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National Chiao Tung University

# Oxygen vacancy-driven orbital multichannel Kondo effect in Dirac nodal line metals $\text{IrO}_2$ and $\text{RuO}_2$

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A Long Journey into Exotic Kondo Physics

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Ta-Kang Su

An-Shao Lien

Chao-Ching Liao



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Stefan Kirchner  
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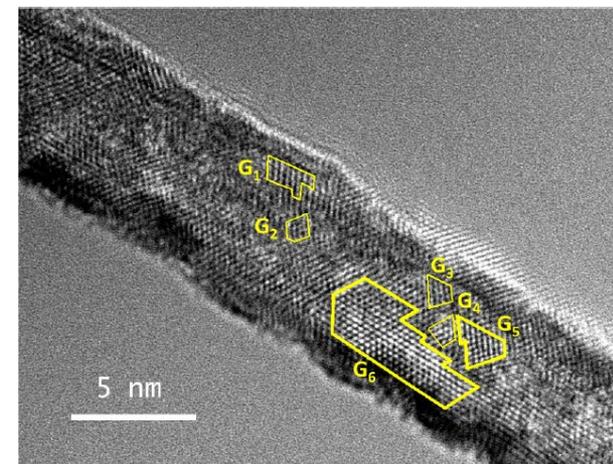
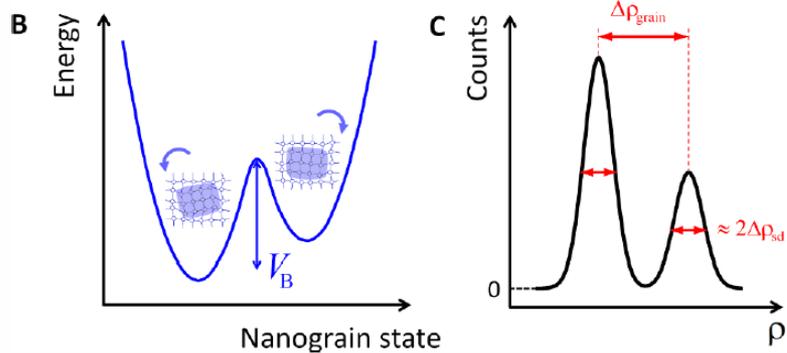
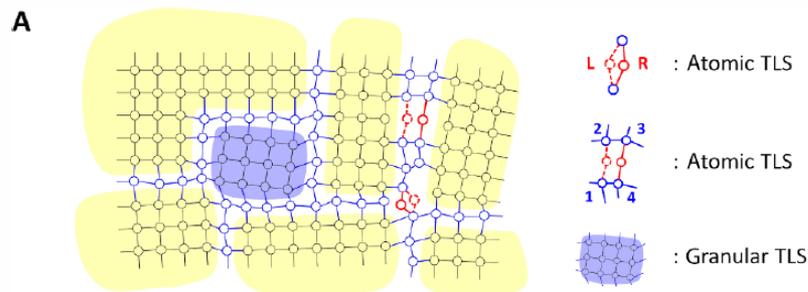
Hans Kroha  
Farzaneh Zamani  
*University of Bonn*



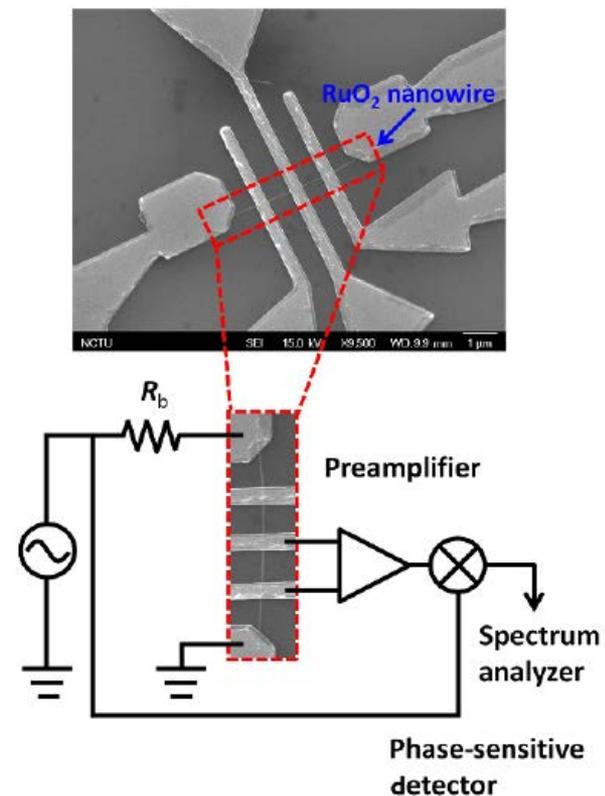
# Probing nanocrystalline grain dynamics in nanodevices

Sheng-Shiuan Yeh,<sup>1</sup> Wen-Yao Chang,<sup>1</sup> Juhn-Jong Lin<sup>1,2\*</sup>

We demonstrate theoretical conception and experimental method to quantitatively characterize nanocrystallite motion in  $\text{RuO}_2$  nanowires.



polycrystalline nanowire



## Keywords:

### Kondo physics

Magnetic spin-half Kondo effect

**Nonmagnetic orbital Kondo effect**

One-channel Kondo effect

**Two-channel Kondo effect**

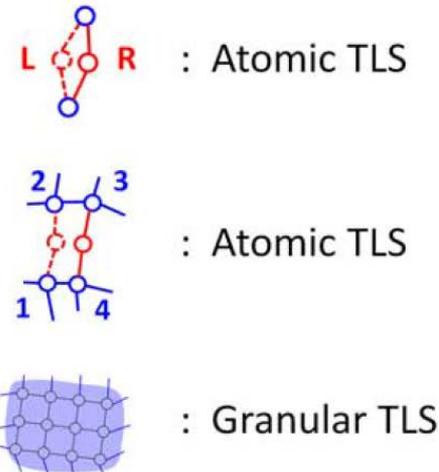
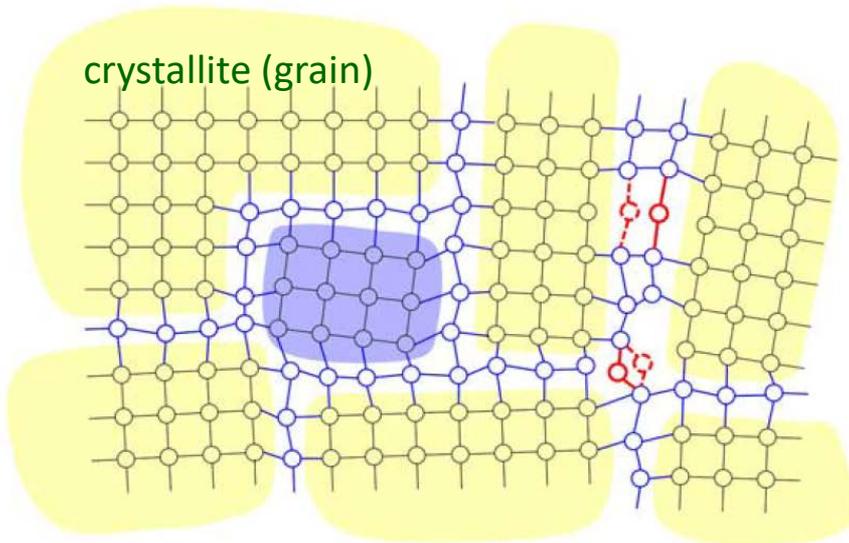
### Dynamic defects

Dynamic scattering centers

Two-level systems

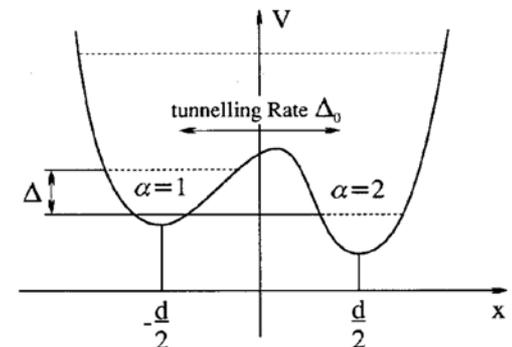
Fast two-level systems

**Defect electrons**



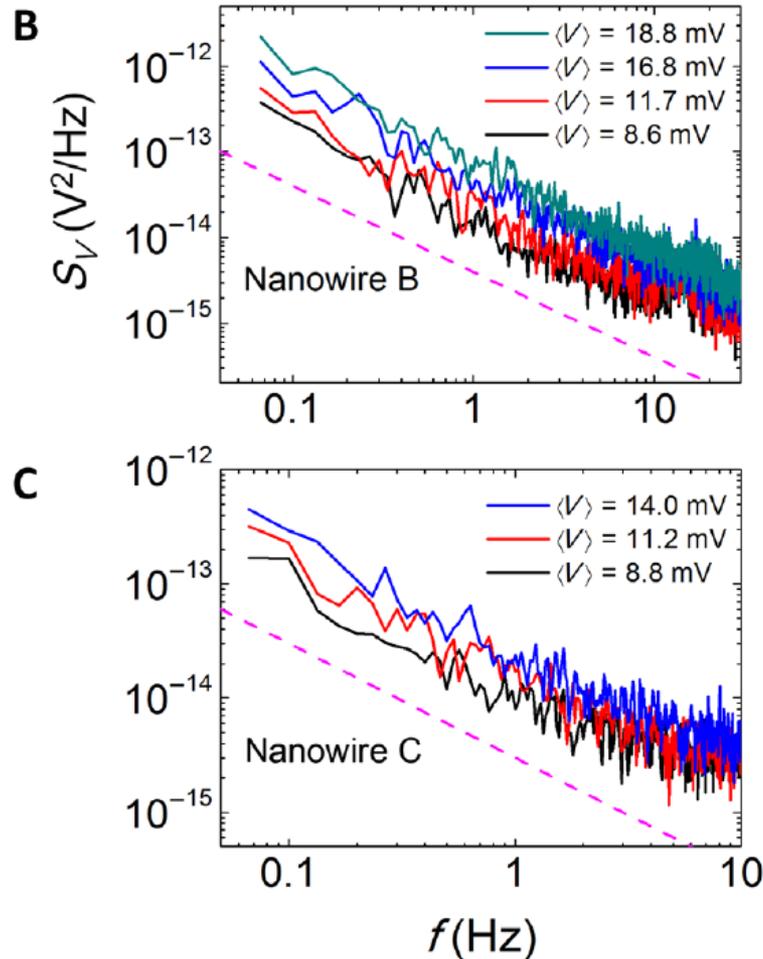
A defect having two equivalent (nearby) sites in a solid

