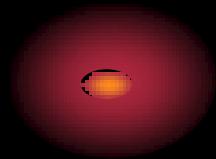
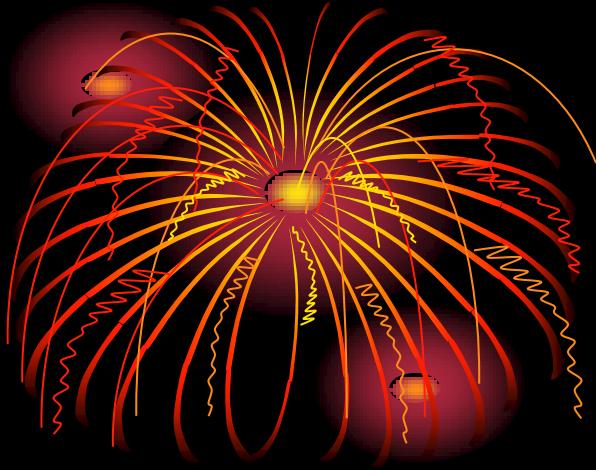


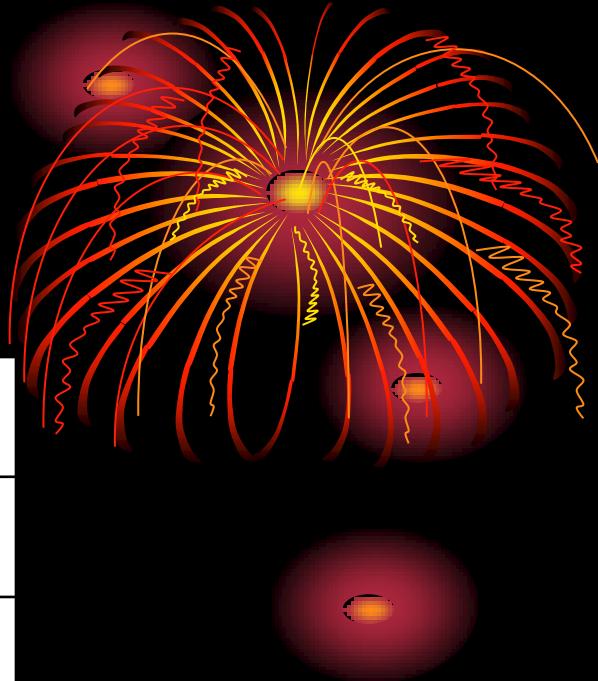
102學年上學期高二物理

黃信健



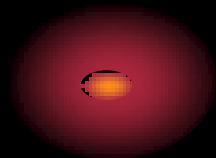
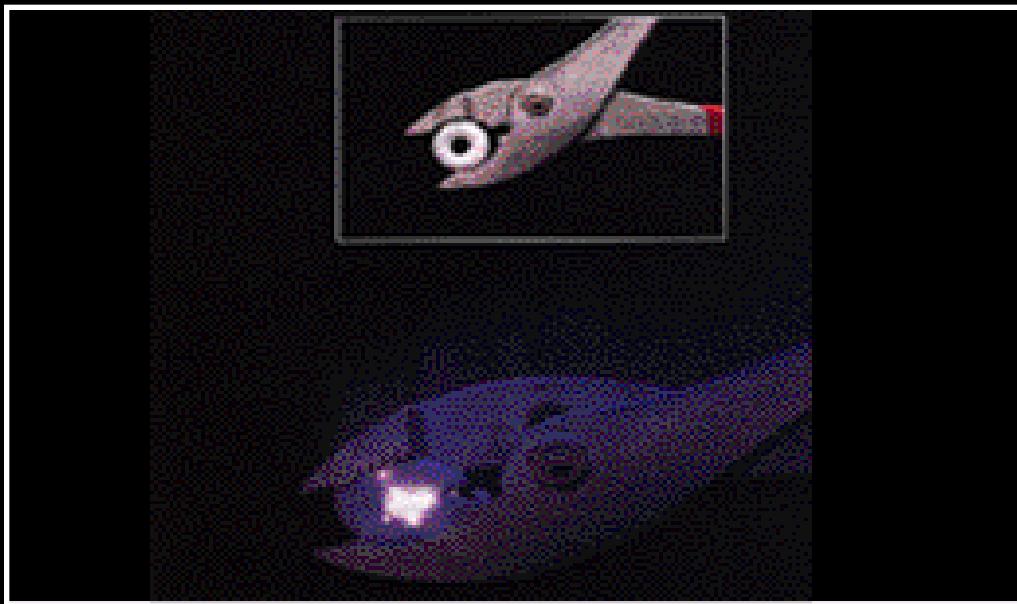
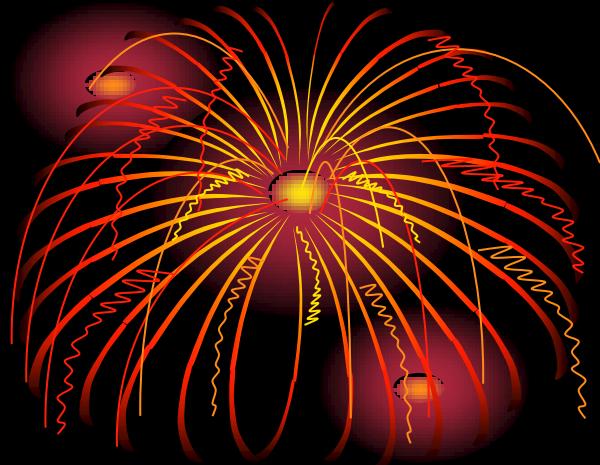
# 電磁學、光學與 量子物理

# 課程表



日期	內容
2013/10/19 (一)	<u>1電荷、靜電的應用</u>
2013/11/02 (二、三)	<u>2電力與電場</u>
2013/11/16 (四)	<u>3高斯定律</u>
2013/11/30 (五)	<u>4電位</u>
2013/12/14 (六)	<u>5電容</u>
2013/12/28 (七)	<u>6電流與電阻</u>
2013/01/11 (八)	<u>7電路</u>

# 電磁學



What causes the “sparking” of a wintergreen lifesaver?

# 電磁學

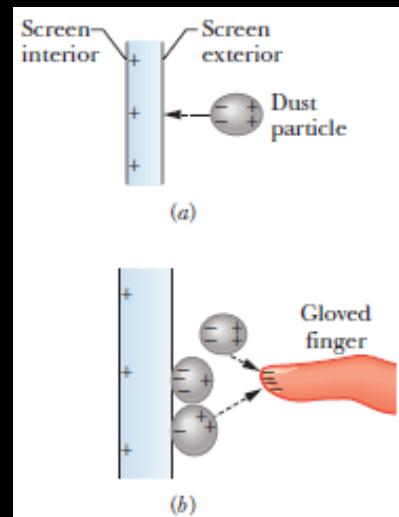
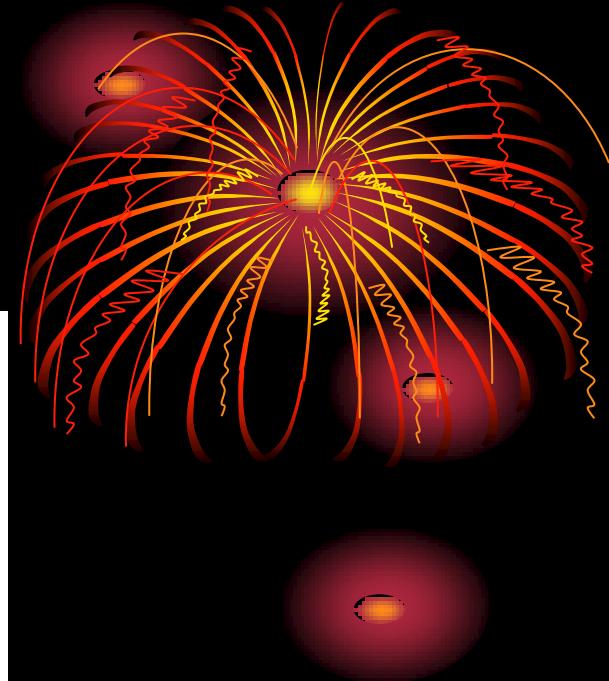


Source: Adapted from Sanyi Insights, Inc.

