8	6.62	6.19	6.15	5.49	6.59	6.13	6.09	5.43
$C_2H_6 + NH_2 \rightarrow NH_3 + C_2H_5$	-7.0	-5.61	-1.55	-0.46	0.14	-5.51	-1.50	-0.40	0.20
$NH_2 + CH_4 \rightarrow CH_3 + NH_3$	-3.3	-2.96	-0.02	0.94	0.97	-2.87	0.03	1.00	1.04
MSE		-0.41	1.08	0.80	0.74	-1.32	0.23	-0.12	-0.20
MAE		8.51	4.39	3.23	3.02	7.09	3.97	3.80	3.67
rms		11.10	6.24	4.37	4.20	9.38	5.97	4.95	4.89
Max(-)		-18.31	-7.86	-7.24	-7.28	-15.92	-8.89	-11.24	-11.71
Max(+)		35.68	22.59	11.96	12.03	30.50	21.60	10.65	10.73

TABLE S5. The 166 experimentally determined equilibrium bond lengths (in Å) of 136 molecules included in EXTS [3]. Optimized bond lengths are calculated by various methods.

Molecule	Experiment	KS-DFT				TAO-DFT			
		LDA	PBE	BLYP	BLYP-D	LDA	PBE	BLYP	BLYP-D
$H_2N^-$	1.028	1.037	1.038	1.038	1.038	1.037	1.037	1.038	1.038
$NO^- (^3\Sigma^-)$	1.258	1.250	1.267	1.279	1.279	1.250	1.267	1.278	1.278
$PO^- (^3\Sigma^-)$	1.540	1.539	1.556	1.563	1.563	1.539	1.556	1.563	1.563
$BeH^+ (^1\Sigma^+)$	1.312	1.337	1.330	1.323	1.323	1.336	1.329	1.322	1.322
$CH^+ (^1\Sigma^+)$	1.131	1.162	1.153	1.147	1.147	1.162	1.153	1.147	1.147
$CN^+ (^1\Sigma^+)$	1.173	1.173	1.181	1.183	1.183	1.203	1.216	1.220	1.220
$H_3^+$	0.877	0.906	0.889	0.886	0.886	0.906	0.888	0.885	0.885
$H_3O^+$	0.976	0.990	0.988	0.989	0.990	0.990	0.987	0.989	0.990
$HCO^+$	1.097 (CH)	1.111	1.104	1.101	1.102	1.111	1.103	1.101	1.102
	1.105 (CO)	1.105	1.113	1.113	1.113	1.105	1.113	1.113	1.113
$MgH^+ (^1\Sigma^+)$	1.652	1.671	1.673	1.669	1.670	1.669	1.671	1.668	1.669
$NO^+ (^1\Sigma^+)$	1.063	1.062	1.070	1.071	1.071	1.062	1.069	1.071	1.071
$NS^+ (^1\Sigma^+)$	1.440	1.433	1.444	1.447	1.447	1.433	1.444	1.446	1.446
$OH^+ (^3\Sigma^-)$	1.029	1.055	1.047	1.050	1.050	1.055	1.046	1.050	1.050
$SiH^+ (^1\Sigma^+)$	1.504	1.538	1.532	1.527	1.527	1.537	1.532	1.526	1.526