An object switching in a double-well potential, modeled as a two-level system

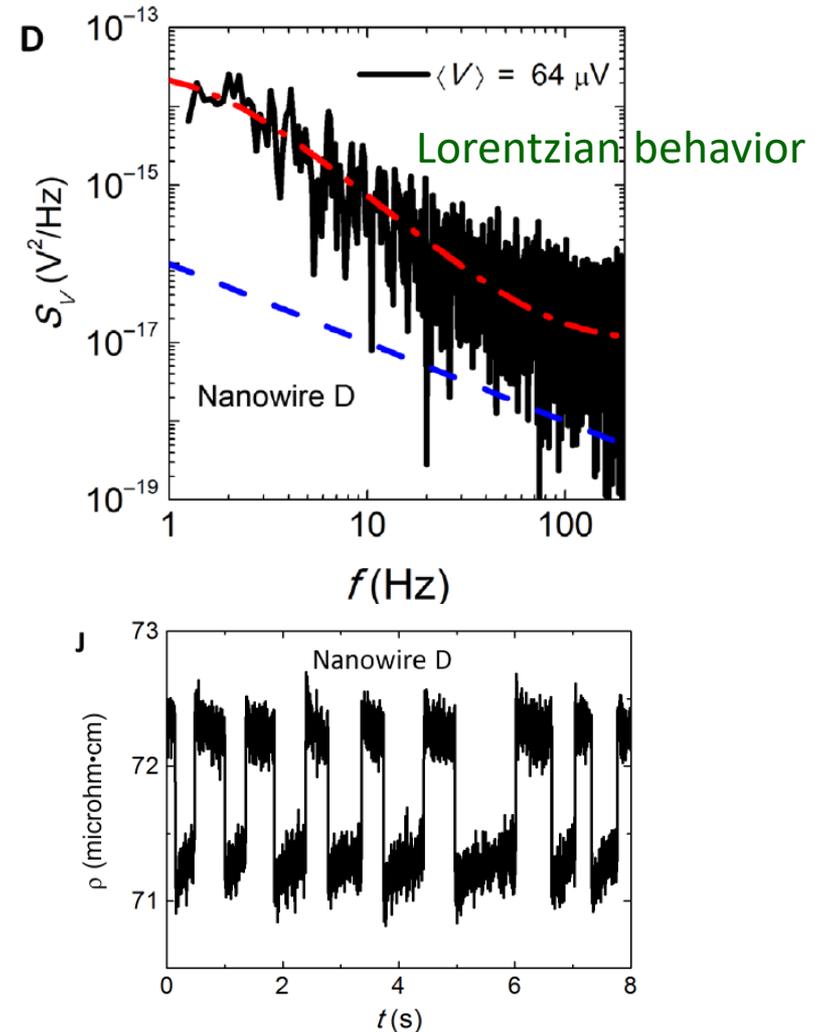


# Noise due to atomic and granular dynamic defects

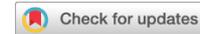
The motion of a large number of slow dynamic defects causes low-frequency ( $1/f$ ) noise.



The motion of a single nanocrystallite leads to random telegraph noise.



ARTICLE



<https://doi.org/10.1038/s41467-020-18407-7>

OPEN

# Oxygen vacancy-driven orbital multichannel Kondo effect in Dirac nodal line metals IrO<sub>2</sub> and RuO<sub>2</sub>

Sheng-Shiuan Yeh<sup>1,2,3</sup>, Ta-Kang Su<sup>1</sup>, An-Shao Lien<sup>1</sup>, Farzaneh Zamani<sup>4</sup>, Johann Kroha<sup>4</sup>, Chao-Ching Liao<sup>1</sup>, Stefan Kirchner<sup>5,6</sup> & Juhn-Jong Lin<sup>1,2,7</sup>

“**Strong electron correlations** may give rise to an **unconventional metallic state** accompanying non-magnetic Kondo scattering. Here, the authors report signatures of **orbital one- and two-channel Kondo physics** in Dirac nodal line metals RuO<sub>2</sub> and IrO<sub>2</sub> nanowires.”

Experimental realization of **non-Fermi liquid** behavior at low temperatures!

# Spin-half magnetic Kondo effect

A localized  $S = \frac{1}{2}$  magnetic impurity causes the standard Kondo effect

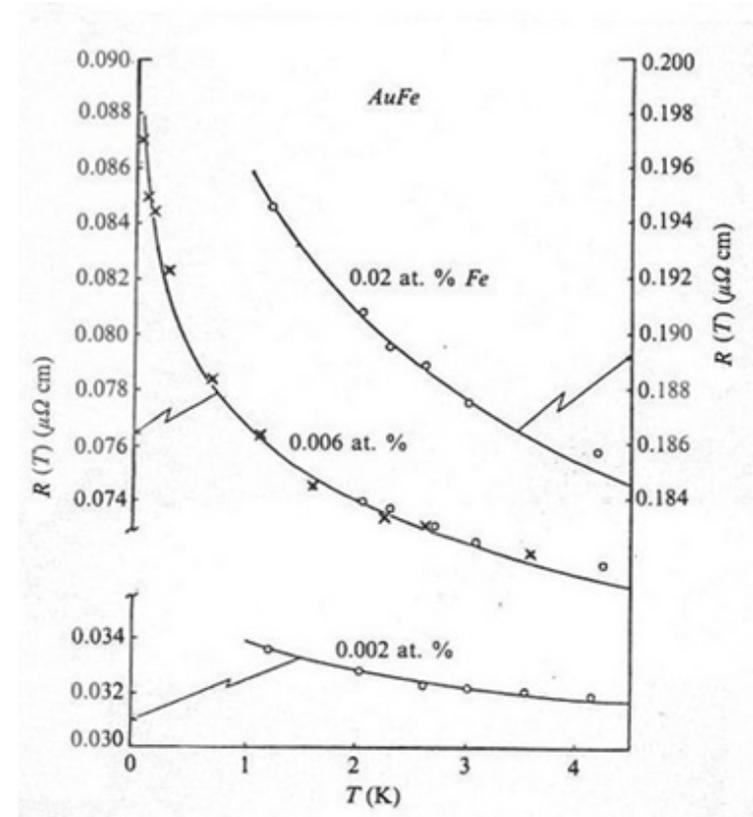
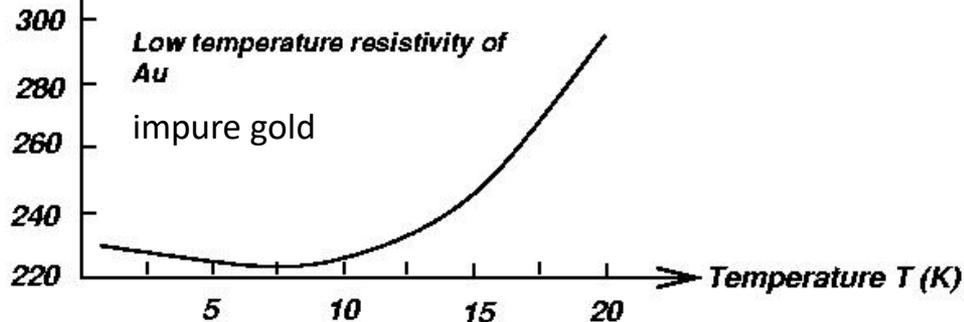
Experimental discovery in 1930s at Kamerlingh Onnes' Lab. (Leiden)

Theoretical explanation in 1960s

W.J. de Haas and G.J. van den Berg (1936)

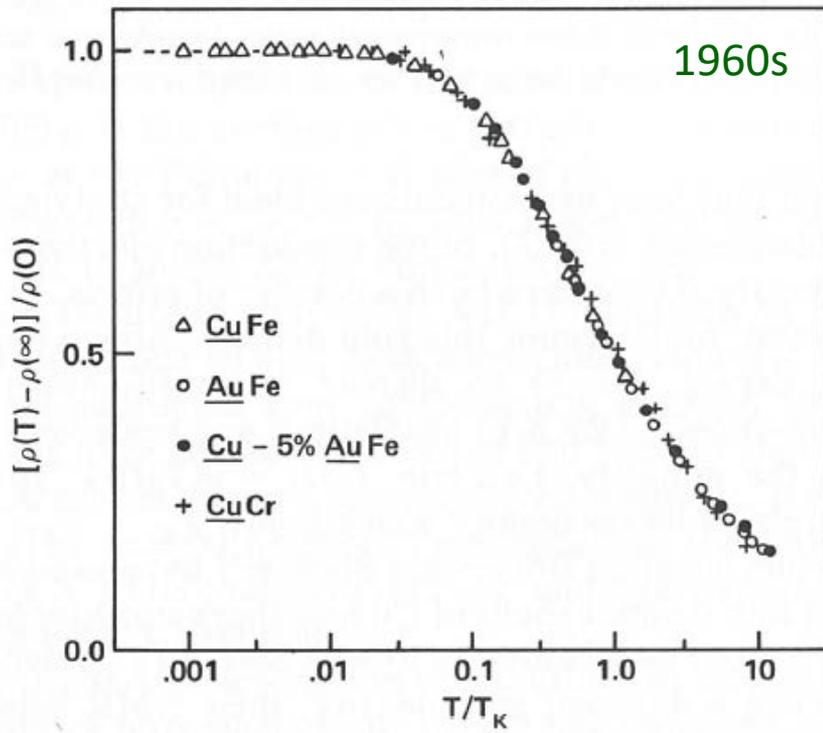
Resistance/Resistance( $T=0$  Celsius)  $\times 10000$

(from W.J. de Haas and G.J. van den Berg, *Physica* vol. 3, page 440, 1936)



Comparison of experimental and theoretical  $\rho(T)$  curves for dilute AuFe alloys [J. Kondo, *Prog. Theor. Phys.* **32**, 37 (1964)]

# Kondo resistivity: universal temperature dependence

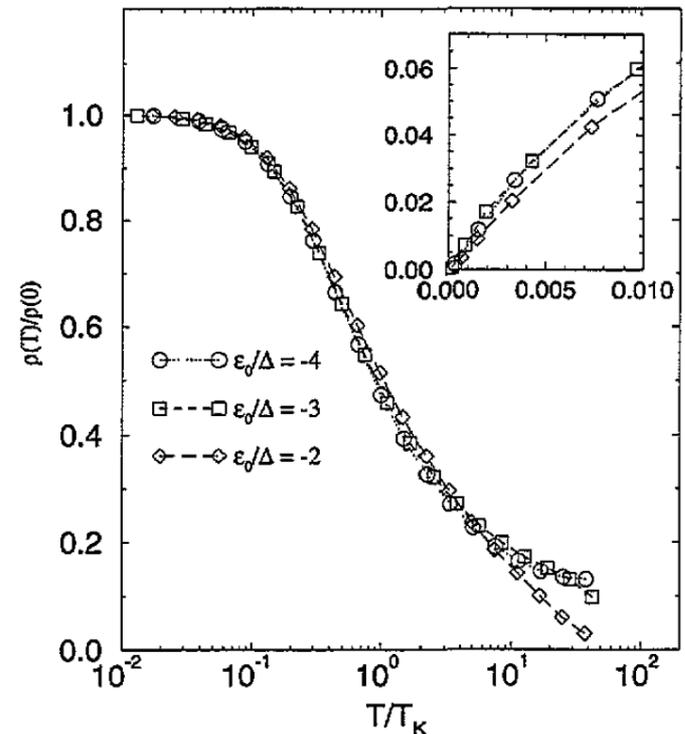


Normalized Kondo resistivity vs. reduced temperature  $T/T_K$

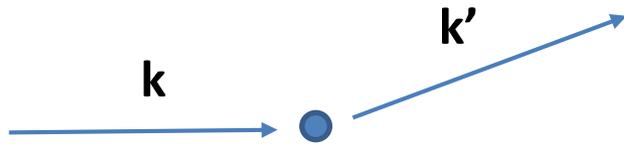
(Taken from "Long Range Order in Solids", by R. M. White and T. H. Geballe, Fig. VII.14)

Numerical renormalization group (NRG) calculations: **one-channel Kondo (1CK) scaling form**

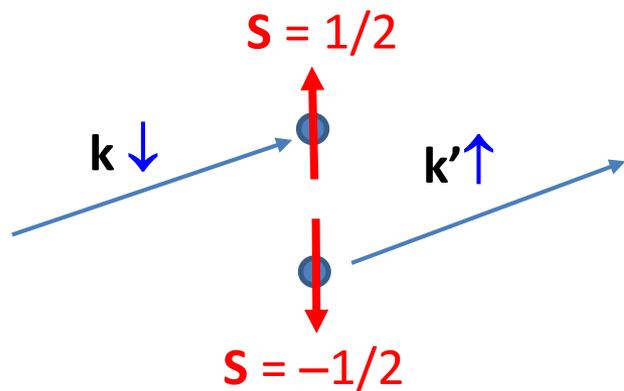
T. A. Costi, A. C. Hewson & V. Zlatic  
JPCM **6**, 2519 (1994)



# Scattering off a localized spin-half magnetic impurity

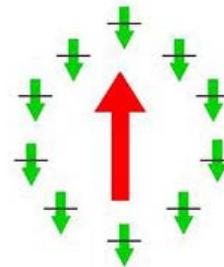


- A **nonmagnetic** impurity (defect) in a metal
- ⇒ Elastic electron scattering
- ⇒ A constant, “residual resistivity” at low T



- A localized **magnetic** impurity ( $S = \frac{1}{2}$ ) in a metal
- ⇒ Spin-spin coupling (**s-d exchange interaction**)
- ⇒  $\log(T)$  resistivity increase below a characteristic energy scale  $T_K$
- ⇒ Fermi-liquid physics as  $T \ll T_K$

$$H = \sum_{k,\sigma} \varepsilon_k c_{k,\sigma}^\dagger c_{k,\sigma} + J_K \vec{S} \cdot \vec{s}_c$$



One conduction-electron band (a Fermi sea) couples with the localized spin- $\frac{1}{2}$  magnetic moment, forming a spin-singlet ground state as  $T \rightarrow 0$  K.