Hospital personnel go to extraordinary lengths to avoid bacterial infection of a patient. Surfaces are scrubbed, masks are donned, hands are meticulously cleaned and then gloved, and instruments are sanitized at high temperature and in alcohol baths. But there are still subtle sources of bacteria, such as possibly in this photograph.

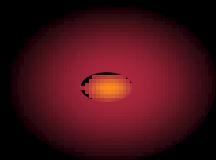
*Can you find  
the bacterial  
source?*

The answer is in this chapter.



# 電磁學 (Electromagnetism)

## 電學 (Electricity)



1. 電荷

2. 電場

3. 高斯定律

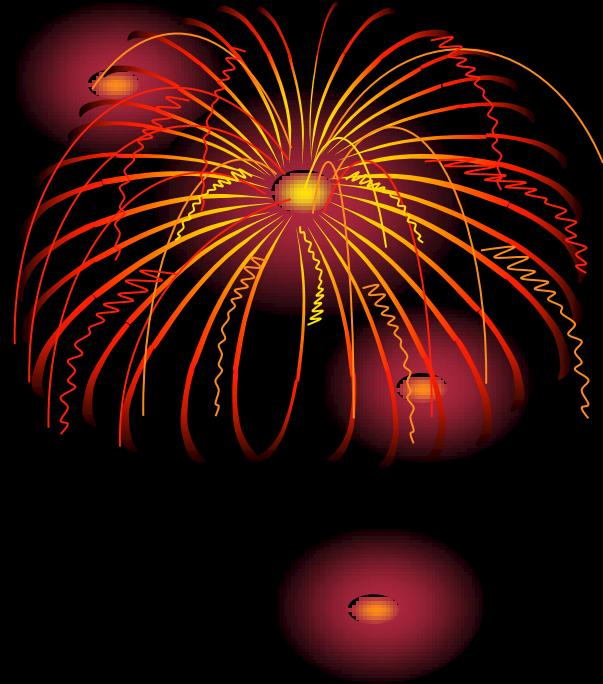
4. 電位

5. 電容

6. 電流與電阻

7. 電路

# 磁學 (Magnetism)



8. 電流與磁場

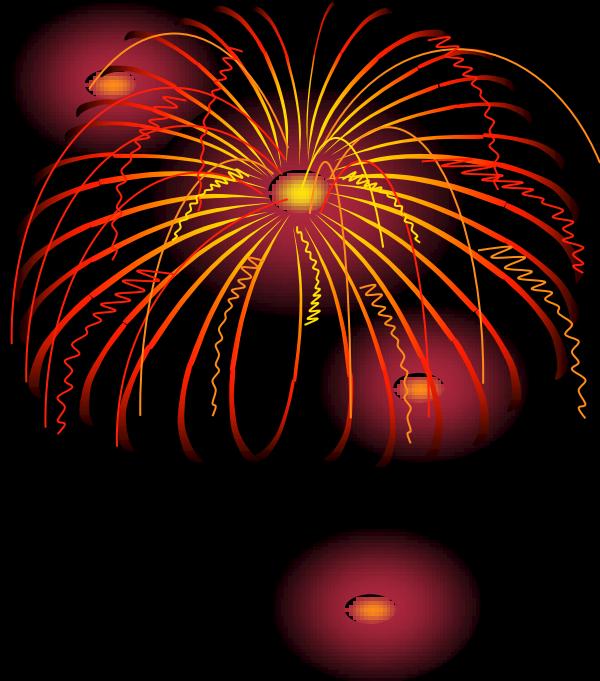
9. 電磁感應

10. 物質的磁性

11. 反射、折射、干涉、繞射

12. 量子物理

# 1-1 電荷、電力與電場

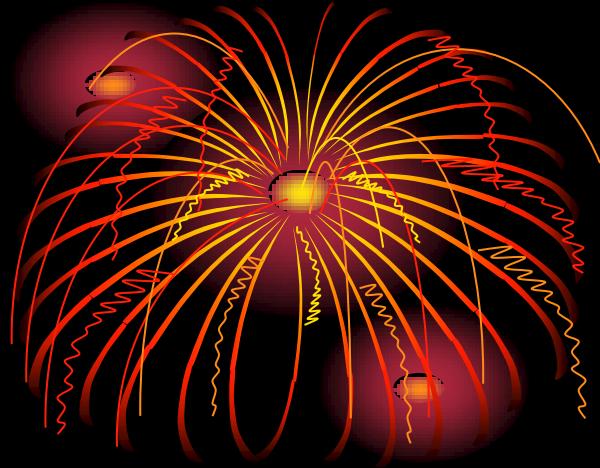


1.1 電荷 (electric charge)

1.2 庫倫定律 (Coulomb's law)

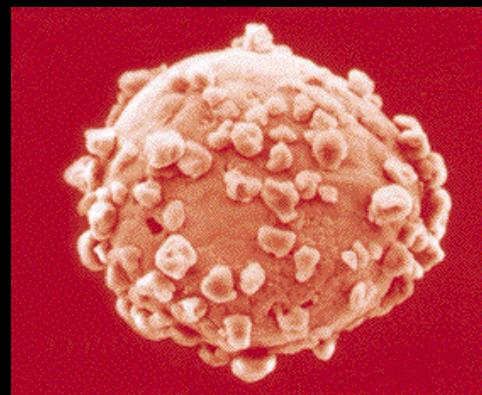
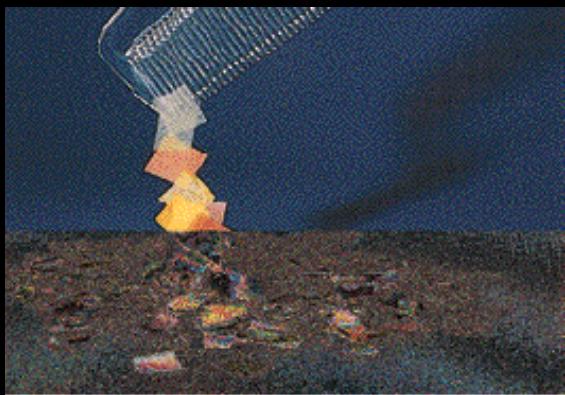
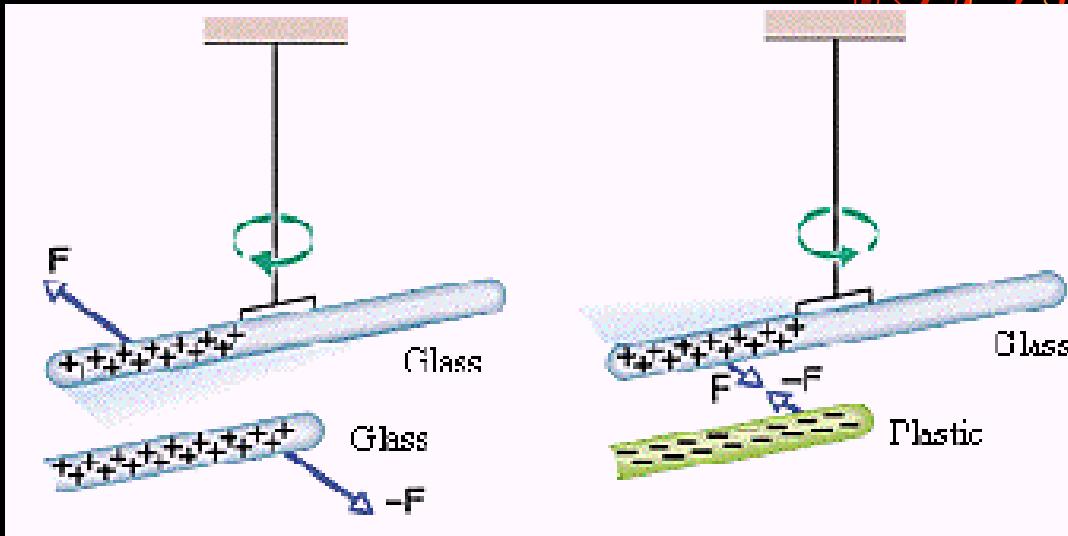
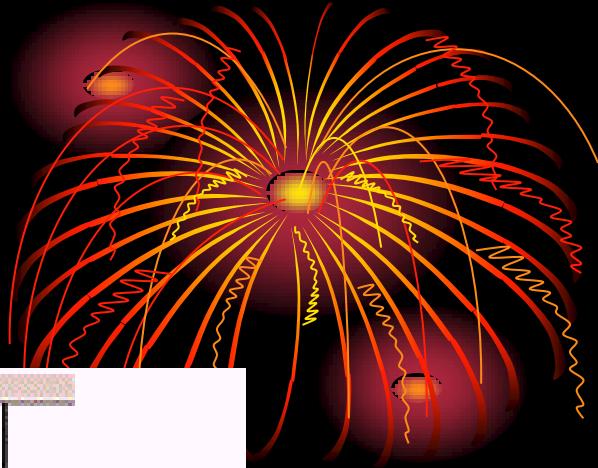
1.3 靜電的應用