NH <sub>4</sub> <sup>+</sup>	1.021	1.035	1.031	1.032	1.033	1.034	1.031	1.031	1.032
AlCl ( <sup>1</sup> Σ <sup>+</sup> )	2.130	2.136	2.162	2.178	2.179	2.135	2.161	2.178	2.178
AlF ( <sup>1</sup> Σ <sup>+</sup> )	1.654	1.669	1.693	1.698	1.698	1.669	1.692	1.698	1.698
AlH ( <sup>1</sup> Σ <sup>+</sup> )	1.648	1.680	1.679	1.674	1.674	1.679	1.678	1.673	1.673
AlN ( <sup>3</sup> Π <sub>i</sub> )	1.786	1.769	1.792	1.799	1.799	1.774	1.799	1.810	1.811
BCl ( <sup>1</sup> Σ <sup>+</sup> )	1.797	1.706	1.729	1.734	1.734	1.706	1.728	1.733	1.733
BeO ( <sup>1</sup> Σ <sup>+</sup> )	1.331	1.326	1.338	1.339	1.339	1.331	1.345	1.347	1.347
BeS ( <sup>1</sup> Σ <sup>+</sup> )	1.742	1.739	1.751	1.754	1.754	1.753	1.768	1.775	1.775
BF ( <sup>1</sup> Σ <sup>+</sup> )	1.263	1.256	1.271	1.272	1.272	1.256	1.271	1.272	1.272
BF <sub>3</sub>	1.307	1.307	1.322	1.325	1.326	1.307	1.322	1.325	1.326
BH ( <sup>1</sup> Σ <sup>+</sup> )	1.232	1.256	1.251	1.240	1.240	1.254	1.250	1.239	1.239
BN ( <sup>3</sup> Π)	1.281	1.323	1.332	1.333	1.333	1.322	1.331	1.332	1.332
C <sub>6</sub> H <sub>6</sub>	1.390 (CC)	1.385	1.397	1.401	1.402	1.385	1.397	1.400	1.402
	1.086 (CH)	1.094	1.091	1.088	1.089	1.093	1.091	1.088	1.088
CCl <sub>2</sub> O	1.177 (CO)	1.177	1.185	1.184	1.184	1.177	1.185	1.184	1.184
	1.737 (CCl)	1.731	1.754	1.777	1.780	1.730	1.754	1.776	1.779
CF <sub>4</sub>	1.315	1.318	1.335	1.343	1.344	1.317	1.335	1.343	1.344
CH <sub>2</sub> Cl <sub>2</sub>	1.766 (CCl)	1.754	1.779	1.801	1.805	1.754	1.778	1.800	1.804
	1.080 (CH)	1.096	1.092	1.088	1.090	1.095	1.091	1.088	1.089
CH <sub>2</sub> F <sub>2</sub>	1.351 (CF)	1.348	1.369	1.380	1.382	1.348	1.369	1.380	1.382
	1.084 (CH)	1.105	1.100	1.096	1.099	1.105	1.100	1.096	1.098
CH <sub>2</sub> O <sub>2</sub> ( <i>trans</i> )	1.201 (C=O)	1.198	1.207	1.208	1.208	1.198	1.206	1.208	1.208
	1.091 (CH)	1.111	1.106	1.103	1.104	1.110	1.106	1.103	1.103
	1.340 (CO)	1.332	1.353	1.362	1.363	1.332	1.353	1.362	1.363
	0.969 (OH)	0.983	0.980	0.981	0.981	0.983	0.979	0.980	0.980
CH <sub>3</sub> Cl	1.086 (CH)	1.096	1.094	1.091	1.093	1.096	1.093	1.090	1.093
	1.778 (CCl)	1.763	1.789	1.815	1.820	1.762	1.788	1.815	1.819
CH <sub>3</sub> F	1.086 (CH)	1.102	1.099	1.096	1.098	1.102	1.098	1.095	1.098
	1.383 (CF)	1.371	1.395	1.409	1.412	1.371	1.395	1.409	1.412
CH <sub>4</sub>	1.087	1.097	1.096	1.094	1.097	1.097	1.095	1.094	1.096
CHF <sub>3</sub>	1.328 (CF)	1.330	1.349	1.358	1.359	1.330	1.349	1.357	1.359
	1.091 (CH)	1.105	1.100	1.096	1.097	1.105	1.099	1.095	1.097
Cl <sub>2</sub> ( <sup>1</sup> Σ <sub>g</sub> <sup>+</sup> )	1.988	1.980	2.005	2.040	2.040	1.979	2.005	2.040	2.040
ClCN	1.629 (CCl)	1.612	1.630	1.642	1.643	1.612	1.629	1.642	1.643
	1.160 (CN)	1.160	1.167	1.166	1.167	1.160	1.167	1.166	1.167
ClF	1.628	1.625	1.653	1.674	1.675	1.625	1.653	1.674	1.674
CO ( <sup>1</sup> Σ <sup>+</sup> )	1.128	1.127	1.136	1.136	1.136	1.127	1.136	1.136	1.136
CO <sub>2</sub>	1.160	1.162	1.171	1.172	1.172	1.161	1.170	1.172	1.172
CS ( <sup>1</sup> Σ <sup>+</sup> )	1.535	1.533	1.546	1.548	1.548	1.533	1.546	1.548	1.548
CS <sub>2</sub>	1.553	1.551	1.562	1.567	1.568	1.550	1.562	1.567	1.568
F <sub>2</sub> ( <sup>1</sup> Σ <sub>g</sub> <sup>+</sup> )	1.412	1.383	1.412	1.431	1.431	1.383	1.411	1.431	1.431
F <sub>2</sub> O	1.405	1.388	1.417	1.437	1.438	1.388	1.417	1.437	1.438
F <sub>2</sub> S	1.587	1.598	1.624	1.638	1.639	1.598	1.623	1.638	1.639
F <sub>2</sub> Si	1.590	1.607	1.629	1.635	1.636	1.607	1.629	1.635	1.636
F <sub>3</sub> HSi	1.562 (SiF)	1.575	1.595	1.599	1.600	1.575	1.594	1.599	1.600
	1.447 (SiH)	1.470	1.468	1.463	1.460	1.469	1.468	1.462	1.460
H <sub>2</sub> ( <sup>1</sup> Σ <sub>g</sub> <sup>+</sup> )	0.741	0.766	0.751	0.747	0.747	0.766	0.750	0.746	0.746
H <sub>2</sub> CCCH <sub>2</sub>	1.076 (CH)	1.095	1.092	1.090	1.091	1.094	1.091	1.089	1.091
	1.308 (CC)	1.298	1.308	1.308	1.309	1.298	1.307	1.308	1.309
H <sub>2</sub> CS	1.611 (CS)	1.601	1.614	1.621	1.622	1.601	1.615	1.622	1.623
	1.086 (CH)	1.100	1.097	1.094	1.096	1.100	1.097	1.094	1.096
H <sub>2</sub> O	0.958	0.971	0.969	0.971	0.971	0.970	0.969	0.971	0.971

