## Home Work 17

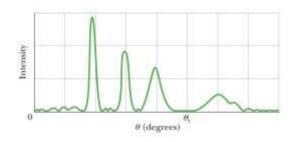
17-1 Manufacturers of wire (and other objects of small dimension) sometimes use a laser to continually monitor the thickness of the product. The wire intercepts the laser beam, producing a diffraction pattern like that of a single slit of the same width as the wire diameter. Suppose a helium–neon laser, of wavelength 632.8 nm,

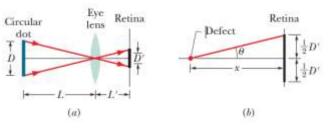
illuminates a wire, and the diffraction pattern appears on a screen at distance L = 2.60 m. If the desired wire diameter is 1.37 mm, what is the observed distance between the two tenth-order minima (one on each side of the central maximum)?

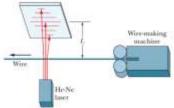
17-2 Floaters. The floaters you see when viewing a bright, featureless background are diffraction patterns of defects in the vitreous humor that fills most of your eye. Sighting through a pinhole sharpens the diffraction pattern. If you also view a

small circular dot, you can approximate the defect's size. Assume that the defect diffracts light as a circular aperture does. Adjust the dot's distance L from your eye (or eye lens) until the dot and the circle of the first minimum in the diffraction pattern appear to have the same size in your view. That is, until they have the same diameter D' on the retina at distance L' = 2.0 cm from the front of the eye, as suggested in Fig. a, where the angles on the two sides of the eye lens are equal. Assume that the wavelength of visible light is  $\lambda = 550$  nm. If the dot has diameter D = 2.0 mm and is distance L = 45.0 cm from the eye and the defect is x = 6.0 mm in front of the retina (Fig. b), what is the diameter of the defect?

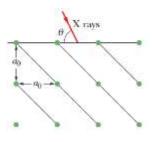
17-3 The Figure is a graph of intensity versus angular position  $\theta$  for the diffraction of an x-ray beam by a crystal. The horizontal scale is set by  $\theta_s = 2.00^\circ$ . The beam consists of two wavelengths, and the spacing between the reflecting planes is 0. 94 nm. What are the (a) shorter and (b) longer wavelengths in the beam?







17-4 In the Figure to the right, first-order reflection from the reflection planes shown occurs when an x-ray beam of wavelength 0.260 nm makes an angle  $\theta = 63.8^{\circ}$  with the top face of the crystal. What is the unit cell size  $a_0$ ?



17-5 A diffraction grating having 180 lines/mm is illuminated with a light signal containing only two wavelengths,  $\lambda_1 = 400$  nm and  $\lambda_2 = 500$  nm. The signal is incident perpendicularly on the grating. (a) What is the angular separation between the second-order maxima of these two wavelengths? (b) What is the smallest angle at which two of the resulting maxima are superimposed? (c) What is the highest order for which maxima for both wavelengths are present in the diffraction pattern?

17-6 The D line in the spectrum of sodium is a doublet with wavelengths 589.0 and 589.6 nm. Calculate the minimum number of lines needed in a grating that will resolve this doublet in the second-order spectrum.

17-7 With a particular grating the sodium doublet (589.00 nm and 589.59 nm) is viewed in the third order at  $10^{\circ}$  to the normal and is barely resolved. Find (a) the grating spacing and (b) the total width of the rulings.