# 1.1 電荷

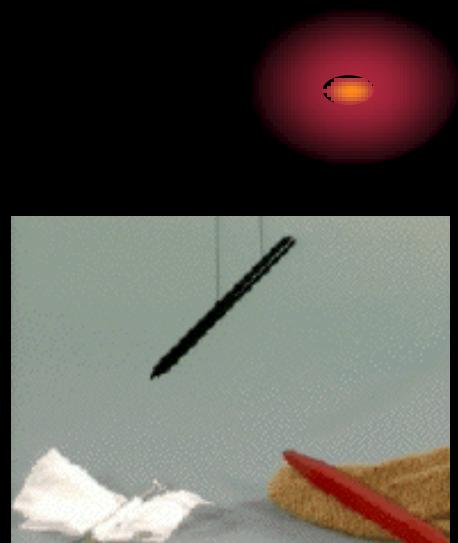
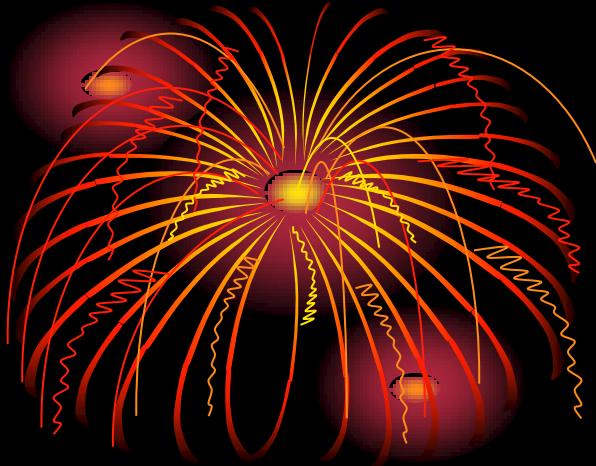


- 摩擦充電
- 塑膠棒（負荷電）與毛皮（正荷電）
- 玻璃棒（正荷電）與絲綢（負荷電）
- 感應充電

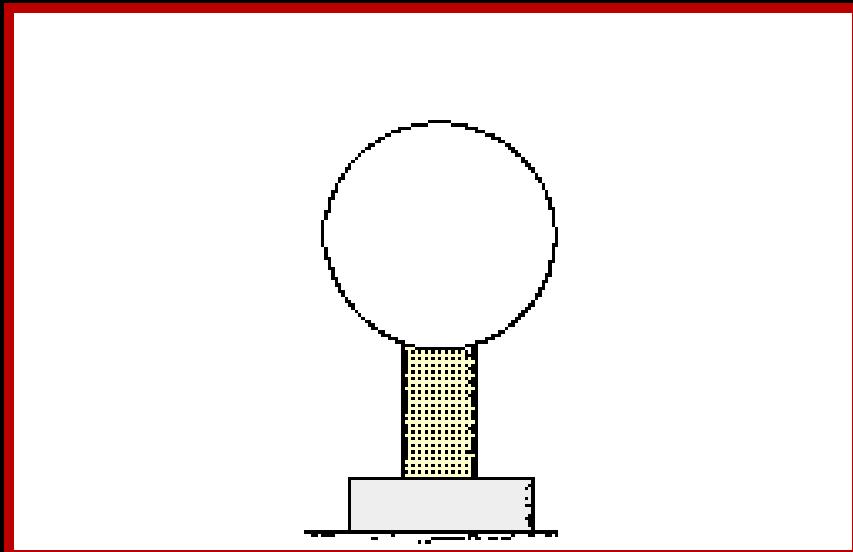
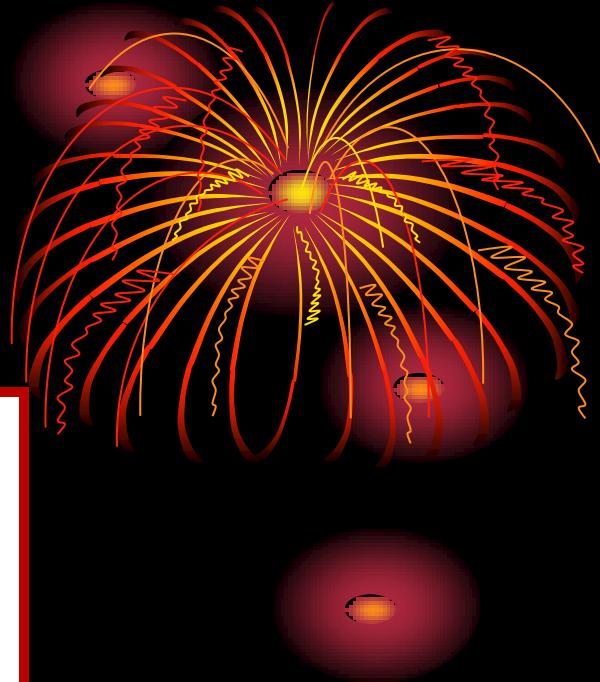
# 正荷電與負荷電



# 摩擦充電

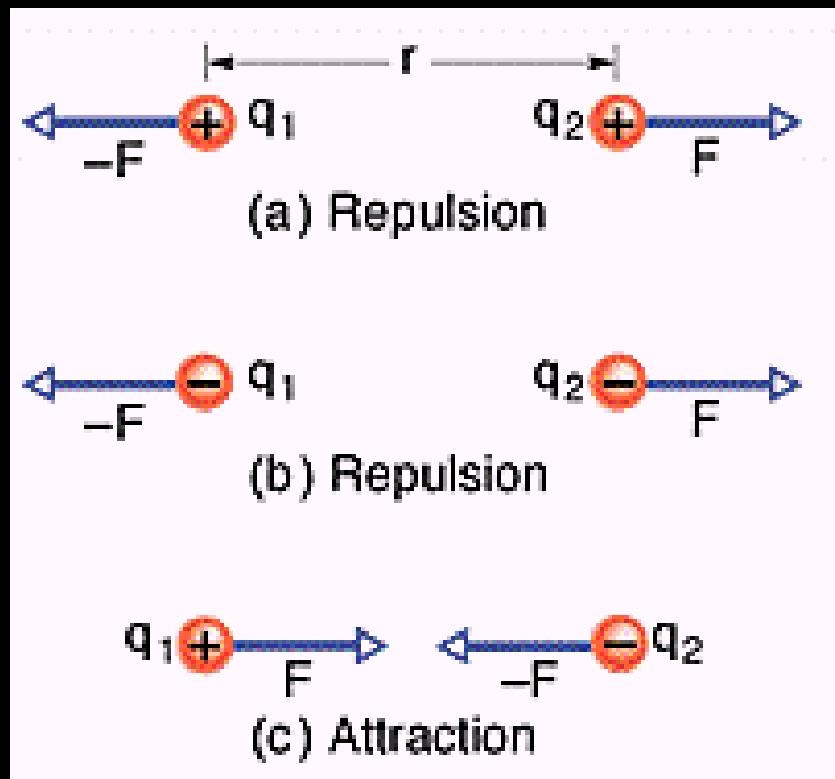
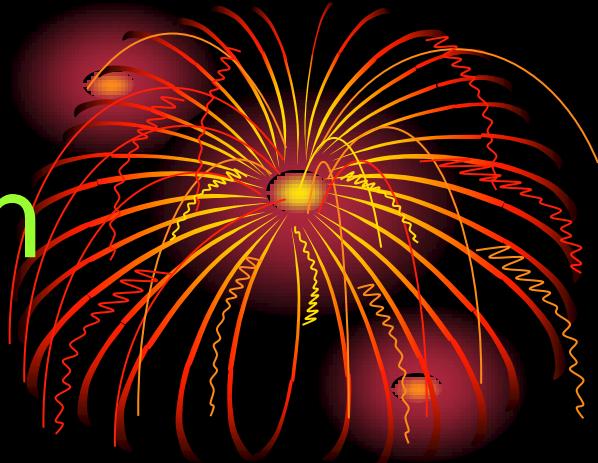


# 感應充電



A negatively charged object is brought near to a neutral, conducting sphere. Electrons in the sphere are forced from the left side of the sphere to the right side.