H <sub>2</sub> S	1.336	1.354	1.352	1.352	1.353	1.353	1.351	1.352	1.352
H <sub>2</sub> Si	1.514	1.538	1.538	1.534	1.533	1.537	1.537	1.533	1.532
HCCCN	1.062 (CH)	1.075	1.071	1.068	1.068	1.075	1.071	1.067	1.068
	1.206 (C≡C)	1.208	1.214	1.212	1.213	1.208	1.214	1.212	1.213
	1.376 (CC)	1.355	1.366	1.367	1.368	1.355	1.365	1.367	1.368
	1.161 (C≡N)	1.162	1.170	1.169	1.169	1.162	1.170	1.169	1.169
HCCH	1.061 (CH)	1.074	1.070	1.067	1.068	1.074	1.070	1.067	1.068
	1.203 (CC)	1.202	1.207	1.206	1.207	1.201	1.207	1.206	1.206
HCl ( <sup>1</sup> Σ <sup>+</sup> )	1.275	1.291	1.288	1.291	1.291	1.291	1.288	1.290	1.290
HCN	1.065 (CH)	1.079	1.075	1.072	1.073	1.079	1.075	1.072	1.073
	1.153 (CN)	1.151	1.158	1.157	1.158	1.151	1.158	1.157	1.157
HCP	1.066 (CH)	1.083	1.080	1.077	1.078	1.083	1.080	1.076	1.077
	1.540 (CP)	1.537	1.547	1.548	1.549	1.536	1.546	1.548	1.548
HF ( <sup>1</sup> Σ <sup>+</sup> )	0.917	0.932	0.930	0.933	0.933	0.931	0.930	0.933	0.933
HNC	0.994 (NH)	1.009	1.006	1.005	1.006	1.009	1.005	1.005	1.005
	1.169 (NC)	1.168	1.176	1.175	1.175	1.167	1.176	1.175	1.175
HOCl	0.964 (OH)	0.978	0.976	0.978	0.978	0.977	0.976	0.977	0.978
	1.689 (OCl)	1.678	1.710	1.736	1.736	1.678	1.709	1.736	1.736
LiCl ( <sup>1</sup> Σ <sup>+</sup> )	2.021	2.004	2.025	2.031	2.041	2.003	2.024	2.030	2.039
LiF ( <sup>1</sup> Σ <sup>+</sup> )	1.564	1.560	1.583	1.584	1.586	1.559	1.582	1.583	1.586
LiH ( <sup>1</sup> Σ <sup>+</sup> )	1.596	1.603	1.603	1.595	1.630	1.600	1.600	1.593	1.626
MgO ( <sup>1</sup> Σ <sup>+</sup> )	1.749	1.726	1.751	1.757	1.757	1.754	1.782	1.789	1.789
MgS ( <sup>1</sup> Σ <sup>+</sup> )	2.143	2.130	2.155	2.168	2.168	2.170	2.200	2.219	2.220
N <sub>2</sub> ( <sup>1</sup> Σ <sub>g</sub> <sup>+</sup> )	1.098	1.095	1.103	1.103	1.103	1.095	1.103	1.103	1.103
N <sub>2</sub> O	1.127 (NN)	1.130	1.138	1.139	1.139	1.130	1.138	1.139	1.139
	1.185 (NO)	1.175	1.188	1.197	1.197	1.175	1.188	1.197	1.197
NaCl ( <sup>1</sup> Σ <sup>+</sup> )	2.361	2.335	2.376	2.387	2.401	2.334	2.374	2.385	2.400
NaF ( <sup>1</sup> Σ <sup>+</sup> )	1.926	1.908	1.947	1.951	1.956	1.907	1.946	1.950	1.955
NaH ( <sup>1</sup> Σ <sup>+</sup> )	1.887	1.867	1.890	1.884	1.912	1.865	1.887	1.882	1.909
NF ( <sup>3</sup> Σ <sup>-</sup> )	1.317	1.302	1.325	1.341	1.341	1.302	1.325	1.341	1.341
NH ( <sup>3</sup> Σ <sup>-</sup> )	1.036	1.054	1.050	1.051	1.051	1.054	1.049	1.050	1.050
NH <sub>3</sub>	1.012	1.007	1.004	1.005	1.006	1.007	1.004	1.004	1.005
O <sub>2</sub> ( <sup>3</sup> Σ <sub>g</sub> <sup>-</sup> )	1.208	1.203	1.217	1.228	1.228	1.203	1.217	1.228	1.228
O <sub>3</sub>	1.272	1.250	1.270	1.286	1.286	1.251	1.271	1.287	1.287
OCS	1.147 (CO)	1.160	1.168	1.170	1.170	1.160	1.168	1.170	1.170
	1.561 (CS)	1.556	1.568	1.574	1.574	1.555	1.568	1.573	1.574
P <sub>2</sub> ( <sup>1</sup> Σ <sub>g</sub> <sup>+</sup> )	1.893	1.890	1.904	1.911	1.911	1.890	1.903	1.910	1.910
PF ( <sup>3</sup> Σ <sup>-</sup> )	1.590	1.600	1.623	1.633	1.633	1.600	1.623	1.633	1.633
PH ( <sup>3</sup> Σ <sup>-</sup> )	1.422	1.442	1.440	1.439	1.439	1.441	1.439	1.438	1.438
PH <sub>3</sub>	1.413	1.431	1.430	1.428	1.429	1.431	1.430	1.428	1.428
PN ( <sup>1</sup> Σ <sup>+</sup> )	1.491	1.486	1.498	1.500	1.500	1.486	1.498	1.499	1.499
S <sub>2</sub> ( <sup>3</sup> Σ <sub>g</sub> <sup>-</sup> )	1.889	1.896	1.911	1.929	1.929	1.895	1.910	1.928	1.928
S <sub>2</sub> O	1.884 (SS)	1.889	1.908	1.925	1.926	1.889	1.908	1.926	1.927
	1.456 (SO)	1.463	1.478	1.485	1.486	1.463	1.478	1.485	1.486
SCS	1.553	1.551	1.562	1.567	1.568	1.550	1.562	1.567	1.568
SiO ( <sup>1</sup> Σ <sup>+</sup> )	1.510	1.515	1.529	1.531	1.531	1.514	1.528	1.531	1.531
SiS ( <sup>1</sup> Σ <sup>+</sup> )	1.929	1.936	1.952	1.960	1.960	1.935	1.951	1.959	1.959
SO ( <sup>3</sup> Σ <sup>-</sup> )	1.481	1.489	1.504	1.513	1.513	1.489	1.503	1.513	1.513
SO <sub>2</sub>	1.431	1.440	1.455	1.461	1.461	1.440	1.455	1.461	1.461
B <sub>2</sub> H <sub>6</sub>	1.314 (BH ×2)	1.312	1.319	1.317	1.321	1.311	1.319	1.317	1.320
	1.184 (BH ×4)	1.198	1.196	1.190	1.191	1.198	1.195	1.190	1.191
cyclopropane	1.501 (CC)	1.492	1.509	1.517	1.520	1.492	1.508	1.516	1.520