# A quantum impurity with internal degree of freedom

Progress of Theoretical Physics, Vol. 32, No. 1, July 1964

## Resistance Minimum in Dilute Magnetic Alloys

Physica 84B (1976) 40–49

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Cf. Localized magnetic moments

### LOCALIZED ATOMIC STATES IN METALS

Physica 84B (1976) 207–212

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### LOCALIZED ATOMIC STATES IN METALS

#### II. RESISTIVITY AND FREE ENERGY

J. KONDO

*Electrotechnical Laboratory, Tanashi, Tokyo and Department of Applied Physics, Faculty of Engineering, University of Tokyo, Japan*

Received 31 May 1976

“We investigate a case where the interaction is of the Coulomb type, which may vary depending on the states of the localized system. The simplest of such a system may be an impurity atom, which can jump between two equivalent sites.”

$$\Psi = \psi(\vec{r}) \cdot \vec{s}_c \Rightarrow \psi(\vec{r}_L), \psi(\vec{r}_R)$$

# A quantum impurity with internal degree of freedom

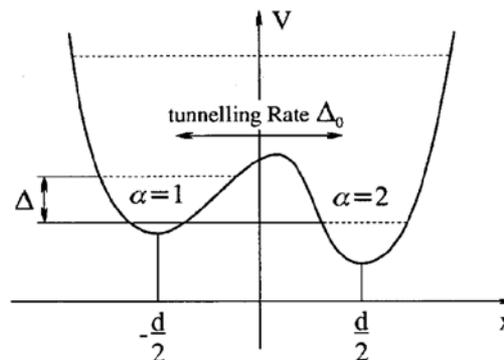
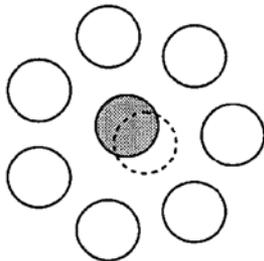
“The problem is similar to the **s-d problem** in that the conduction electrons interact with **an impurity system having an internal degree of freedom**. In the present case, the relevant interaction is the **orbital-orbital interaction**, since we are considering the Coulomb-type interaction.”

“Impurity-spin flipping” vs. “Impurity-site switching”

Two equivalent sites

Double-well potential  $\Rightarrow$  “Two-level system” model

$\Rightarrow$  Non-magnetic orbital Kondo effect !



J. Kondo (1976)

# Spin multi-channel Kondo effect

*J. Physique* **41** (1980) 193-211

MARS 1980, PAGE 193

Classification  
*Physics Abstracts*  
75.20H

## **Kondo effect in real metals**

Ph. Nozières

Institut Laue-Langevin, 156X, 38042 Grenoble Cedex, France

and A. Blandin

Laboratoire de Physique des Solides, Université Paris-Sud, 91405 Orsay, France

*(Reçu le 21 septembre 1979, accepté le 30 octobre 1979)*

One-channel Kondo effect  
⇒ Fermi-liquid ground state

Multi- (two-) channel Kondo effect  
⇒ a non-Fermi liquid ground state  
⇒ Strange metal physics

## **The multichannel Kondo model:**

**A few** conduction-electron bands interact with a localized quantum impurity which has internal degree of freedom.

“Over-screening” shall result in a non-Fermi-liquid ground state.

# Orbital multi-channel Kondo effect

## Exotic Kondo effects in metals: magnetic ions in a crystalline electric field and tunnelling centres

344 pages

D. L. Cox

Department of Physics, The Ohio State University, Columbus, Ohio 43210, USA  
and Department of Physics, University of California, Davis, California 95616, USA

and A. ZAWADOWSKI

Institute of Physics and Research Group of Hungarian Academy of Sciences,

Techn  
Resea

PHYSICAL REVIEW B

VOLUME 28, NUMBER 3

1 AUGUST 1983

### Theory of the interaction between electrons and the two-level system in amorphous metals. I. Noncommutative model Hamiltonian and scaling of first order

K. Vladár

*Central Research Institute for Physics, Post Office Box 49, H-1525 Budapest, Hungary*

A. Zawadowski\*

*Department of Physics, University of California, Los Angeles, California 90024*

(Received 10 June 1982)

I. 18 pages

II. 14 pages

III. 17 pages

$$H = \sum_{i,k,\sigma} \varepsilon_k \psi_{i,k,\sigma}^\dagger \psi_{i,k,\sigma} + J_K \sum_{i=1}^{M=2} \bar{S} \cdot \bar{s}_c^i$$

- Two-channel Kondo effect
- non-Fermi-liquid ground state

M channels (M Fermi seas)

# Vacancies in $\text{ZrAs}_{1.58}\text{Se}_{0.39}$ & two-level systems

Defect potential gives rise to several minima separated by a potential barrier: **two-level systems**

$\left. \begin{array}{l} |\uparrow\rangle \\ |\downarrow\rangle \end{array} \right\}$  if atom is in  $\left\{ \begin{array}{l} \text{left} \\ \text{right} \end{array} \right\}$  position

➔ **pseudospin algebra**

coupling to conduction electrons induces ‘assisted’ tunneling

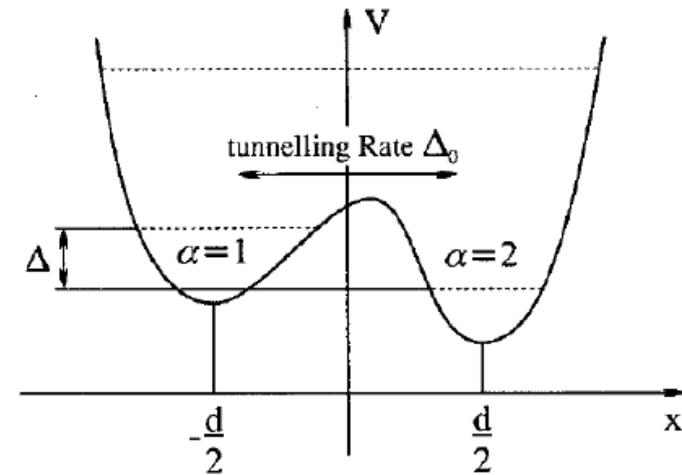
effective “spin-spin” interaction is very anisotropic

conduction electron spin acts as a bystander

– gives rise to 2 degenerate channels due to time-reversal symmetry

→ **system should flow to the non-magnetic two-channel Kondo fixed point**

→ **insensitivity to applied magnetic fields** (Vladar, Zawadowski, Zarand, von Delft ...)

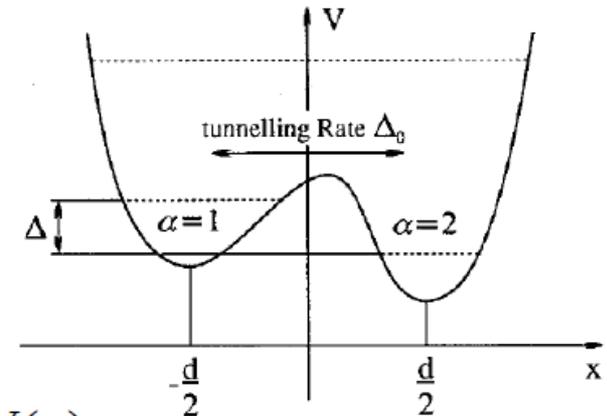


# Two-level systems: the no-go theorem

**Problem:** a tunneling term between the two minima appears, not forbidden by symmetry

effect of excited states cannot be ignored

Aleiner, et al (2002):



Consider heavy particle in a general double well potential  $V(q)$ :

- bosonization of the action
- integrating out conduction electrons



One-dimensional Coulomb gas of kinks, anti-kinks which describe tunneling events between the solutions of

$$M \frac{d^2 q}{d\tau^2} = V'[q]$$

Tunneling rate  $\Delta_0$  and effective magnetic field  $h$  are not independent



$$h_{\text{eff}} \gg T_K$$

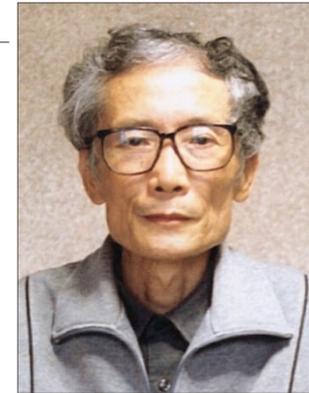


The two-channel Kondo fixed point can never be reached!

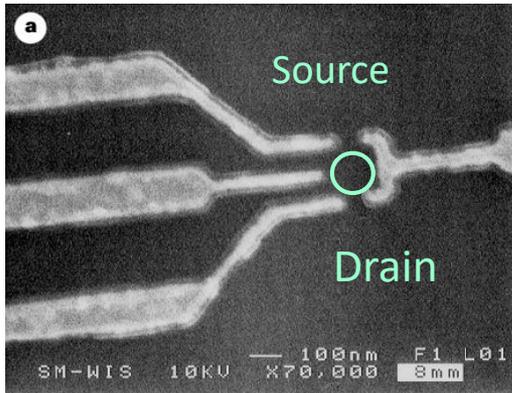
Nanotechnology has rekindled interest in the Kondo effect, one of the most widely studied phenomena in condensed-matter physics

# Revival of the Kondo effect

Leo Kouwenhoven and Leonid Glazman



The theory that describes the scattering of electrons from a localized magnetic impurity was initiated by the work of Jun Kondo in 1964