# The Electric Interaction



# Charge is quantized



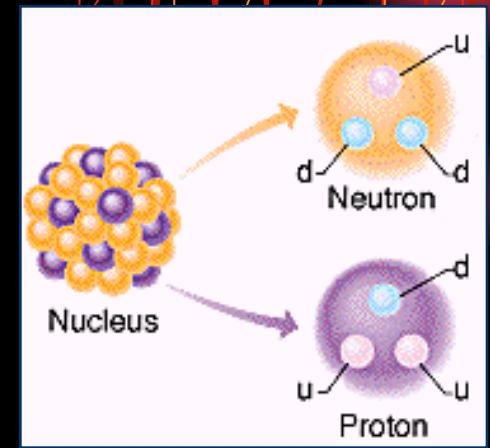
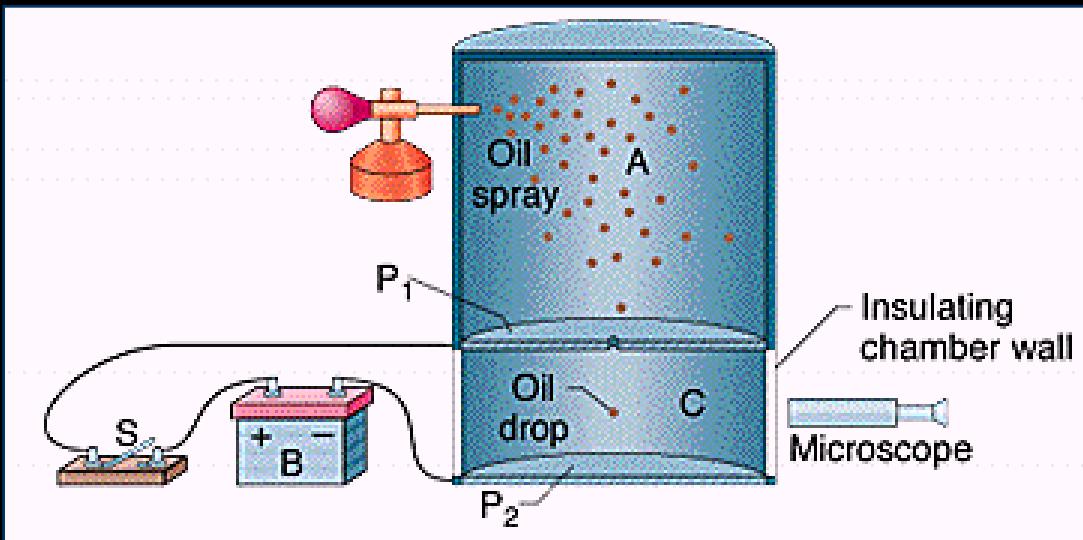
- The electric charge ( $e$ ) is discrete (quantized)

$$q = ne, n = \pm 1, \pm 2, \pm 3, \dots$$

$$e = 1.6 \times 10^{-19} C$$

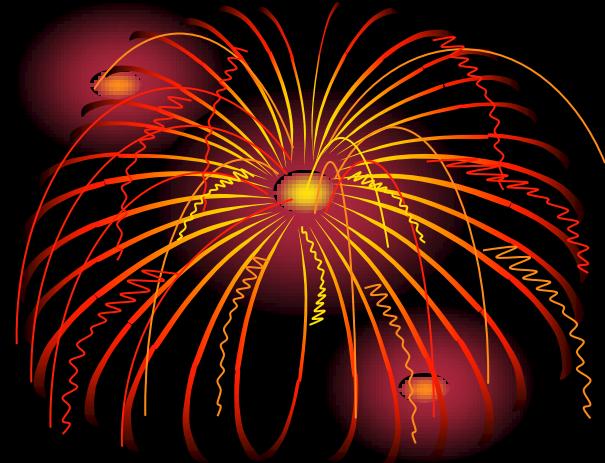
- SI unit: coulomb (C), defined in term of ampere

# Millikan's Oil Drop Experiment

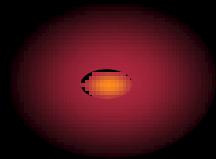
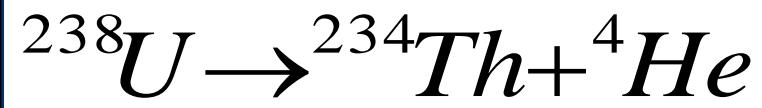


- Quarks:  $q = \pm e / 3$  or  $\pm 2e / 3$

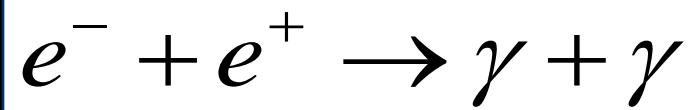
# Charge is conserved



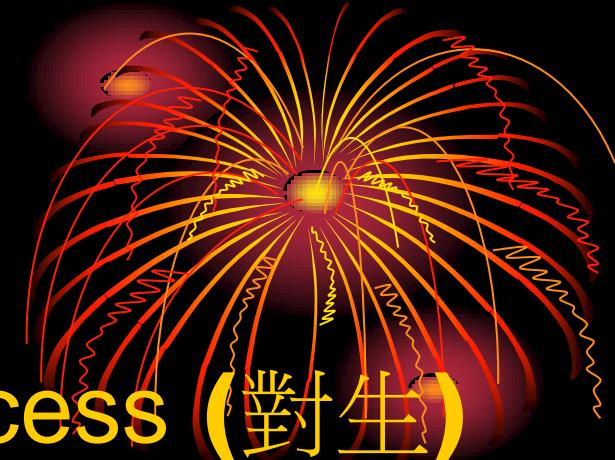
- The radioactive decay



- The annihilation process (對滅)

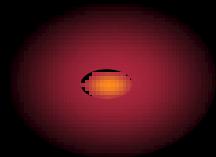


# Elementary Particles



- The pair production process (對生)

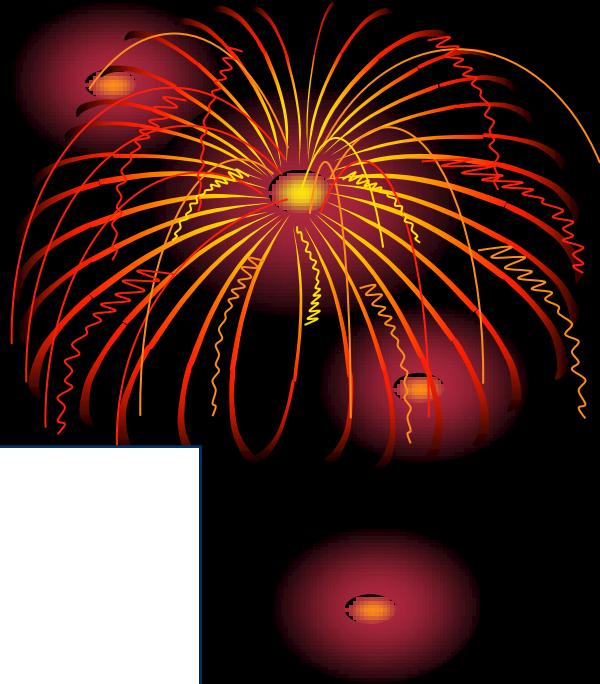
$$\gamma \rightarrow e^- + e^+$$



- The bubble (cloud) chamber



# 1.2 Coulomb's Law



$$F = k \frac{|q_1||q_2|}{r^2}$$

$$k = \frac{1}{4\pi\epsilon_0} = 8.99 \times 10^9 N \cdot m^2 / C^2$$

$$\epsilon_0 = 8.85 \times 10^{-12} C^2 / N \cdot m^2 = \text{permittivity}$$

## Ex. 1-1 一庫倫負電荷含有多少電子

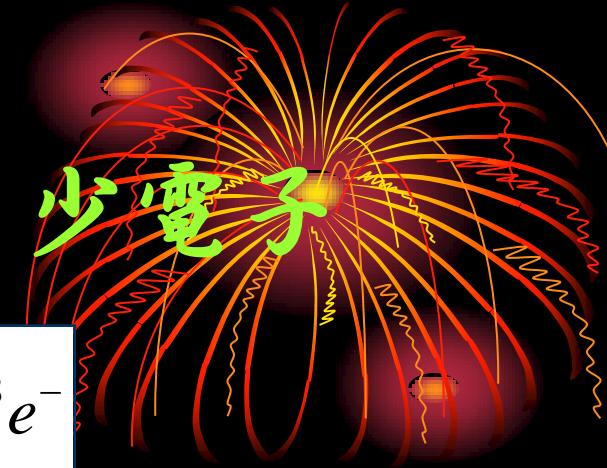
$$N = \frac{q}{e} = \frac{1.00\text{Coul}}{1.6 \times 10^{-19}\text{C/e}} = 6.25 \times 10^{18} e^-$$