	1.083 (CH)	1.091	1.089	1.087	1.089	1.091	1.089	1.087	1.088
C <sub>2</sub> <sup>-</sup> ( <sup>2</sup> Σ <sub>g</sub> <sup>+</sup> )	1.268	1.258	1.269	1.268	1.268	1.265	1.274	1.275	1.275
NH <sup>-</sup> ( <sup>2</sup> Π <sub>i</sub> )	1.047	1.051	1.051	1.052	1.052	1.051	1.051	1.051	1.051
AlH <sup>+</sup> ( <sup>2</sup> Σ <sup>+</sup> )	1.602	1.642	1.635	1.638	1.639	1.640	1.634	1.637	1.637
Cl <sub>2</sub> <sup>+</sup> ( <sup>2</sup> Π <sub>3/2g</sub> )	1.892	1.893	1.913	1.941	1.941	1.892	1.913	1.941	1.941
CO <sup>+</sup> ( <sup>2</sup> Σ <sup>+</sup> )	1.115	1.114	1.122	1.123	1.123	1.114	1.121	1.123	1.123
HCl <sup>+</sup> ( <sup>2</sup> Π <sub>i</sub> )	1.315	1.339	1.332	1.334	1.334	1.339	1.332	1.334	1.334
He <sub>2</sub> <sup>+</sup> ( <sup>2</sup> Σ <sub>u</sub> <sup>+</sup> )	1.081	1.161	1.176	1.183	1.184	1.161	1.175	1.183	1.183
HF <sup>+</sup> ( <sup>2</sup> Π <sub>i</sub> )	1.001	1.028	1.021	1.026	1.026	1.028	1.021	1.026	1.026
N <sub>2</sub> <sup>+</sup> ( <sup>2</sup> Σ <sub>g</sub> <sup>+</sup> )	1.116	1.107	1.115	1.116	1.116	1.108	1.115	1.117	1.117
NH <sup>+</sup> ( <sup>2</sup> Π <sub>r</sub> )	1.070	1.098	1.090	1.090	1.090	1.098	1.091	1.090	1.090
NH <sub>3</sub> <sup>+</sup>	1.014	1.037	1.032	1.032	1.034	1.037	1.032	1.032	1.033
O <sub>2</sub> <sup>+</sup> ( <sup>2</sup> Π <sub>g</sub> )	1.116	1.110	1.121	1.127	1.127	1.110	1.121	1.127	1.127
PF <sup>+</sup> ( <sup>2</sup> Π <sub>r</sub> )	1.500	1.517	1.535	1.541	1.541	1.517	1.535	1.541	1.541
H <sub>2</sub> O <sup>+</sup> ( <sup>2</sup> B <sub>1</sub> )	0.999	1.019	1.014	1.017	1.017	1.019	1.014	1.016	1.017
AlS ( <sup>2</sup> Σ <sup>+</sup> )	2.029	2.031	2.049	2.064	2.064	2.052	2.067	2.095	2.096
BeCl ( <sup>2</sup> Σ <sup>+</sup> )	1.797	1.789	1.806	1.811	1.811	1.788	1.806	1.811	1.811
BeF ( <sup>2</sup> Σ <sup>+</sup> )	1.361	1.358	1.374	1.376	1.376	1.358	1.373	1.375	1.375
BeH ( <sup>2</sup> Σ <sup>+</sup> )	1.343	1.361	1.356	1.346	1.346	1.359	1.354	1.345	1.345
BO ( <sup>2</sup> Σ <sup>+</sup> )	1.205	1.204	1.213	1.213	1.213	1.203	1.212	1.213	1.213
BS ( <sup>2</sup> Σ <sup>+</sup> )	1.609	1.609	1.620	1.623	1.623	1.609	1.620	1.623	1.623
CCl ( <sup>2</sup> Π <sub>1/2</sub> , <sup>2</sup> Π <sub>3/2</sub> )	1.645	1.632	1.657	1.672	1.672	1.630	1.654	1.668	1.668
CF ( <sup>2</sup> Π <sub>r</sub> )	1.272	1.263	1.283	1.291	1.291	1.262	1.282	1.289	1.289