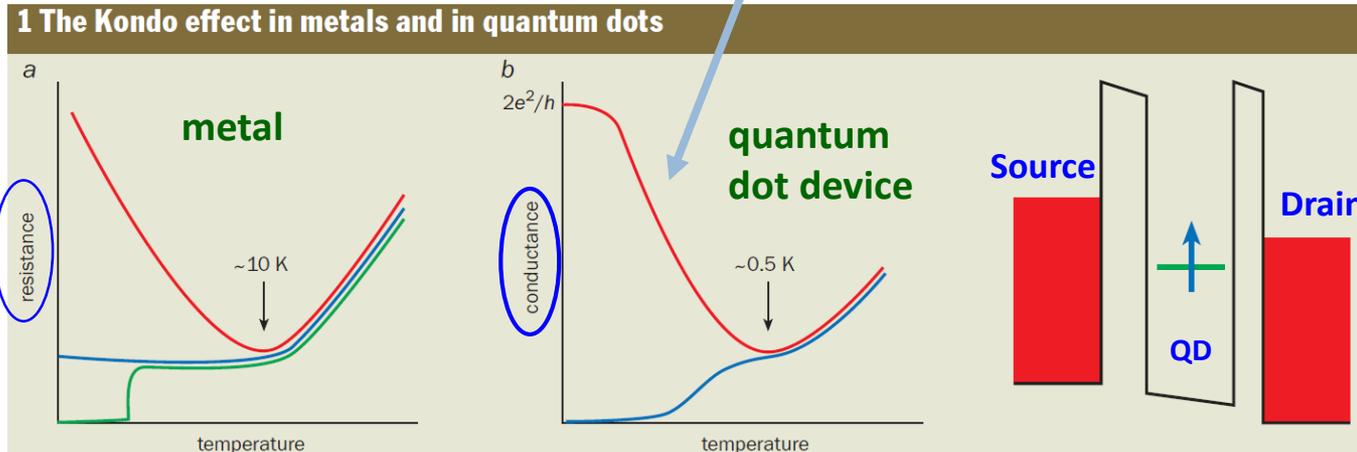
A semiconductor quantum dot ( $\sim 100$  nm) containing an **odd** number of electrons can act as a localized spin- $\frac{1}{2}$  magnetic impurity, giving rise to Kondo physics

$\Rightarrow$  **Kondo “conductance”  $G(T)$**

$T_K \sim 0.2$  K

A quantum dot ( $S=1/2$ ) coupled to source-drain electrodes

Goldhaber-Gordon et al., Nature 391, 156 (1998)



# Motivation

**two-channel**

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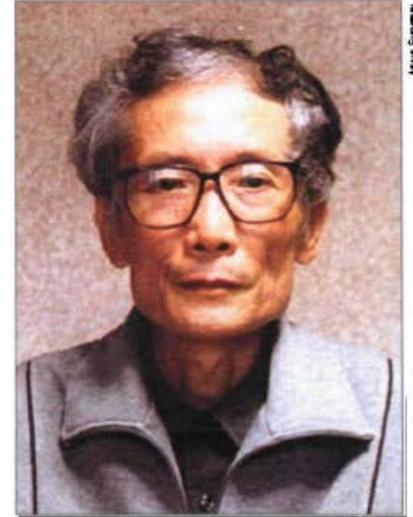
Nanotechnology has rekindled interest in the Kondo effect,  
one of the most widely studied phenomena in condensed-matter physics

## Revival of the Kondo effect

**Leo Kouwenhoven and Leonid Glazman**

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Phys. World **14**, 33 (2001)



The theory that describes the scattering of electrons from a localized magnetic impurity was initiated by the work of Jun Kondo in 1964

Adria Smeets

# A suggested route to 2CK effect

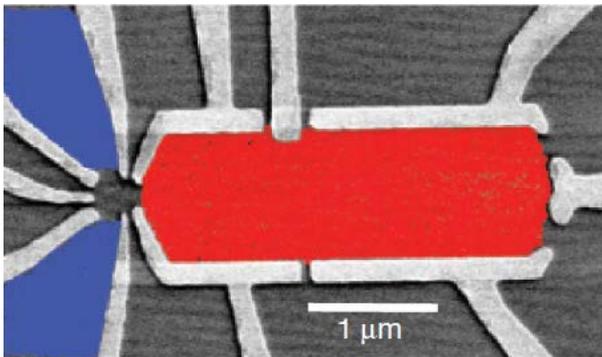
Vol 446 | 8 March 2007 | doi:10.1038/nature05556

nature

LETTERS

## Observation of the two-channel Kondo effect

R. M. Potok<sup>1,3,†</sup>, I. G. Rau<sup>2</sup>, Hadas Shtrikman<sup>4</sup>, Yuval Oreg<sup>4</sup> & D. Goldhaber-Gordon<sup>1</sup>

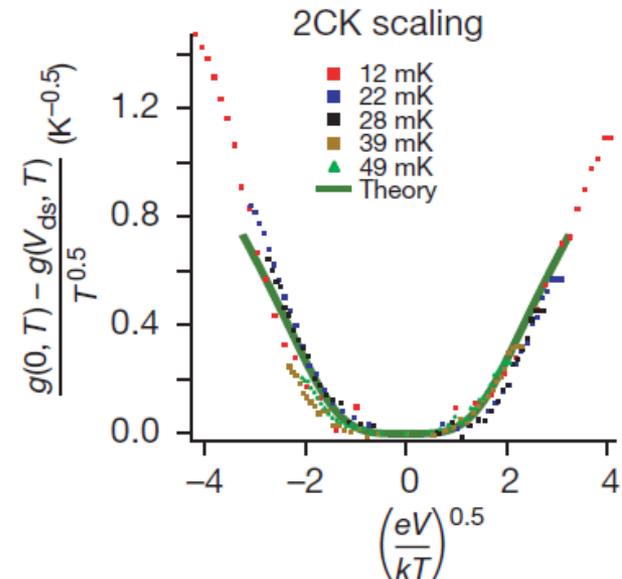


$$G(V, T) = \frac{dI(V, T)}{dV}$$

$\sqrt{T}$  temperature behavior  
A non-Fermi-liquid signature

### Problems and difficulties:

- 1) Fine-tuning is required.
- 2) Implications for real solids and topological quantum materials is unclear.
- 3)  $T_K$  value is very small.



# Orbital two-channel Kondo effect in real materials

## Experimental signature:

A  $\sqrt{T}$  resistivity increase at low temperatures (in the residual-resistivity regime). The resistivity increase is independent of an applied magnetic field.

$$\Delta\rho_{2CK}(T, B) \propto -n_d \sqrt{T} \quad n_d : \text{dynamic defect density}$$

## Altshuler & Aronov:      An ubiquitous effect in real conductors !

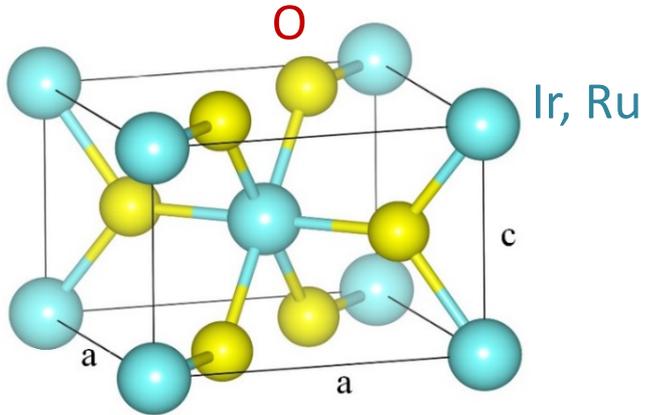
Electron-electron interaction (EEI) effect causes a  $\sqrt{T}$  resistivity increase at low temperatures in 3D weakly disordered metals.

$$\frac{\Delta\rho(T)}{\rho_0} = -\frac{0.915e^2}{4\pi^2\hbar} \left( \frac{4}{3} - \frac{3}{2}F \right) \rho_0 \sqrt{\frac{k_B T}{\hbar D}}$$

$D$ : electron diffusion constant  
 $0 \leq F \leq 1$ : a screening factor

The presence of impurities cause multiple elastic scattering, leading to quantum interference of electronic waves, which in turn results in enhanced e-e interaction.  $\Rightarrow$  The density of states at  $E_F$  is suppressed.

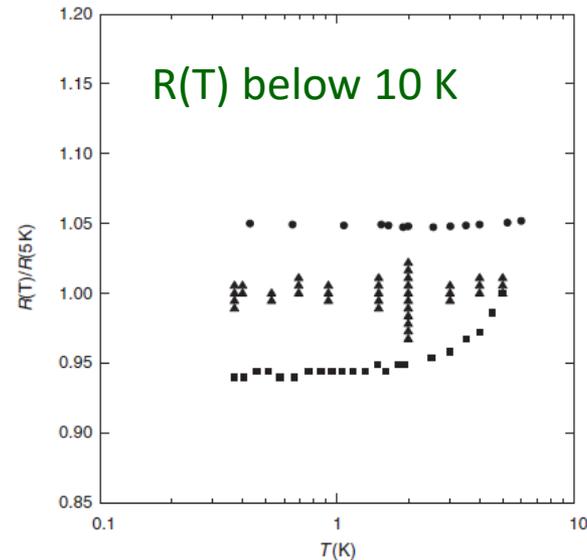
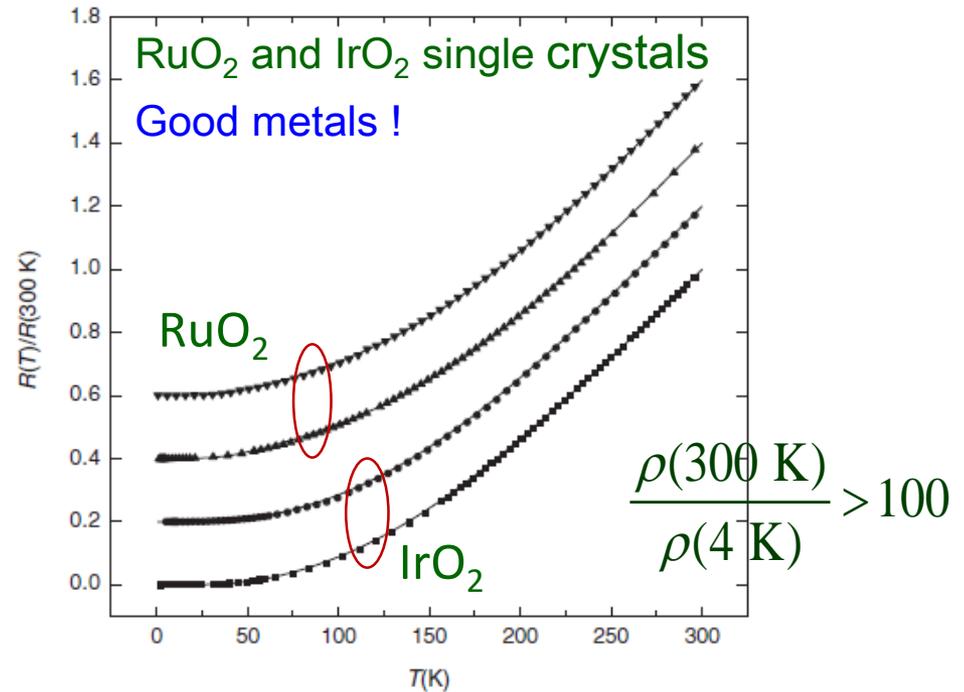
# $\text{IrO}_2$ and $\text{RuO}_2$ crystalizes in the rutile structure



Ir:  $[\text{Xe}]4f^{14}5d^76s^2$

$\text{Ir}^{+4}$ :  $[\text{Xe}]4f^{14}5d^5$

5d orbitals are half-filled in  $\text{IrO}_2$



# Recent discovery: Dirac nodal line metals IrO<sub>2</sub> and RuO<sub>2</sub>



Large spin Hall resistivity

PHYSICAL REVIEW B **99**, 195106 (2019)

ARTI

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Kohei F  
YoshiC

## Strong spin-orbit coupling and Dirac nodal lines in the three-dimensional electronic structure of metallic rutile IrO<sub>2</sub>

X. Xu,<sup>1,\*</sup> J. Jiang,<sup>2,3,4,\*</sup> W. J. Shi,<sup>5</sup> Vicky Süß,<sup>5</sup> C. Shekhar,<sup>5</sup> S. C. Sun,<sup>1</sup> Y. J. Chen,<sup>1</sup> S.-K. Mo,<sup>4</sup> C. Felser,<sup>5</sup> B. H. Yan,<sup>5</sup> H. F. Yang,<sup>2</sup> Z. K. Liu,<sup>2</sup> Y. Sun,<sup>5</sup> L. X. Yang,<sup>1,6,†</sup> and Y. L. Chen<sup>1,2,3,‡</sup>