## Ex. 1-2 氢原子內電子與質子之間電力與重力之比

$$F_e = \frac{q_1 q_2}{4\pi\epsilon_0 r^2} = \left(9 \times 10^9 \frac{N \cdot m^2}{C^2}\right) \frac{(1.60 \times 10^{-19} C)^2}{(5.3 \times 10^{-11} m)^2} = 8.2 \times 10^{-8} N$$

$$F_g = \frac{G m_e m_p}{r^2} = 6.67 \times 10^{-11} \frac{Nm^2}{kg^2} \frac{(9.11 \times 10^{-31} kg)(1.67 \times 10^{-27} kg)}{(5.3 \times 10^{-11} m)^2} = 3.6 \times 10^{-47} N$$

$$\frac{F_e}{F_g} = \frac{K q_e q_p}{G m_e m_p} \cong 10^{39}$$



# Ex. 1-3 鐵 ( $Fe^{26}$ ) 原子核中，兩個相距 一個原子核半徑的質子間之斥力

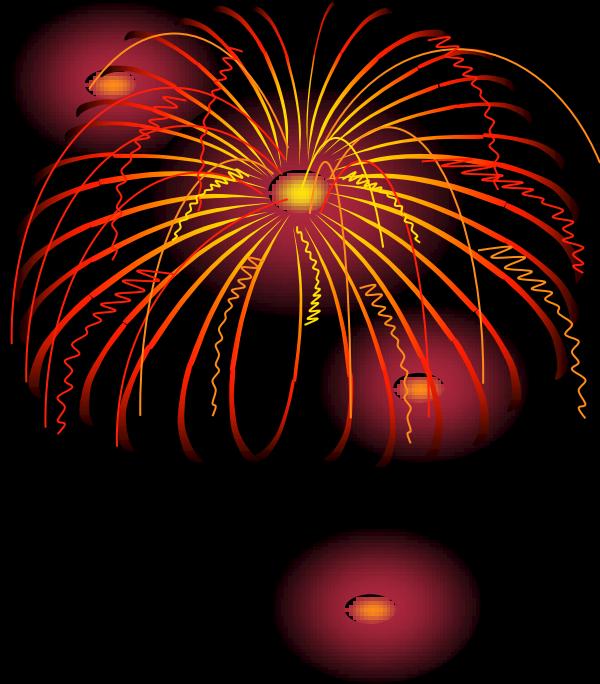


$$F_e = \frac{q_P q_P}{4\pi\epsilon_0 r^2} = 8.99 \times 10^9 \frac{N \cdot m^2}{C^2} \frac{(1.60 \times 10^{-19} C)^2}{(4 \times 10^{-15} m)^2} = 14N \sim 3lb$$

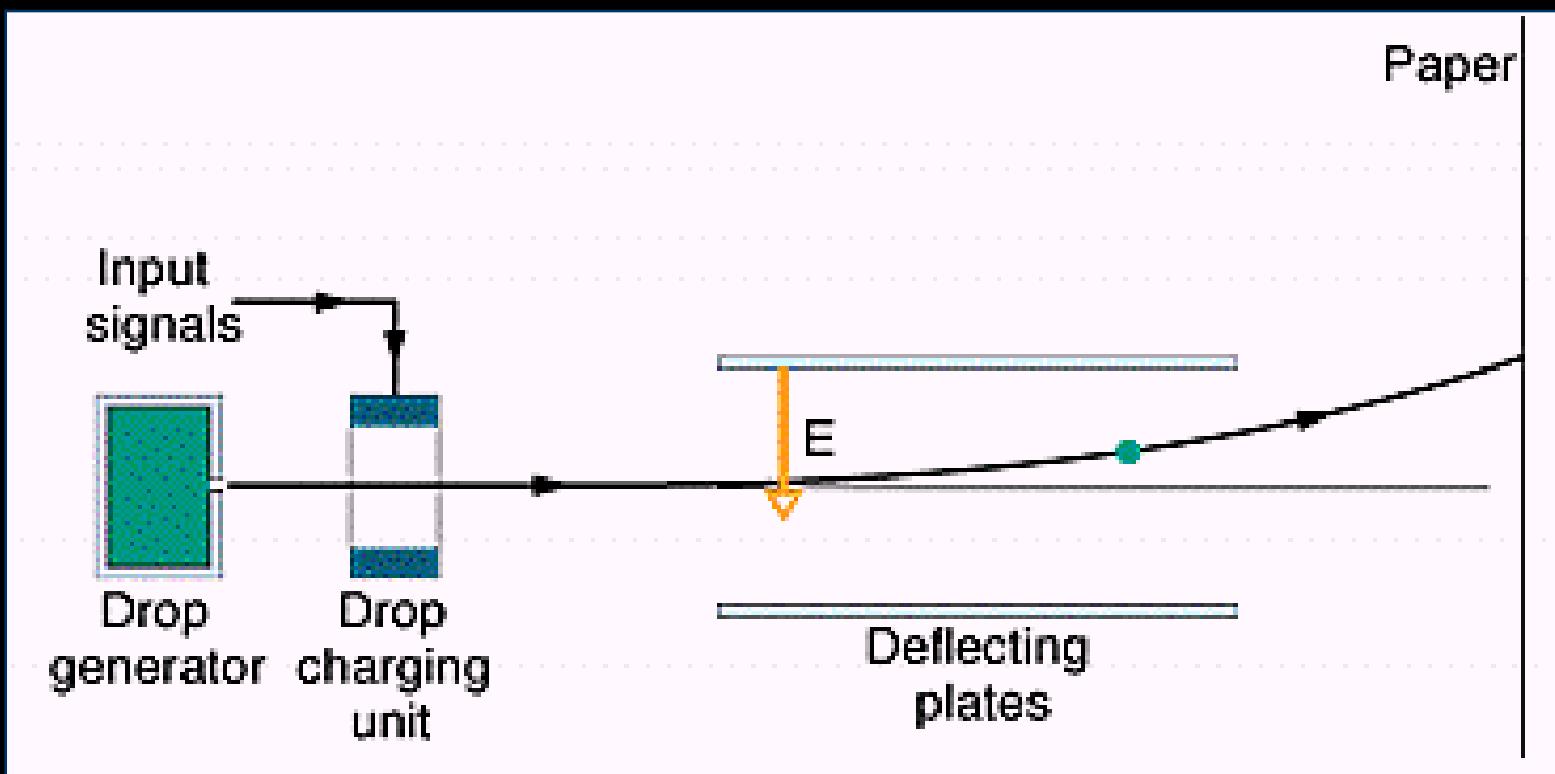
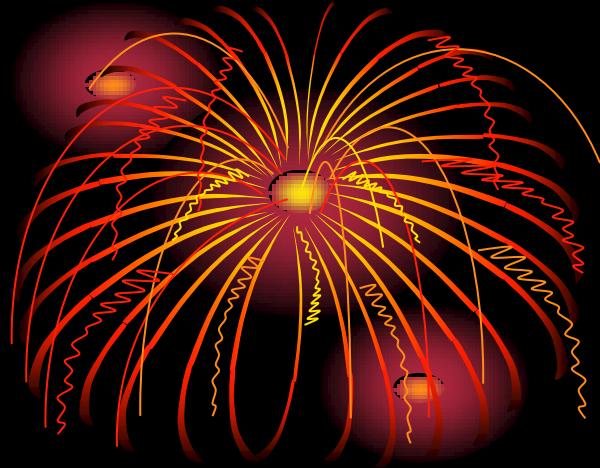
- $R = 4 \times 10^{-15} m$
- 如此大之斥力，必須有更強的核力與之抗衡，方能維持原子核的穩定。