CH ( <sup>2</sup> Π <sub>r</sub> )	1.120	1.139	1.136	1.132	1.132	1.139	1.135	1.131	1.131
CH <sub>3</sub>	1.076	1.089	1.086	1.084	1.086	1.089	1.086	1.084	1.086
ClO ( <sup>2</sup> Π <sub>i</sub> )	1.570	1.553	1.580	1.600	1.600	1.552	1.576	1.596	1.596
CN ( <sup>2</sup> Σ <sup>+</sup> )	1.172	1.166	1.174	1.175	1.175	1.168	1.175	1.176	1.176
CP ( <sup>2</sup> Σ <sup>+</sup> )	1.562	1.555	1.566	1.569	1.569	1.562	1.569	1.576	1.576
H <sub>2</sub> N ( <sup>2</sup> B <sub>1</sub> )	1.025	1.039	1.037	1.037	1.037	1.038	1.036	1.037	1.037
HO	0.970	0.986	0.983	0.985	0.985	0.985	0.983	0.985	0.985
HOO	0.971 (OH)	0.991	0.987	0.988	0.988	0.991	0.987	0.988	0.988
	1.331 (OO)	1.308	1.333	1.353	1.353	1.311	1.334	1.353	1.353
MgCl ( <sup>2</sup> Σ <sup>+</sup> )	2.199	2.196	2.225	2.239	2.240	2.195	2.223	2.238	2.239
MgF ( <sup>2</sup> Σ <sup>+</sup> )	1.750	1.756	1.783	1.788	1.789	1.755	1.782	1.788	1.788
MgH ( <sup>2</sup> Σ <sup>+</sup> )	1.730	1.753	1.756	1.756	1.757	1.750	1.754	1.754	1.755
NO ( <sup>2</sup> Π <sub>r</sub> )	1.151	1.146	1.157	1.161	1.161	1.146	1.157	1.161	1.161
NO <sub>2</sub> ( <sup>2</sup> A <sub>1</sub> )	1.195	1.189	1.203	1.210	1.210	1.189	1.203	1.210	1.210
NS ( <sup>2</sup> Π <sub>r</sub> )	1.494	1.491	1.505	1.510	1.510	1.491	1.505	1.510	1.510
OP ( <sup>2</sup> Π <sub>r</sub> )	1.474	1.481	1.494	1.498	1.498	1.481	1.495	1.499	1.499
SF ( <sup>2</sup> Π <sub>3/2</sub> , <sup>2</sup> Π <sub>1/2</sub> )	1.601	1.601	1.626	1.642	1.642	1.601	1.626	1.641	1.641
SH ( <sup>2</sup> Π <sub>i</sub> )	1.345	1.359	1.356	1.357	1.357	1.358	1.356	1.356	1.356
SiCl ( <sup>2</sup> Π <sub>r</sub> )	2.058	2.058	2.084	2.104	2.104	2.057	2.082	2.102	2.102
SiF ( <sup>2</sup> Π <sub>r</sub> )	1.601	1.617	1.640	1.646	1.646	1.617	1.639	1.646	1.646
SiH ( <sup>2</sup> Π <sub>r</sub> )	1.520	1.545	1.544	1.540	1.540	1.544	1.544	1.539	1.539
SiN ( <sup>2</sup> Σ <sup>+</sup> )	1.572	1.564	1.578	1.582	1.582	1.586	1.597	1.607	1.607
HCO	1.119 (CH)	1.138	1.134	1.133	1.134	1.137	1.134	1.132	1.133
	1.175 (CO)	1.172	1.181	1.183	1.184	1.172	1.181	1.183	1.184
MSE		0.004	0.014	0.018	0.019	0.005	0.014	0.019	0.020
MAE		0.013	0.015	0.019	0.020	0.013	0.015	0.020	0.021
rms		0.017	0.019	0.024	0.025	0.017	0.020	0.025	0.026
Max(-)		-0.091	-0.069	-0.064	-0.063	-0.091	-0.069	-0.064	-0.064
Max(+)		0.081	0.095	0.103	0.103	0.080	0.095	0.102	0.102

