

$$I = \frac{1}{3} ML^2$$

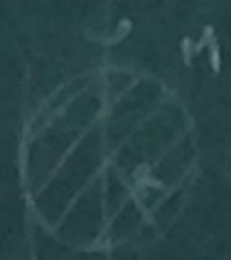
$$\tau = \frac{L}{2} \cdot Mg = I\alpha = \frac{1}{3} ML^2 \alpha$$

$$\alpha = \frac{3}{2} \frac{g}{L}$$

a

$$\frac{1}{2} I \omega^2 = \frac{1}{2} Mg L$$

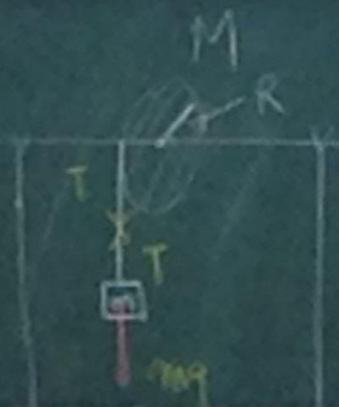
$$\frac{1}{3} ML^2 \omega^2 = Mg L \quad \omega = \sqrt{\frac{3g}{L}}$$



$$\frac{MR^2}{2}$$

$$\frac{1}{2} MR^2$$

$$\frac{1}{4} MR^2$$



$$I\alpha = TR \rightarrow a = \frac{TR}{I}$$

$$mg - T = ma \Rightarrow a = \frac{mg - T}{m} = R\alpha$$

$$mg - mR\alpha = T \Rightarrow mg = T + mR\frac{TR}{I}$$

$$= (1 + \frac{mR^2}{I})T$$

$$T = \frac{mg}{1 + \frac{mR^2}{I}}$$



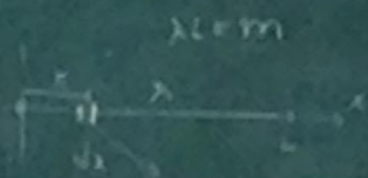
$$T = \frac{mg}{1 + \frac{MR^2}{I}}$$

$$= (1 + \frac{MR^2}{I}) T$$

$$mg - \frac{mg}{1 + \frac{MR^2}{I}} = ma$$

$$a = g \left(1 - \frac{1}{1 + \frac{MR^2}{I}} \right) = g \frac{MR^2/I}{1 + \frac{MR^2}{I}}$$

$$= g \frac{1}{1 + \frac{I}{MR^2}}$$



$m \int_0^L x^2 dx$

$L = \underbrace{m_1 v^2}_{\frac{1}{2} m v^2} + \underbrace{m_2 v^2}_{\frac{1}{2} m v^2} + \underbrace{I \frac{v}{R}}_{\frac{1}{2} I \frac{v^2}{R^2}}$

$\frac{dL}{dt} = \tau$

$\tau = m_1 g R - m_2 g R = \frac{dL}{dt} = (m_1 R + m_2 R + \frac{I}{R}) \frac{dv}{dt} \rightarrow a$

$a = \frac{(m_1 - m_2) g R}{(m_1 + m_2) R + \frac{I}{R}} = \frac{(m_1 - m_2) g}{m_1 + m_2 + \frac{I}{R^2}}$

$\vec{r} \times \vec{p}$

$I \vec{\omega}$



$$mgh = \frac{1}{2} \left(m + \frac{I_{cm}}{R^2} \right) v^2 \quad \frac{I_{cm}}{R^2} = \alpha$$
$$= \frac{1}{2} (m + \alpha) v^2$$

$$v^2 = \frac{2mgh}{m + \alpha} \Rightarrow v = \sqrt{\frac{2gh}{1 + \frac{I_{cm}}{mR^2}}}$$