# 1.3 靜電的應用

- Ink-Jet Printing
- Soil Decontamination
- Electroplating
- Electromagnetic Predators
- Electric Precipitator
- Xerography
- Laser Printer



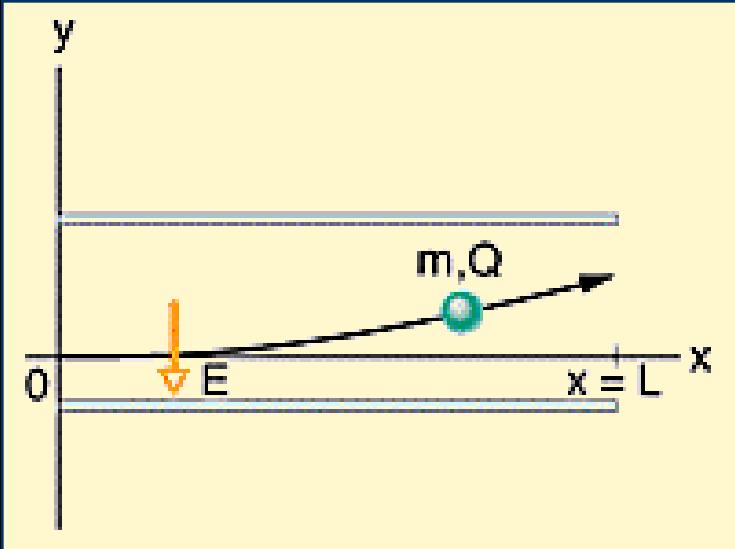
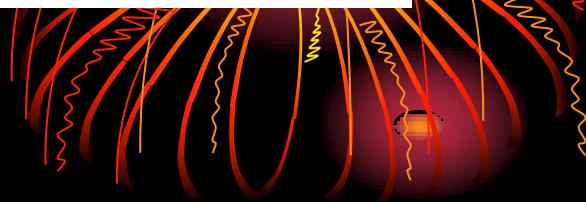
# Ink-Jet Printing



# An ink drop with

$$Q = 1.5 \times 10^{-13} C$$

$$m = 1.3 \times 10^{-10} kg$$



$$L = 1.6\text{cm}, v_x = 18\text{m/s}$$

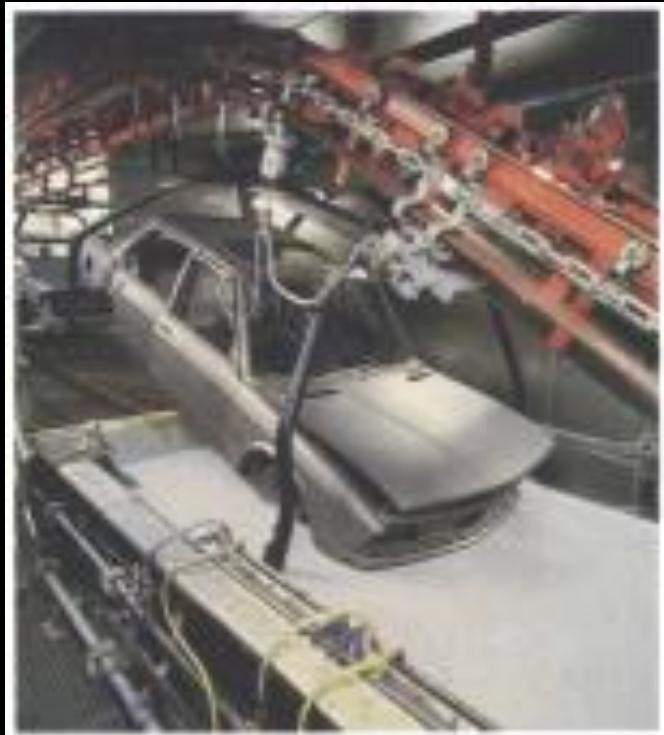
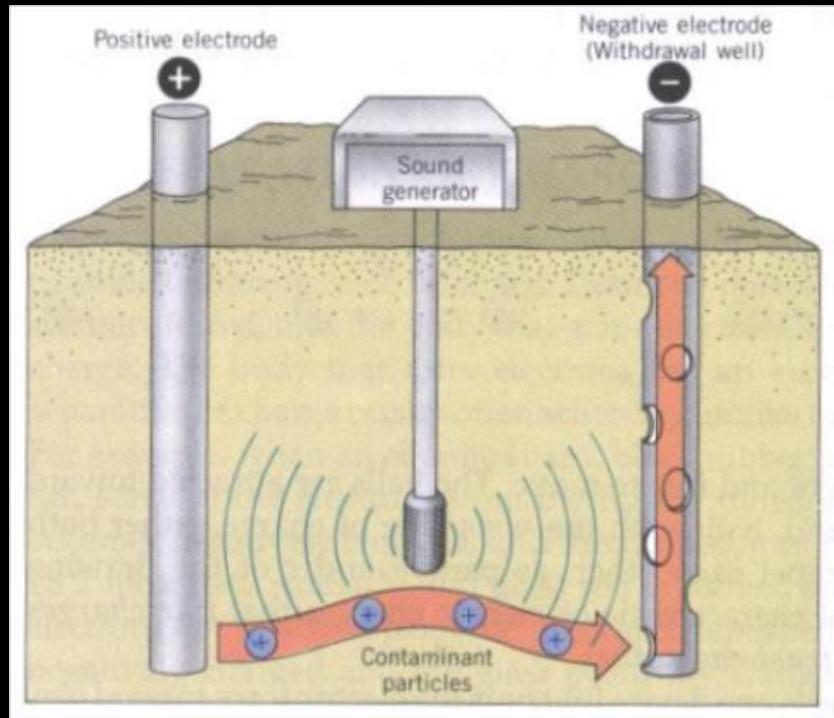
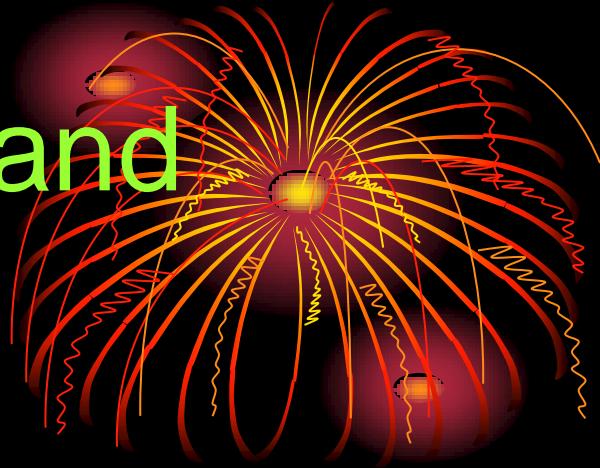
$$E = 1.4 \times 10^6 \text{N/C}$$

$$a_y = \frac{F}{m} = \frac{QE}{m}$$

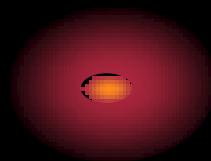
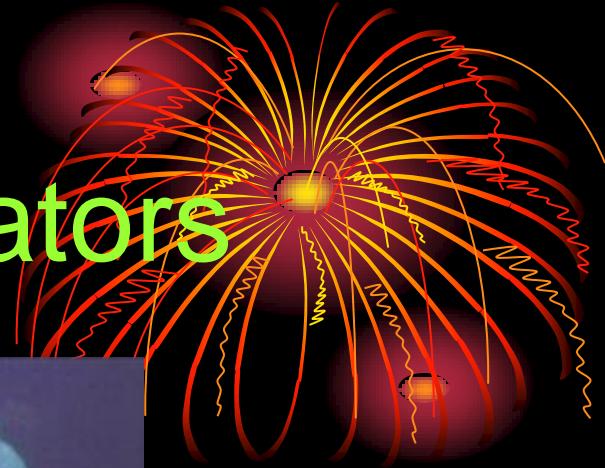
$$y = \frac{1}{2} a_y t^2, L = v_x t$$