TABLE S6. Singlet-triplet energy gap [ $E_T - E_S$ ] (in kcal/mol), as a function of the acene length, calculated by various functionals in spin-unrestricted KS-DFT and TAO-DFT. The experimental data (uncorrected for zero-point vibrations, thermal vibrations, etc.) are taken from Refs. [4–7], the DMRG data are taken from Ref. [8], and the CCSD(T)/CBS data are taken from Ref. [9].

<i>n</i> -acene	Experiment	DMRG/cc-pVDZ	DMRG/STO-3G	CCSD(T)/CBS	KS-DFT				TAO-DFT			
					LDA	PBE	BLYP	BLYP-D	LDA	PBE	BLYP	BLYP-D
2	61.0	61.0	61.5	65.83	65.19	60.88	60.44	60.30	64.77	60.59	60.14	59.99
3	43.1	44.0	45.9	48.21	43.40	40.26	40.19	40.20	43.22	40.12	40.03	40.04
4	29.3	31.9	34.7	33.49	29.06	26.61	26.74	26.82	29.01	26.60	26.71	26.79
5	19.8	23.4	26.7	25.27	19.20	17.20	17.45	17.58	19.60	17.62	17.83	17.95
6		17.5	21.0	17.71	12.16	10.48	10.81	10.95	13.55	11.84	12.11	12.22
8			14.2	9.20	3.07	1.81	2.87	2.37	7.85	6.41	6.65	6.72
10			11.6	4.64	0.53	1.43	1.31	1.31	5.91	4.66	4.82	4.86
12			10.7		1.59	2.17	1.95	1.89	4.82	3.77	3.88	3.91
14					3.47	1.57	3.27	3.18	3.98	3.09	3.19	3.21
16					4.43	2.10	3.86	3.83	3.37	2.60	2.68	2.69
18									2.94	2.29	2.32	2.33
20									2.62	2.00	2.06	2.07
22									2.37	1.80	1.85	1.86
24									2.15	1.64	1.69	1.70
26									1.98	1.51	1.55	1.56
28									1.83	1.39	1.43	1.44
30									1.70	1.29	1.33	1.33
32									1.59	1.21	1.24	1.25
34									1.49	1.13	1.16	1.16
36									1.40	1.07	1.10	1.10
38									1.33	1.01	1.04	1.04
40									1.26	0.95	0.98	0.99
42									1.20	0.91	0.93	0.93
44									1.14	0.86	0.88	0.89
46									1.09	0.83	0.85	0.85
48									1.04	0.79	0.81	0.82
50									1.00	0.76	0.78	0.78
52									0.96	0.73	0.75	0.75
54									0.92	0.70	0.72	0.72
56									0.89	0.66	0.69	0.70
58									0.86	0.65	0.67	0.66
60									0.83	0.63	0.64	0.65
62									0.80	0.61	0.63	0.63
64									0.78	0.59	0.61	0.61
66									0.75	0.57	0.59	0.59
68									0.73	0.55	0.56	0.56
70									0.71	0.54	0.55	0.55
72									0.69	0.52	0.54	0.54
74									0.67	0.51	0.52	0.53
76									0.65	0.50	0.51	0.51
78									0.64	0.48	0.50	0.50
80									0.62	0.46	0.47	0.48
82									0.60	0.46	0.47	0.47
84									0.59	0.45	0.46	0.46
86									0.58	0.44	0.45	0.45
88									0.56	0.42	0.44	0.44
90									0.55	0.41	0.43	0.43
92									0.54	0.41	0.41	0.41
94									0.53	0.40	0.41	0.41

96	0.51	0.39	0.40	0.40
98	0.50	0.38	0.39	0.39
100	0.49	0.38	0.38	0.39

TABLE S7. Vertical ionization potential (in eV) for the lowest singlet state of  $n$ -acene as a function of the acene length, calculated by various functionals in spin-unrestricted TAO-DFT. The experimental data are taken from the compilation in Ref. [10], and the CCSD(T)/CBS data are taken from Ref. [11].