<sup>1</sup>State Key Laboratory of Low Dimensional Quantum Physics, Department of Physics, Tsinghua University,

PHYSICAL REVIEW MATERIALS **3**, 064205 (2019)

Editors' Suggestion

## Dirac nodal lines protected against spin-orbit interaction in IrO<sub>2</sub>

J. N. Nelson,<sup>1</sup> J. P. Ruf,<sup>1</sup> Y. Lee,<sup>1</sup> C. Zeledon,<sup>2</sup> J. K. Kawasaki,<sup>3</sup> S. Moser,<sup>4</sup> C. Jozwiak,<sup>5</sup> E. Rotenberg,<sup>5</sup> A. Bostwick,<sup>5</sup> D. G. Schlom,<sup>2,6</sup> K. M. Shen,<sup>1,6,\*</sup> and L. Moreschini<sup>2,†</sup>

<sup>1</sup>Laboratory of Atomic and Solid State Physics, Department of Physics, Cornell University, Ithaca, New York 14853, USA

<sup>2</sup>Department of Materials Science and Engineering, Cornell University, Ithaca, New York 14853, USA

<sup>3</sup>Department of Materials Science and Engineering, University of Wisconsin, Madison, Wisconsin 53706, USA

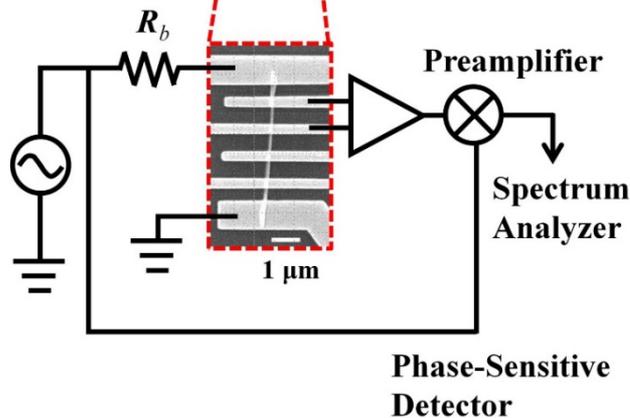
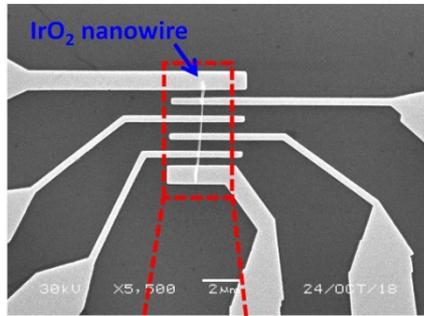
<sup>4</sup>Physikalisches Institut, Universität Würzburg, D-97074 Würzburg, Germany

<sup>5</sup>Advanced Light Source, Lawrence Berkeley National Laboratory, Berkeley, California 94720, USA

<sup>6</sup>Kavli Institute at Cornell for Nanoscale Science, Ithaca, New York 14853, USA

# Low-temperature Kondo resistivity in rutile nanowires

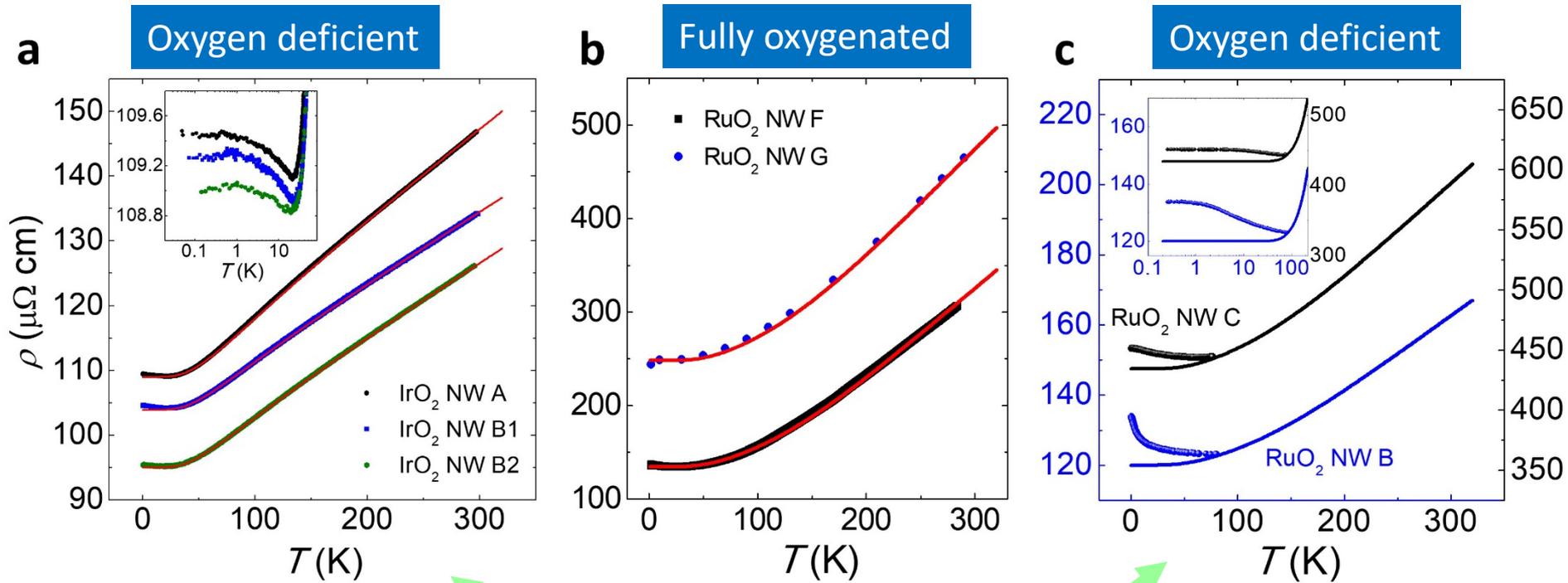
nanowire diameter  
 $\approx 50 - 190 \text{ nm}$



Nanowires were grown by Y.S. Huang's group (NTUST), and F.R. Chen & J.J. Kai's group (NTHU).

- IrO<sub>2</sub> nanowires were grown via MOCVD. RuO<sub>2</sub> nanowires were grown via thermal evaporation.
- Four-probe R(T) measurements down to 50 mK, in applied magnetic field up to 9 T.
- Nanowires were measured as-grown, after annealing in vacuum, and after oxygenation.
- **Thermal annealing in vacuum generates oxygen vacancies which generate dynamic scattering defects, causing orbital Kondo effect.**
- **The orbital Kondo effect is suppressed in (fully) oxygenated nanowires.**

# Resistivity vs. temperature for IrO<sub>2</sub> and RuO<sub>2</sub> nanowires

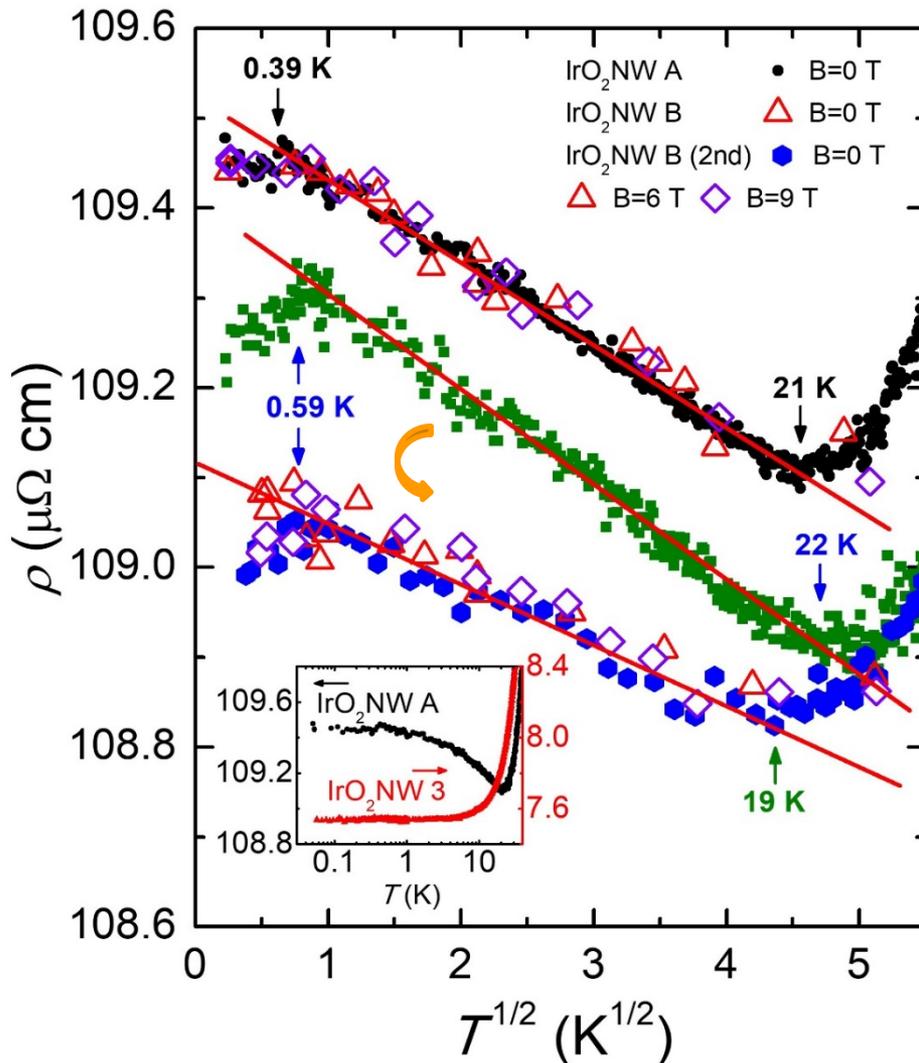


Thermal annealing in vacuum  
caused a low-T resistivity increase

The overall resistivity curve  $\rho(T)$  reveals Boltzmann-transport behavior.

The low-T resistivity increase can be repeatedly introduced (suppressed) by thermal annealing in vacuum (oxygen).

# $\sqrt{T}$ resistivity increase in paramagnetic IrO<sub>2</sub> nanowires



- A  $\sqrt{T}$  resistivity increase is found after annealing in vacuum.
- The  $\sqrt{T}$  resistivity increase shows insensitivity to magnetic field.
- After aging in air, the  $\sqrt{T}$  behavior persists, but showing a smaller resistivity increase.
- Oxygenation reduces dynamic scattering defects, producing a smaller orbital Kondo effect.
- A deviation from the  $\sqrt{T}$  behavior occurs around 0.5 K !

# Ruling out 3D electron-electron interaction effect

- A deviation from the  $\sqrt{T}$  dependence at  $\sim 0.5$  K is incompatible with the 3D EEI effect.
- The observed resistivity increase ( $\sim 0.5\%$ ) is more than one order of magnitude as would be predicted by the 3D EEI effect ( $\sim 0.03\%$ ).
- The residual resistivities  $\rho_0(\text{B1}) = 73.9 \mu\Omega \text{ cm}$  and  $\rho_0(\text{B2}) = 75.0 \mu\Omega \text{ cm}$  differ by  $\approx 1\%$ . The 3D EEI effect predicts a  $\approx 3\%$  difference in resistivity increase. But, experiment shows  $\approx 50\%$  difference.