$$y = \frac{QEL^2}{2mv_x^2} = 0.64\text{mm}$$

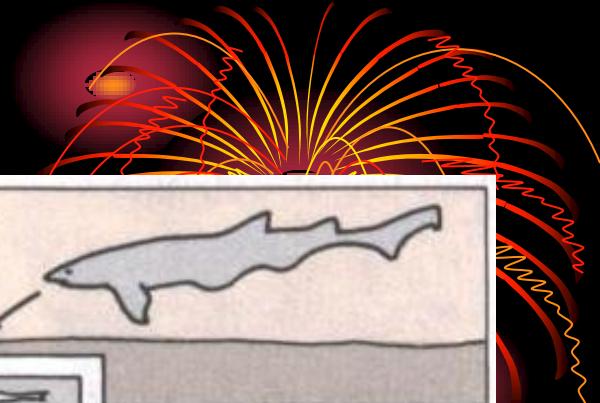
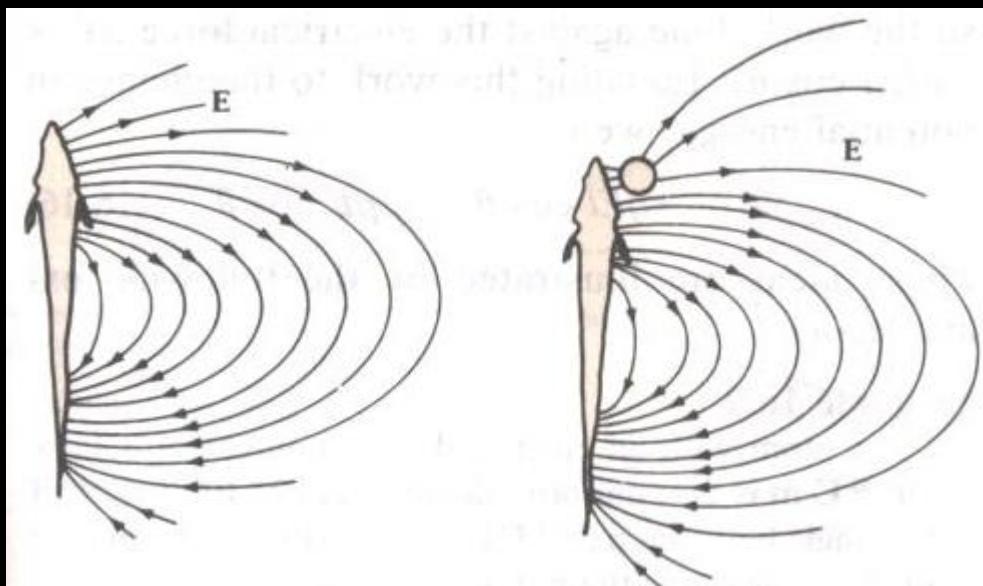
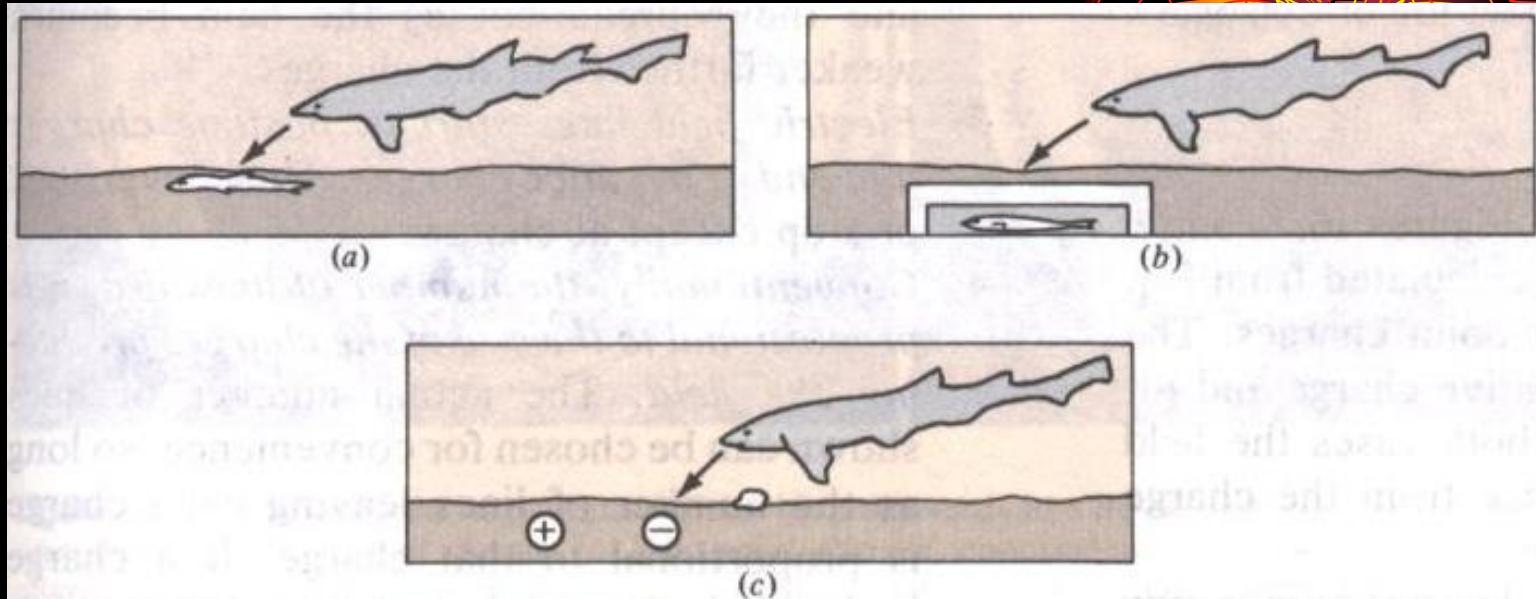
# Soil Decontamination and Electroplating