$n$ -acene	Experiment	CCSD(T)/CBS	TAO-DFT			
			LDA	PBE	BLYP	BLYP-D
2	8.14	8.24	7.81	7.58	7.33	7.32
3	7.44	7.47	7.00	6.79	6.54	6.54
4	6.97	6.95	6.46	6.25	6.00	6.00
5	6.59	6.57	6.07	5.87	5.62	5.62
6		6.43	5.79	5.59	5.34	5.34
8			5.44	5.25	4.99	4.99
10			5.23	5.04	4.78	4.78
12			5.08	4.89	4.63	4.62
14			4.96	4.77	4.51	4.50
16			4.86	4.67	4.41	4.41
18			4.78	4.60	4.33	4.33
20			4.71	4.53	4.27	4.26
22			4.66	4.48	4.21	4.20
24			4.61	4.43	4.16	4.16
26			4.57	4.39	4.12	4.11
28			4.53	4.35	4.08	4.08
30			4.50	4.32	4.05	4.04
32			4.47	4.29	4.02	4.01
34			4.44	4.26	3.99	3.99
36			4.42	4.24	3.97	3.96
38			4.39	4.21	3.95	3.94
40			4.37	4.19	3.93	3.92
42			4.35	4.18	3.91	3.90
44			4.34	4.16	3.90	3.88
46			4.32	4.14	3.88	3.87
48			4.31	4.13	3.86	3.85
50			4.29	4.11	3.85	3.84
52			4.28	4.10	3.84	3.83
54			4.27	4.09	3.82	3.82
56			4.26	4.08	3.81	3.80
58			4.24	4.07	3.80	3.79
60			4.23	4.06	3.79	3.78
62			4.23	4.05	3.78	3.77
64			4.22	4.04	3.77	3.76
66			4.21	4.03	3.76	3.76
68			4.20	4.02	3.76	3.75
70			4.19	4.01	3.75	3.74
72			4.18	4.01	3.74	3.73
74			4.18	4.00	3.73	3.73
76			4.17	3.99	3.73	3.72
78			4.16	3.99	3.72	3.71
80			4.16	3.98	3.71	3.71

82	4.15	3.98	3.71	3.70
84	4.15	3.97	3.70	3.70
86	4.14	3.96	3.70	3.69
88	4.14	3.96	3.69	3.68
90	4.13	3.95	3.69	3.68
92	4.13	3.95	3.68	3.67
94	4.12	3.95	3.68	3.67
96	4.12	3.94	3.67	3.67
98	4.11	3.94	3.67	3.66
100	4.11	3.93	3.67	3.66

TABLE S8. Vertical electron affinity (in eV) for the lowest singlet state of  $n$ -acene as a function of the acene length, calculated by various functionals in spin-unrestricted TAO-DFT. The experimental data are taken from the compilation in Ref. [10], and the CCSD(T)/CBS data are taken from Ref. [12].

$n$ -acene	Experiment	CCSD(T)/CBS	TAO-DFT			
			LDA	PBE	BLYP	BLYP-D
2	-0.20	-0.48	-0.62	-0.72	-0.94	-0.94
3	0.53	0.28	0.28	0.16	-0.07	-0.07
4	1.07	0.82	0.90	0.77	0.52	0.52
5	1.39	1.21	1.34	1.20	0.95	0.95
6		1.47	1.66	1.52	1.26	1.26
8			2.06	1.92	1.66	1.65
10			2.30	2.15	1.90	1.89
12			2.48	2.33	2.07	2.06
14			2.61	2.46	2.20	2.20
16			2.72	2.57	2.31	2.30
18			2.81	2.66	2.40	2.39
20			2.89	2.73	2.47	2.46
22			2.95	2.79	2.53	2.52
24			3.00	2.84	2.58	2.58
26			3.05	2.89	2.63	2.62
28			3.09	2.93	2.67	2.66
30			3.13	2.97	2.71	2.70
32			3.16	3.00	2.74	2.73
34			3.19	3.03	2.77	2.76
36			3.22	3.06	2.79	2.79
38			3.25	3.08	2.82	2.81
40			3.27	3.10	2.85	2.83
42			3.29	3.12	2.87	2.85
44			3.31	3.14	2.88	2.87
46			3.33	3.16	2.90	2.89
48			3.34	3.18	2.91	2.90
50			3.36	3.19	2.93	2.92
52			3.37	3.21	2.94	2.93
54			3.39	3.22	2.95	2.95
56			3.40	3.23	2.97	2.96
58			3.41	3.24	2.98	2.97
60			3.42	3.25	2.99	2.98
62			3.43	3.26	3.00	2.99
64			3.44	3.27	3.01	3.00

66	3.45	3.28	3.02	3.01
68	3.46	3.29	3.03	3.02
70	3.47	3.30	3.04	3.03
72	3.48	3.31	3.04	3.04
74	3.48	3.32	3.05	3.04
76	3.49	3.32	3.06	3.05
78	3.50	3.33	3.07	3.06
80	3.51	3.34	3.07	3.06
82	3.51	3.34	3.08	3.07
84	3.52	3.35	3.08	3.08
86	3.52	3.36	3.09	3.08
88	3.53	3.36	3.10	3.09
90	3.54	3.37	3.10	3.09
92	3.54	3.37	3.11	3.10
94	3.55	3.38	3.11	3.10
96	3.55	3.38	3.12	3.11
98	3.56	3.39	3.12	3.11
100	3.56	3.39	3.13	3.12

TABLE S9. Fundamental gap (in eV) for the lowest singlet state of  $n$ -acene as a function of the acene length, calculated by various functionals in spin-unrestricted TAO-DFT. The experimental data are taken from the compilation in Ref. [10], and the CCSD(T)/CBS data are taken from Refs. [11, 12].

