

# Home Work 14

14-1 *More mirrors.* Object  $O$  stands on the central axis of a spherical or plane mirror. For this situation, each problem in the Table refers to (a) the type of mirror, (b) the focal distance  $f$ , (c) the radius of curvature  $r$ , (d) the object distance  $p$ , (e) the image distance  $i$ , and (f) the lateral magnification  $m$ . (All distances are in centimeters.) It also refers to whether (g) the image is real (R) or virtual (V), (h) inverted (I) or noninverted (NI) from  $O$ , and (i) on the *same* side of the mirror as object  $O$  or on the *opposite* side. Fill in the missing information. Where only a sign is missing, answer with the sign.

|    | (a)     | (b) | (c) | (d) | (e) | (f)   | (g) | (h)  | (i)  |
|----|---------|-----|-----|-----|-----|-------|-----|------|------|
|    | Type    | $f$ | $r$ | $p$ | $i$ | $m$   | R/V | I/NI | Side |
| 17 | Concave | 20  |     | +10 |     |       |     |      |      |
| 18 |         |     |     | +24 |     | 0.50  |     | I    |      |
| 22 |         | 20  |     |     |     | +0.10 |     |      |      |
| 23 |         | 30  |     |     |     | +0.20 |     |      |      |
| 29 | Convex  |     | 40  |     | 4.0 |       |     |      |      |

14-2 *Spherical refracting surfaces.* An object  $O$  stands on the central axis of a spherical refracting surface. For this situation, each problem in the Table refers to the index of refraction  $n_1$  where the object is located, (a) the index of refraction  $n_2$  on the other side of the refracting surface, (b) the object distance  $p$ , (c) the radius of curvature  $r$  of the surface, and (d) the image distance  $i$ . (All distances are in centimeters.) Fill in the missing information, including whether the image is (e) real (R) or virtual (V) and (f) on the *same* side of the surface as object  $O$  or on the *opposite* side.

|    |       | (a)   | (b)   | (c) | (d)  | (e) | (f)  |
|----|-------|-------|-------|-----|------|-----|------|
|    | $n_1$ | $n_2$ | $p$   | $r$ | $i$  | R/V | Side |
| 33 | 1.0   | 1.5   | +10   |     | -13  |     |      |
| 34 | 1.5   |       | + 100 | -30 | +600 |     |      |
| 35 | 1.5   | 1.0   | +70   | +30 |      |     |      |
| 36 | 1.5   | 1.0   |       | -30 | -7.5 |     |      |
| 37 | 1.5   | 1.0   | +10   |     | -6.0 |     |      |

14-3 *Thin lenses*. Object  $O$  stands on the central axis of a thin symmetric lens. For this situation, each problem in the Table gives object distance  $p$  (centimeters), the type of lens (C stands for converging and D for diverging), and then the distance (centimeters, without proper sign) between a focal point and the lens. Find (a) the image distance  $i$  and (b) the lateral magnification  $m$  of the object, including signs. Also, determine whether the image is (c) real (R) or virtual (V), (d) inverted (I) from object  $O$  or noninverted (NI), and (e) on the *same* side of the lens as object  $O$  or on the *opposite* side.

|    |      |        | (a) | (b) | (c) | (d)  | (e)  |
|----|------|--------|-----|-----|-----|------|------|
|    | $p$  | Lens   | $i$ | $m$ | R/V | I/NI | Side |
| 53 | +8.0 | D, 12  |     |     |     |      |      |
| 54 | +10  | D, 6.0 |     |     |     |      |      |
| 55 | +22  | D, 14  |     |     |     |      |      |
| 56 | +12  | D, 31  |     |     |     |      |      |
| 57 | +45  | C, 20  |     |     |     |      |      |

14-4 (a) A luminous point is moving at speed  $v_O$  toward a spherical mirror with radius of curvature  $r$ , along the central axis of the mirror. Show that the image of this point is moving at speed

$$v_1 = - \left( \frac{r}{2p - r} \right)^2 v_0,$$

where  $p$  is the distance of the luminous point from the mirror at any given time. Now assume the mirror is concave, with  $r = 15$  cm, and let  $v_O = 5.0$  cm/s. Find  $v_I$  when (b)  $p = 30$  cm (far outside the focal point), (c)  $p = 8.0$  cm (just outside the focal point), and (d)  $p = 10$  mm (very near the mirror).

14-5 The formula  $1/p + 1/i = 1/f$  is called the *Gaussian* form of the thin-lens formula. Another form of this formula, the *Newtonian* form, is obtained by considering the distance  $x$  from the object to the first focal point and the distance  $x'$  from the second focal point to the image. Show that  $xx' = f^2$  is the Newtonian form of the thin-lens formula.