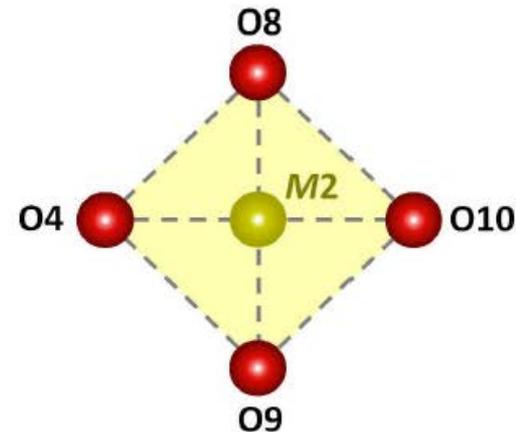
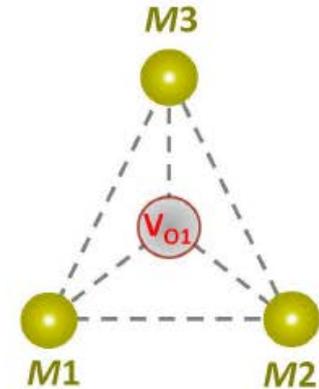
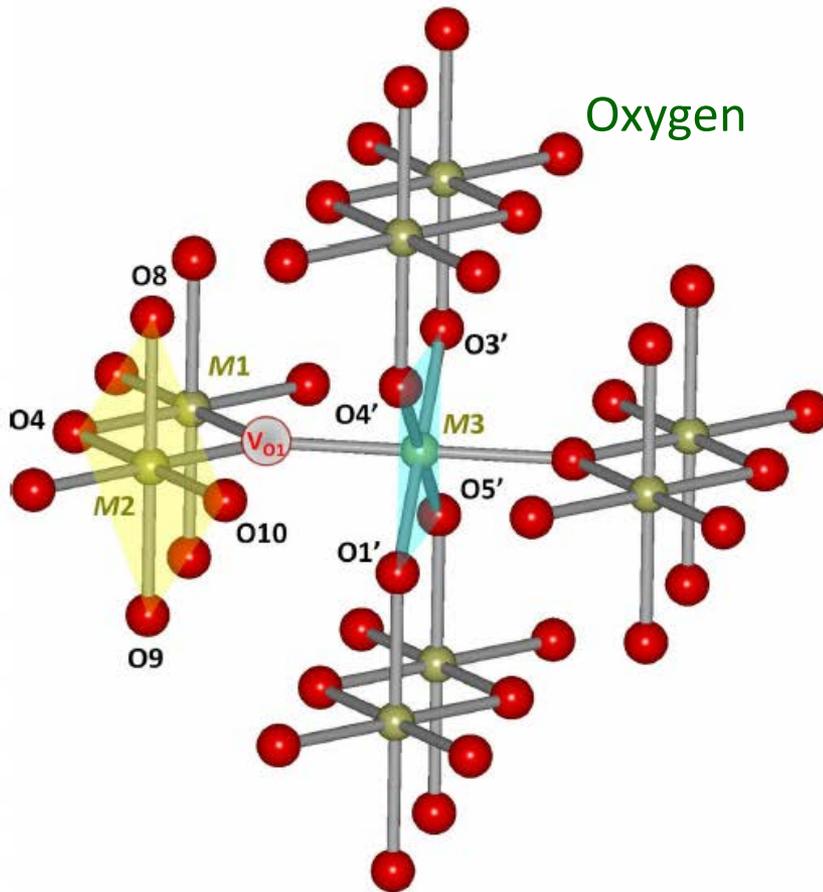
$$\frac{\Delta\rho(T)}{\rho(T_0)} = -\frac{0.915e^2}{4\pi^2\hbar} \left( \frac{4}{3} - \frac{3}{2} \tilde{F} \right) \rho(T_0) \sqrt{\frac{k_B}{\hbar D}} \left( \sqrt{T} - \sqrt{T_0} \right)$$

$\approx 3 \times 10^{-4}$  in our  $\text{MO}_2$  nanowires

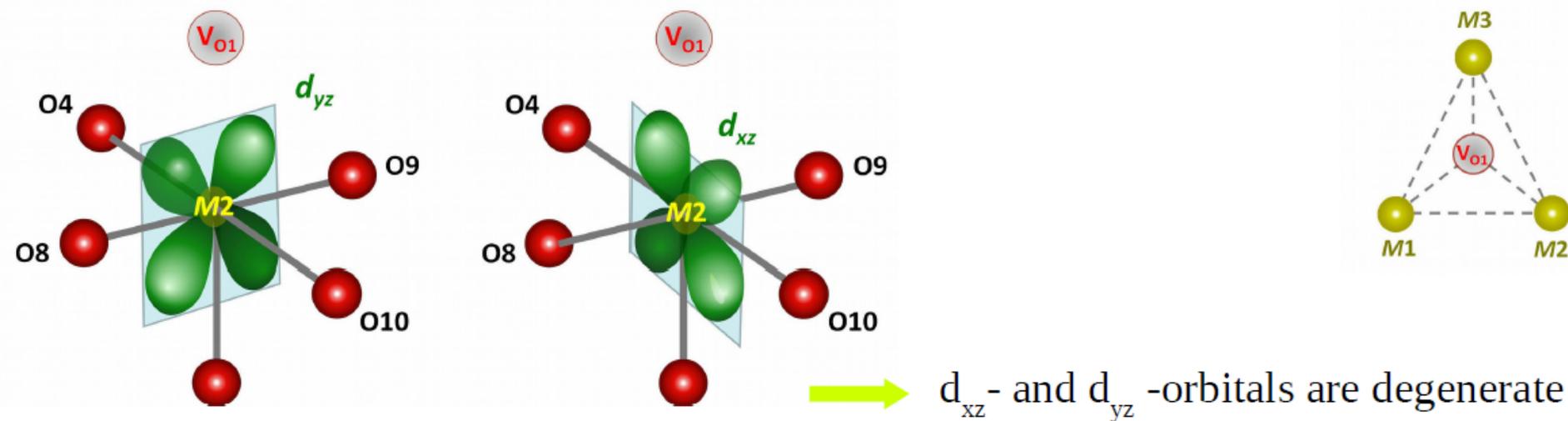
Independence of applied magnetic field of the resistivity increase is in accord with nonmagnetic orbital 2CK effect !

# Crystal Structure of $\text{MO}_2$ & Oxygen Vacancies

Oxygen vacancies lead to an almost perfect  $C_4$ -symmetry around the transition metal ions M1 & M2 next to the vacant site:



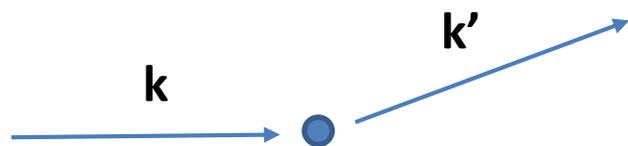
# Orbital two-channel Kondo effect in $\text{MO}_2$



- Every oxygen vacancy generates two *defect electrons* due to charge neutrality.
- Coulomb repulsion forces the *defect electrons* to localize at different transition metal ion sites near the vacancy site.
- For Ir-ions in  $\text{IrO}_2$ : 5d-shell is half-filled
- The defect electron at M2 (M1) can localize in the  $d_{xz}$ -orbital or  $d_{yz}$ -orbital – equivalent to spin-up and spin-down state  $\longrightarrow$  orbital Kondo effect
- Spin-degenerate conduction band: two independent scattering channels

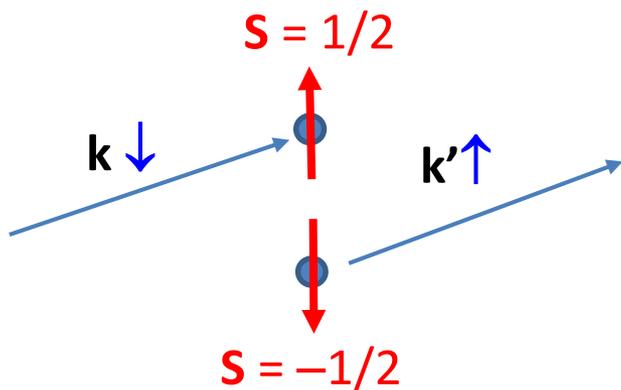
$\longrightarrow$  **Orbital two-channel Kondo effect**

# Heuristic picture for electron-quantum impurity scattering



Elastic electron-impurity scattering

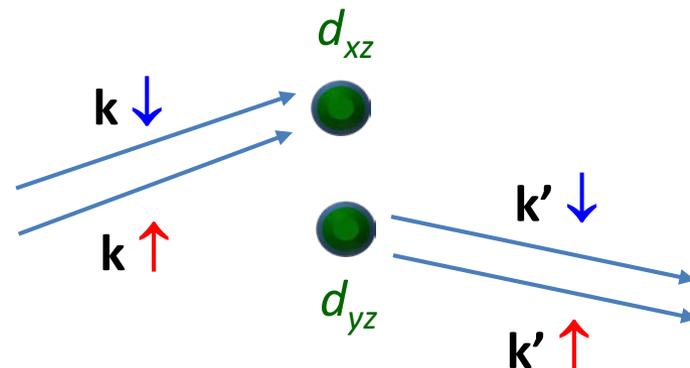
⇒ “residual resistivity”



Magnetic spin-flip scattering

⇒ Standard 1CK effect

$S = \pm 1/2$  degenerate doublet states



**Electron-quantum impurity scattering:**

The quantum impurity  $M^{+3}$  contains a **defect electron** which tunnels between the **two-fold degenerate**  $d_{xz}$  and  $d_{yz}$  orbitals.

The spin-up and spin-down conduction electrons act as two **independent** and **equivalent** channels.

⇒ **Nonmagnetic orbital 2CK effect !**

# Transport anomalies in $\text{MO}_2$

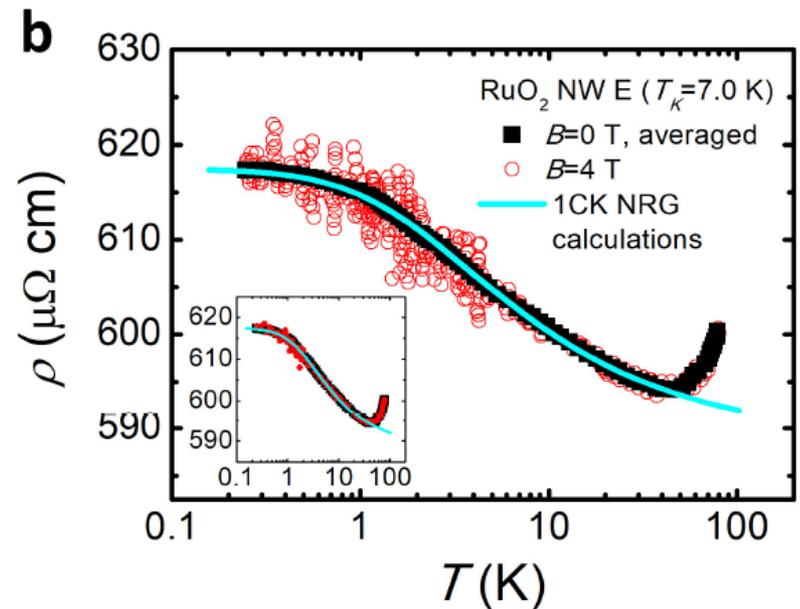
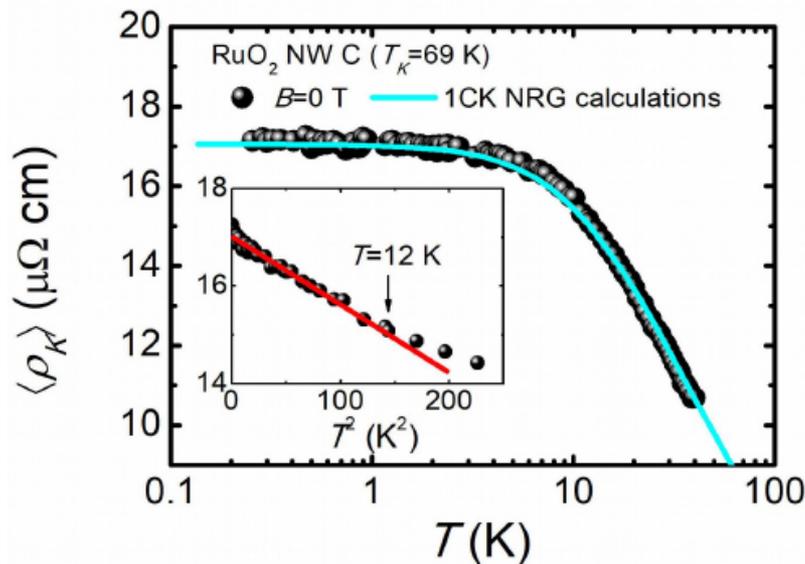
## Can we test that model?