$n$ -acene	Experiment	CCSD(T)/CBS	TAO-DFT			
			LDA	PBE	BLYP	BLYP-D
2	8.34	8.72	8.43	8.30	8.27	8.26
3	6.91	7.19	6.73	6.63	6.61	6.61
4	5.90	6.13	5.56	5.49	5.48	5.48
5	5.20	5.37	4.73	4.67	4.67	4.67
6		4.96	4.13	4.08	4.08	4.08
8			3.38	3.33	3.33	3.33
10			2.93	2.89	2.89	2.89
12			2.60	2.56	2.56	2.56
14			2.34	2.31	2.30	2.31
16			2.13	2.11	2.10	2.10
18			1.97	1.94	1.94	1.94
20			1.83	1.80	1.80	1.80
22			1.71	1.68	1.68	1.68
24			1.60	1.58	1.58	1.58
26			1.52	1.49	1.49	1.49
28			1.44	1.42	1.41	1.42
30			1.37	1.35	1.34	1.35
32			1.30	1.29	1.28	1.28
34			1.25	1.23	1.23	1.23
36			1.20	1.18	1.18	1.18
38			1.15	1.13	1.13	1.13
40			1.11	1.09	1.09	1.09
42			1.07	1.05	1.05	1.05
44			1.03	1.02	1.01	1.01
46			1.00	0.98	0.98	0.98
48			0.96	0.95	0.95	0.95

50	0.94	0.92	0.92	0.92
52	0.91	0.90	0.89	0.89
54	0.88	0.87	0.87	0.87
56	0.86	0.85	0.85	0.85
58	0.84	0.82	0.82	0.82
60	0.81	0.80	0.80	0.80
62	0.79	0.78	0.78	0.78
64	0.77	0.76	0.76	0.76
66	0.76	0.75	0.75	0.75
68	0.74	0.73	0.73	0.73
70	0.72	0.71	0.71	0.71
72	0.71	0.70	0.70	0.70
74	0.69	0.68	0.68	0.68
76	0.68	0.67	0.67	0.67
78	0.67	0.66	0.66	0.66
80	0.65	0.64	0.64	0.64
82	0.64	0.63	0.63	0.63
84	0.63	0.62	0.62	0.62
86	0.62	0.61	0.61	0.61
88	0.61	0.60	0.60	0.60
90	0.59	0.59	0.59	0.59
92	0.58	0.58	0.58	0.58
94	0.58	0.57	0.57	0.57
96	0.57	0.56	0.56	0.56
98	0.56	0.55	0.55	0.55
100	0.55	0.54	0.54	0.54

TABLE S10. Symmetrized von Neumann entropy for the lowest singlet state of  $n$ -acene as a function of the acene length, calculated by various functionals in spin-restricted TAO-DFT.

$n$ -acene	TAO-DFT			
	LDA	PBE	BLYP	BLYP-D
2	0.00	0.00	0.00	0.00
3	0.03	0.03	0.03	0.03
4	0.15	0.15	0.15	0.15
5	0.40	0.39	0.39	0.39
6	0.75	0.73	0.73	0.72
8	1.34	1.32	1.32	1.31
10	1.67	1.67	1.67	1.66
12	1.98	1.99	2.00	1.99
14	2.36	2.37	2.38	2.37
16	2.75	2.76	2.78	2.77
18	3.13	3.15	3.17	3.15
20	3.50	3.53	3.55	3.54
22	3.88	3.91	3.94	3.92
24	4.26	4.30	4.32	4.31
26	4.63	4.68	4.71	4.69
28	5.01	5.06	5.09	5.08
30	5.39	5.44	5.48	5.46
32	5.77	5.83	5.87	5.85
34	6.14	6.21	6.25	6.23

36	6.52	6.59	6.64	6.62
38	6.90	6.98	7.03	7.00
40	7.27	7.36	7.41	7.39
42	7.65	7.74	7.80	7.77
44	8.03	8.13	8.18	8.16
46	8.41	8.51	8.57	8.54
48	8.78	8.89	8.96	8.93
50	9.16	9.27	9.34	9.31
52	9.54	9.66	9.73	9.70
54	9.92	10.04	10.11	10.08
56	10.29	10.42	10.50	10.47
58	10.67	10.80	10.89	10.85
60	11.05	11.19	11.27	11.23
62	11.42	11.57	11.66	11.62
64	11.80	11.95	12.04	12.00
66	12.18	12.34	12.43	12.39
68	12.56	12.72	12.81	12.77
70	12.93	13.10	13.20	13.16
72	13.31	13.48	13.59	13.55
74	13.69	13.87	13.97	13.93
76	14.06	14.25	14.36	14.31
78	14.44	14.63	14.74	14.70
80	14.82	15.01	15.13	15.08
82	15.20	15.40	15.51	15.47
84	15.57	15.78	15.90	15.85
86	15.95	16.16	16.29	16.24
88	16.33	16.55	16.67	16.62
90	16.70	16.93	17.06	17.01
92	17.08	17.31	17.44	17.39
94	17.46	17.69	17.83	17.78
96	17.84	18.08	18.22	18.16
98	18.21	18.46	18.60	18.54
100	18.59	18.84	18.99	18.93