

hw4: $A = (x_1, y_1), B = (x_2, y_2), C = (x_3, y_3)$

prove that

$$\Delta ABC \text{ 之面積} = \frac{1}{2} |x_1 y_2 + x_2 y_3 + x_3 y_1 - x_2 y_1 - x_3 y_2 - x_1 y_3|$$

hw5: $w = \frac{1}{2}(-1 + \sqrt{3}i)$, 求 $w^{51} + w^{52} + \dots + w^{2001} = ?$ (1)

hw6: $1 < x < 2$, 若 $\log_2 x, \log_2 2x, \log_2 x^2$ 為一直角三角形之三邊長, 則 $x = ?$

$$2^{\frac{1+\sqrt{5}}{4}}$$

hw7: ① $\sin(\alpha + \beta)\sin(\alpha - \beta) = \sin^2 \alpha - \sin^2 \beta = \cos^2 \beta - \cos^2 \alpha$

② $\cos(\alpha + \beta)\cos(\alpha - \beta) = \cos^2 \alpha - \sin^2 \beta = \cos^2 \beta - \sin^2 \alpha$

hw8: prove that

1. 二倍角公式 $\sin 2\theta = \frac{2 \tan \theta}{1 + \tan^2 \theta} = 2 \sin \theta \cos \theta$

$$\cos 2\theta = \cos^2 \theta - \sin^2 \theta = \frac{1 - \tan^2 \theta}{1 + \tan^2 \theta}$$

2. 三倍角 $\sin 3\theta = 3 \sin \theta - 4 \sin^3 \theta$

$$\cos 3\theta = 4 \cos^3 \theta - 3 \cos \theta$$

3. 半角 $\sin^2 \frac{\theta}{2} = \frac{1 - \cos \theta}{2}$ $\cos \frac{2\theta}{2} = \frac{1 + \cos \theta}{2}$

hw9: 求 $\frac{d e^{\alpha x^2}}{dx} = ?$ $\frac{d}{dx}(\sqrt{x + \sqrt{x}}) = ?$

hw10: prove that $\frac{d}{dx} \left[\frac{f(x)}{g(x)} \right] = \frac{f'(x)}{g(x)} - \frac{g'(x)f(x)}{[g(x)]^2}$