Lifting the spin degeneracy would lead to an orbital one-channel Kondo effect

→ study anti-ferromagnetic  $\text{RuO}_2$  (same structure as  $\text{IrO}_2$ )

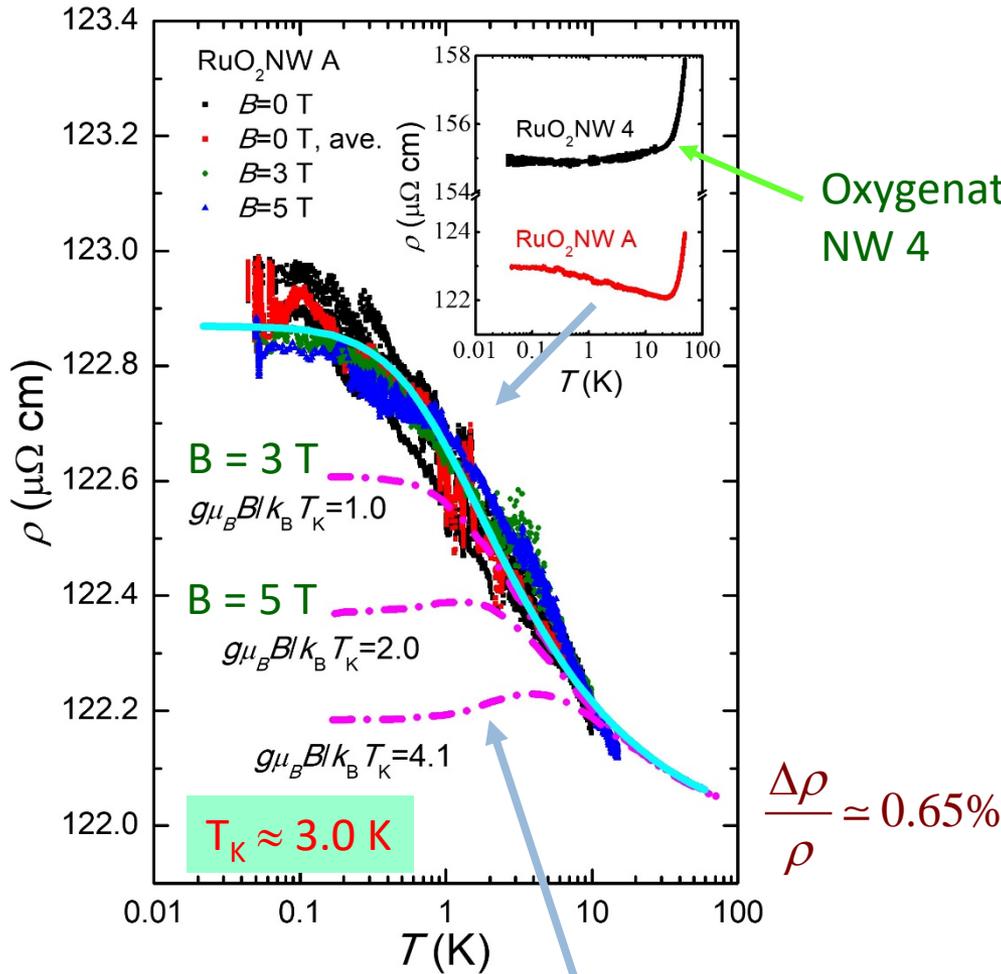
In  $\text{RuO}_2$  the  $4d_{xz}$  and  $4d_{yz}$  orbitals are half filled while the  $4d_{x^2-y^2}$  orbital is located well below the Fermi energy and is completely filled.

[ Berlijn et al. "Itinerant antiferromagnetism in  $\text{RuO}_2$ " Phys.Rev.Lett. (2017) ]



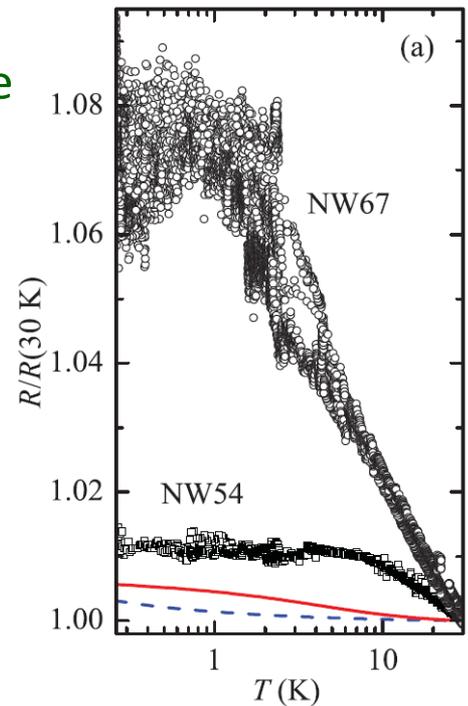
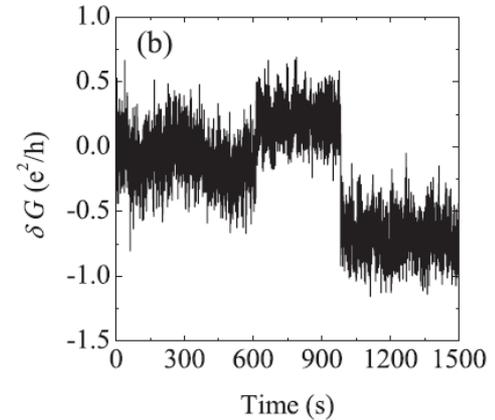
# The low-T resistance increase is insensitive to large magnetic fields !

$$g\mu_B B / k_B T_K \geq 1, T_K = 3.0 \text{ K}$$



Oxygenated NW 4

Temporal universal conductance fluctuations (UCFs) in RuO<sub>2</sub> wires

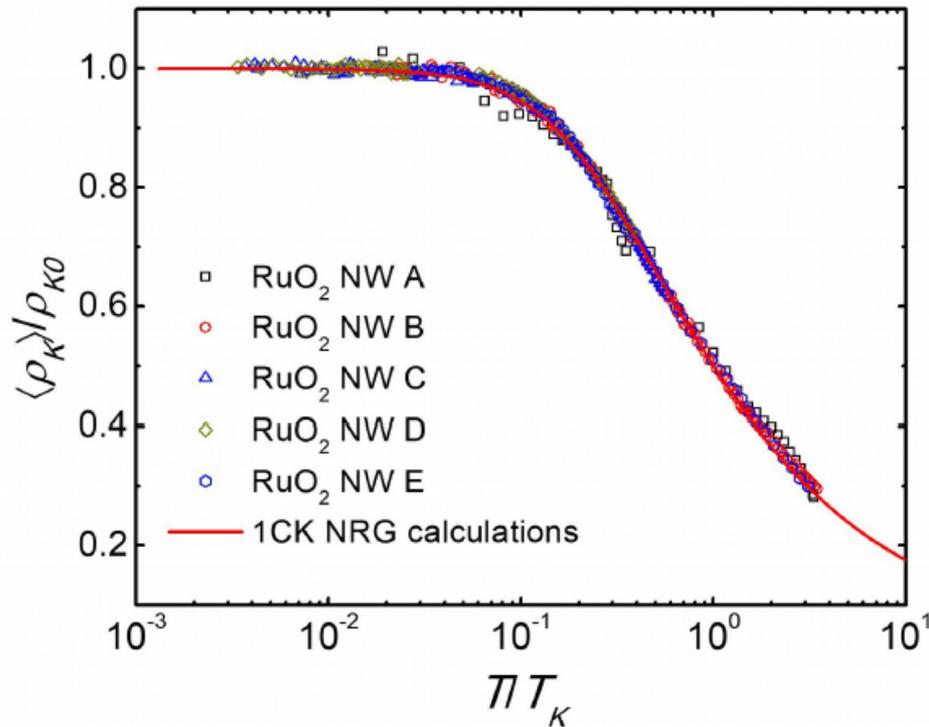


Magnetoconductance for magnetic spin-1/2 Kondo effect by NRG calculations.  
 T. A. Costi, PRL 85, 1504 (2000)

Lien et al., PRB 84, 155432 (2011)

# Transport anomalies in $\text{MO}_2$

## Orbital one-channel Kondo effect in anti-ferromagnetic $\text{RuO}_2$



Single-channel Kondo scaling  
over three decades in  $T/T_K$  !

$T_K$  values vary from 3 to 80 K. The  
Kondo resistivities conform to the  
universal 1CK scaling function !

Oxygen vacancies drive an orbital one-channel Kondo effect in  $\text{RuO}_2$  !

**Itinerant Antiferromagnetism in RuO<sub>2</sub>**

T. Berlijn,<sup>1,2</sup> P. C. Snijders,<sup>3,4</sup> O. Delaire,<sup>3,5</sup> H.-D. Zhou,<sup>4</sup> T. A. Maier,<sup>1,2</sup> H.-B. Cao,<sup>6</sup> S.-X. Chi,<sup>6</sup> M. Matsuda,<sup>6</sup>  
Y. Wang,<sup>3</sup> M. R. Koehler,<sup>7</sup> P. R. C. Kent,<sup>1,2</sup> and H. H. Weiering<sup>4,3</sup>

<sup>1</sup>Center for Nanophase Materials Sciences, Oak Ridge National Laboratory, Oak Ridge, Tennessee 37831, USA

<sup>2</sup>Computer Science and Mathematics Division, Oak Ridge National Laboratory, Oak Ridge, Tennessee 37831, USA

<sup>3</sup>Materials Science and Technology Division, Oak Ridge National Laboratory, Oak Ridge, Tennessee 37831, USA

PHYSICAL REVIEW LETTERS **122**, 017202 (2019)

<sup>7</sup>De

**Anomalous Antiferromagnetism in Metallic RuO<sub>2</sub> Determined by Resonant X-ray Scattering**

Z. H. Zhu,<sup>1,\*</sup> J. Stempfer,<sup>2</sup> R. R. Rao,<sup>3</sup> C. A. Occhialini,<sup>1</sup> J. Pellicciari,<sup>1</sup> Y. Choi,<sup>2</sup> T. Kawaguchi,<sup>4</sup>  
H. You,<sup>4</sup> J. F. Mitchell,<sup>4</sup> Y. Shao-Horn,<sup>3,5</sup> and R. Comin<sup>1,†</sup>

<sup>1</sup>Department of Physics, Massachusetts Institute of Technology, Cambridge, Massachusetts 02139, USA

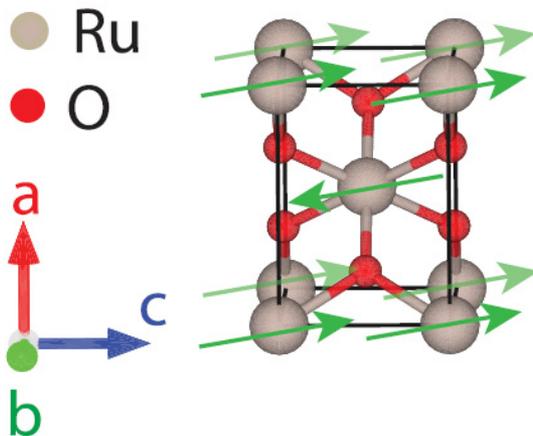
<sup>2</sup>Advanced Photon Source, Argonne National Laboratory, Argonne, Illinois 60439, USA

<sup>3</sup>Materials Science and Engineering, Massachusetts Institute of Technology, Cambridge, Massachusetts 02139, USA

<sup>4</sup>Computer Science and Mathematics Division, Argonne National Laboratory, Argonne, Illinois 60439, USA

<sup>5</sup>Materials Science and Engineering, Massachusetts Institute of Technology, Cambridge, Massachusetts 02139, USA

<sup>6</sup>Materials Science and Engineering, Massachusetts Institute of Technology, Cambridge, Massachusetts 02139, USA



# Ruling out 3D electron-electron interaction effect

- Conformation to the one-channel Kondo scaling form for three decades in  $T/T_K$  rules out the 3D EEI effect
- The observed resistivity increase is more than one order of magnitude as would be expected from the 3D EEI effect

$$\frac{\Delta\rho(T)}{\rho(T_0)} = -\frac{0.915e^2}{4\pi^2\hbar} \left( \frac{4}{3} - \frac{3}{2}\tilde{F} \right) \rho(T_0) \sqrt{\frac{k_B}{\hbar D}} \left( \sqrt{T} - \sqrt{T_0} \right)$$

$\approx 3 \times 10^{-4}$  in our  $\text{MO}_2$  nanowires

The insensitivity to applied magnetic field indicates nonmagnetic orbital one-channel Kondo effect !

# Recent 2CK experiment of layered compound Zr-As-Se (?)

PRL **117**, 106601 (2016)

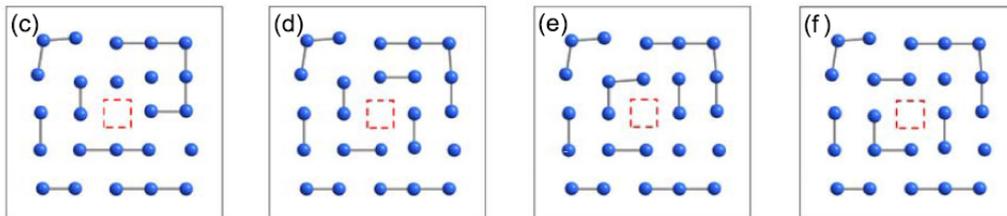
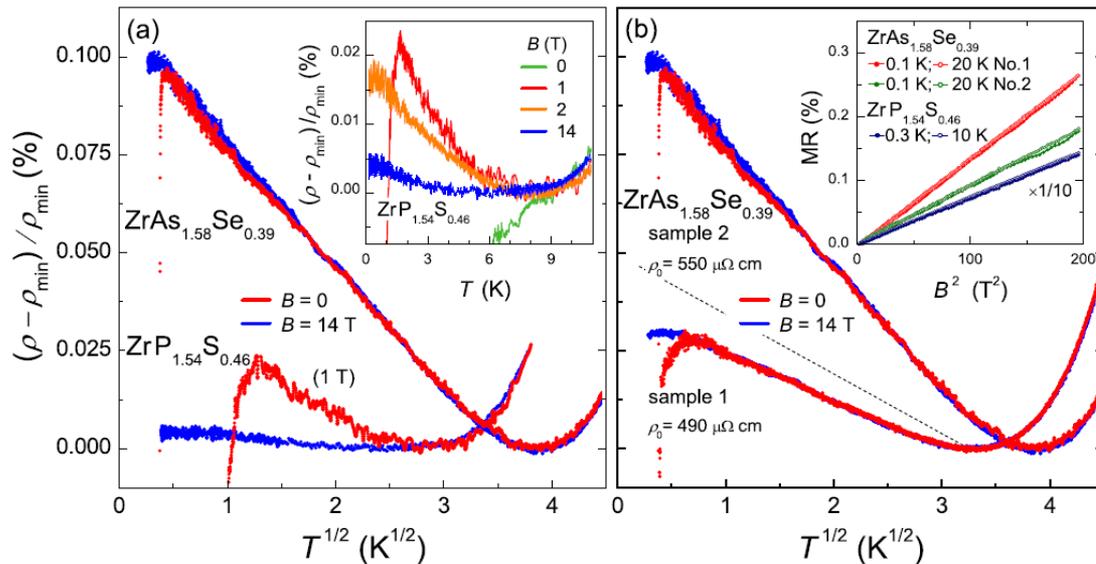
PHYSICAL REVIEW LETTERS

week ending  
2 SEPTEMBER 2016

## Two-Channel Kondo Physics due to As Vacancies in the Layered Compound $\text{ZrAs}_{1.58}\text{Se}_{0.39}$

T. Cichorek and L. Bochenek

*Institute of Low Temperature and Structure Research, Polish Academy of Sciences, 50-950 Wroclaw, Poland*



in collaboration with MPI Dresden, Zhejiang University

For the layered compound  $\text{ZrAs}_{1.58}\text{Se}_{0.39}$ , the authors argue that vacancies in the square nets of As give rise to the low- $T$  transport anomaly in line with the nonmagnetic version of the 2CK effect.

# Recent 2CK experiment of layered compound Zr-As-Se (?)

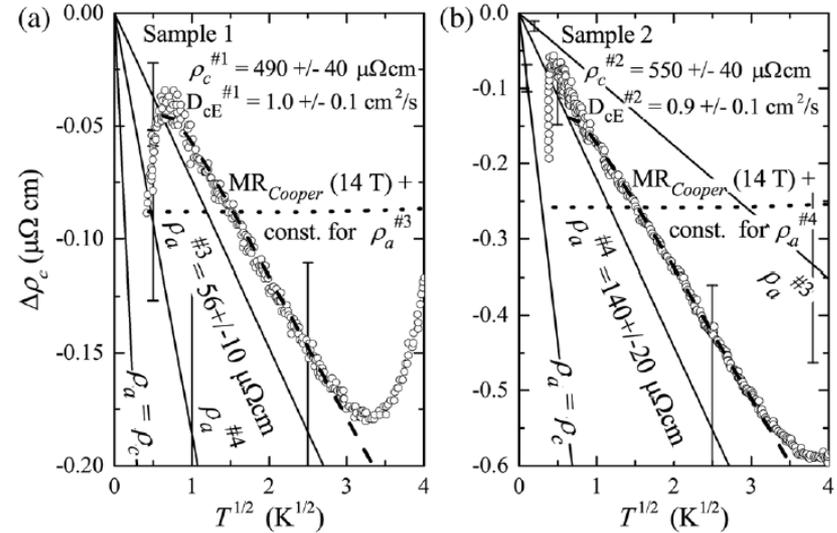
PRL 118, 259701 (2017)

PHYSICAL REVIEW LETTERS

week ending  
23 JUNE 2017

## Comment on “Two-Channel Kondo Physics due to As Vacancies in the Layered Compound $\text{ZrAs}_{1.58}\text{Se}_{0.39}$ ”

In a recent Letter [1], Cichorek *et al.* reported that a magnetic field independent  $AT^{1/2}$  term in the low-temperature resistivity of  $\text{ZrAs}_{1.58}\text{Se}_{0.39}$  could not be caused by electron-electron interaction (EEI) and could only be explained by a two-channel Kondo effect (2CKE). This statement was formulated on the basis of quantitative analysis of experimentally obtained  $A$ -coefficient values in light of the Altshuler-Aronov theory of EEI in disordered conductors [2]. The authors argue that even when the electron screening factor  $F = 0$ , the values of the  $A$  coefficient for samples 1 and 2 of single-crystalline  $\text{ZrAs}_{1.58}\text{Se}_{0.39}$  give unrealistic diffu-



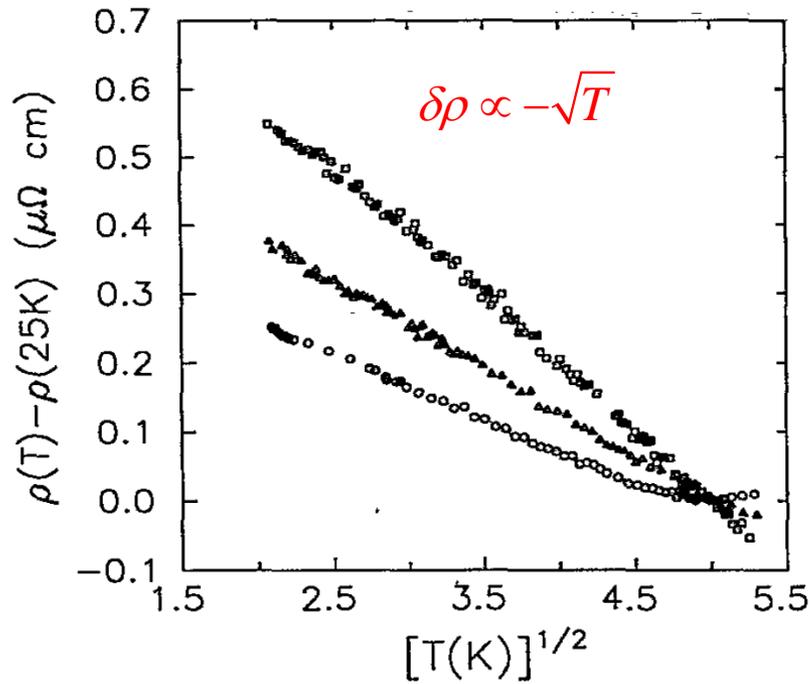
PHYSICAL REVIEW B 97, 134201 (2018)

## Origin of the $-|A|T^{1/2}$ term in the resistivity of disordered $\text{ZrAs}_{1.58}\text{Se}_{0.39}$

Daniel Gnida

Institute of Low Temperature and Structure Research, Polish Academy of Sciences, P.O. Box 1410, 50-950 Wrocław, Poland

# 3D electron-electron interaction effect in Ti-Al alloys



Resistivity increase for Al-doped Ti alloys with  $\rho_0 = 143, 167$  and  $204 \mu\Omega \text{ cm}$ .

Phys. Rev B 48, 5021 (1993)

吳至原副教授 (輔仁物理系)  
PhD in 1996, NTU Physics



# CONCLUSION

- IrO<sub>2</sub> and RuO<sub>2</sub> crystalize in the rutile structure, with approximate C<sub>4</sub> symmetry. Properties of the C<sub>4</sub> group imply **two-fold degeneracy** of the nonmagnetic impurity.
- In **paramagnetic** IrO<sub>2</sub>, the spin-degeneracy of the conduction bands is preserved. ⇒ **Orbital 2CK effect !**
- In **antiferromagnetic** RuO<sub>2</sub>, the conduction band is (locally) spin-polarized. ⇒ **Orbital 1CK effect !**
- The symmetries that enforces the existence of Dirac nodal lines also promote the formation of non-magnetic Kondo correlation.
- Both the emergence of the strange metallic state that accompanies unconventional superconductivity and the formation of the 2CK effect originate from strong electron interactions.

A quantum impurity (a localized spin, a moving electron or atom, etc.) with internal degree of freedom (two-fold degeneracy) generates the Kondo effect.

Kondo, 1976  
Nozieres, 1980  
Zawadowski, 1980s  
Many more .....