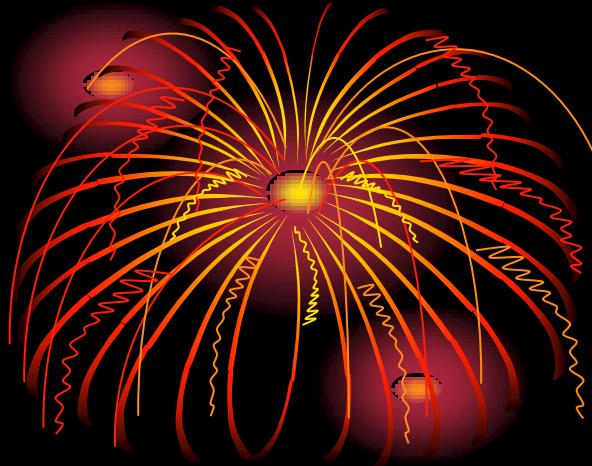
# Electromagnetic Predators



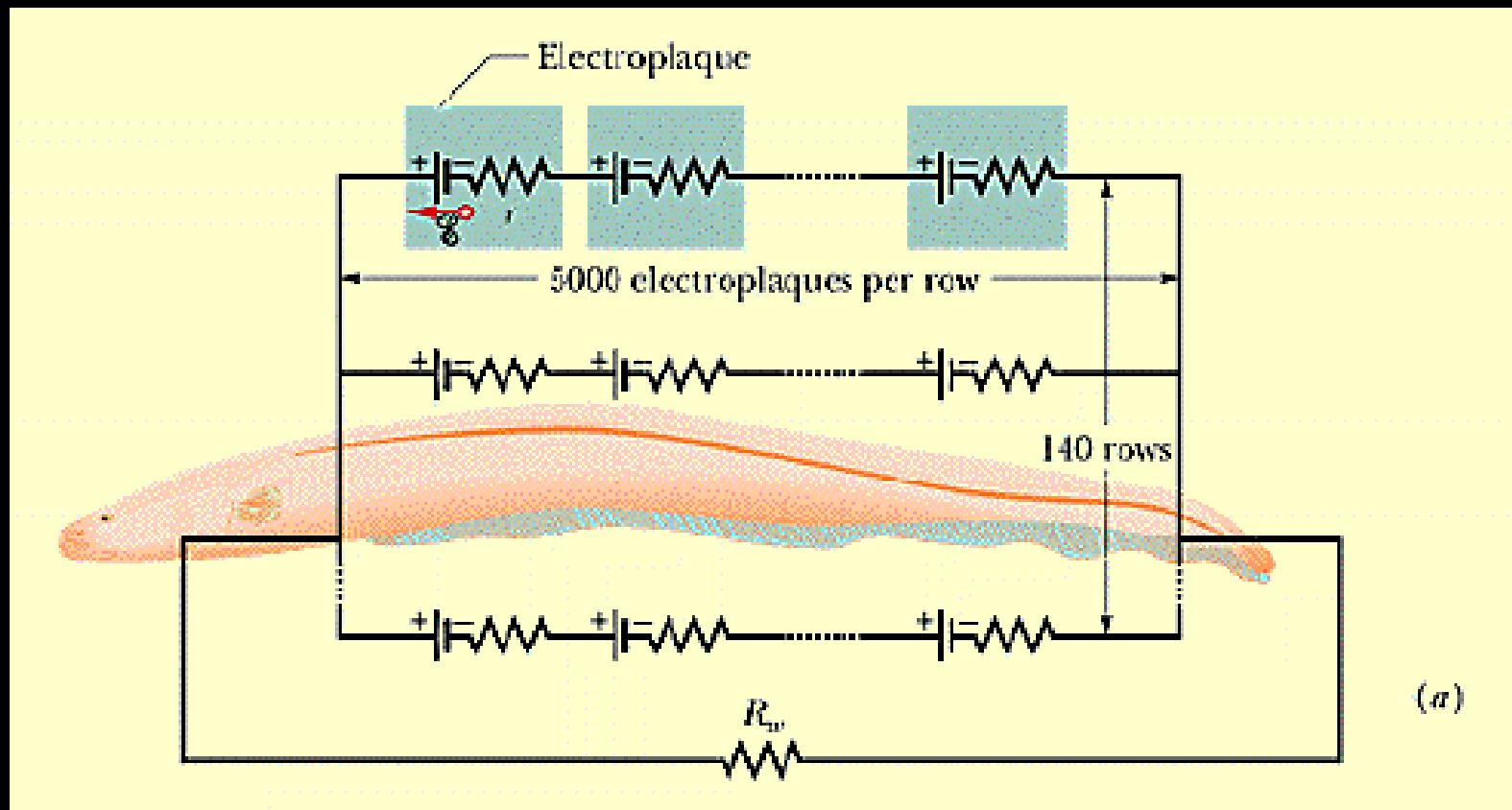
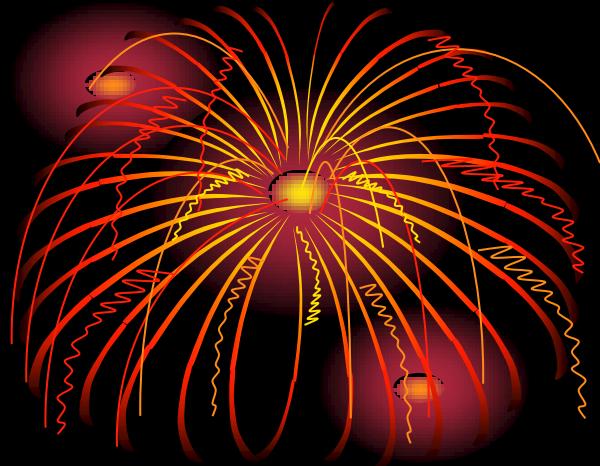
# 電 磁 掠 食 者



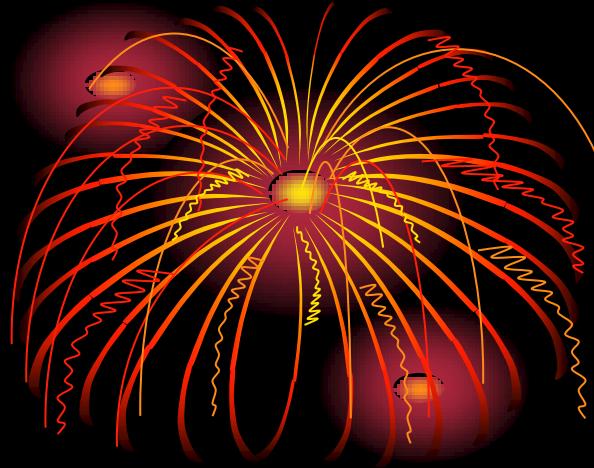
# The torpedo ray and electric eel



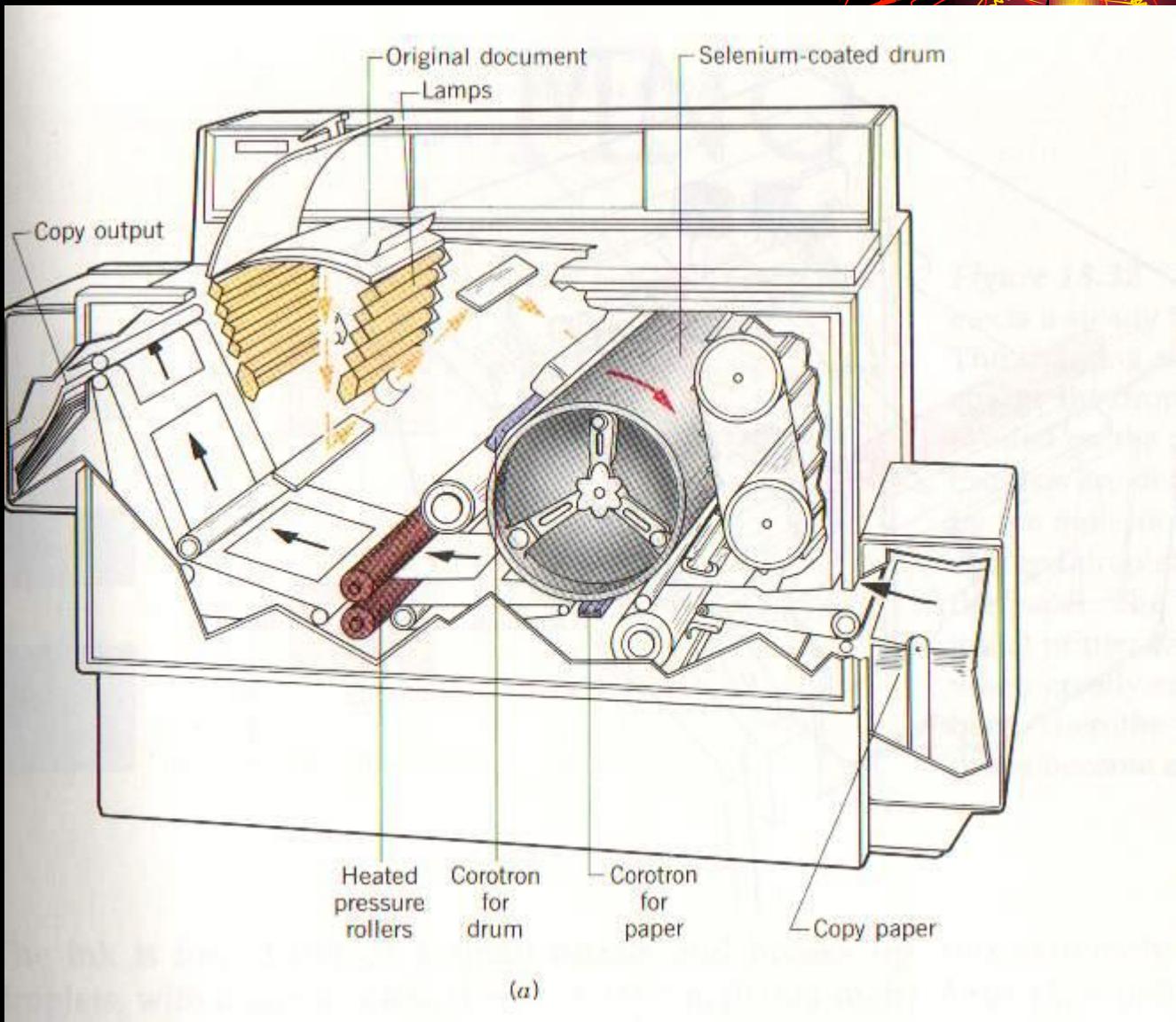
# Electroplaques



# Electric Precipitator

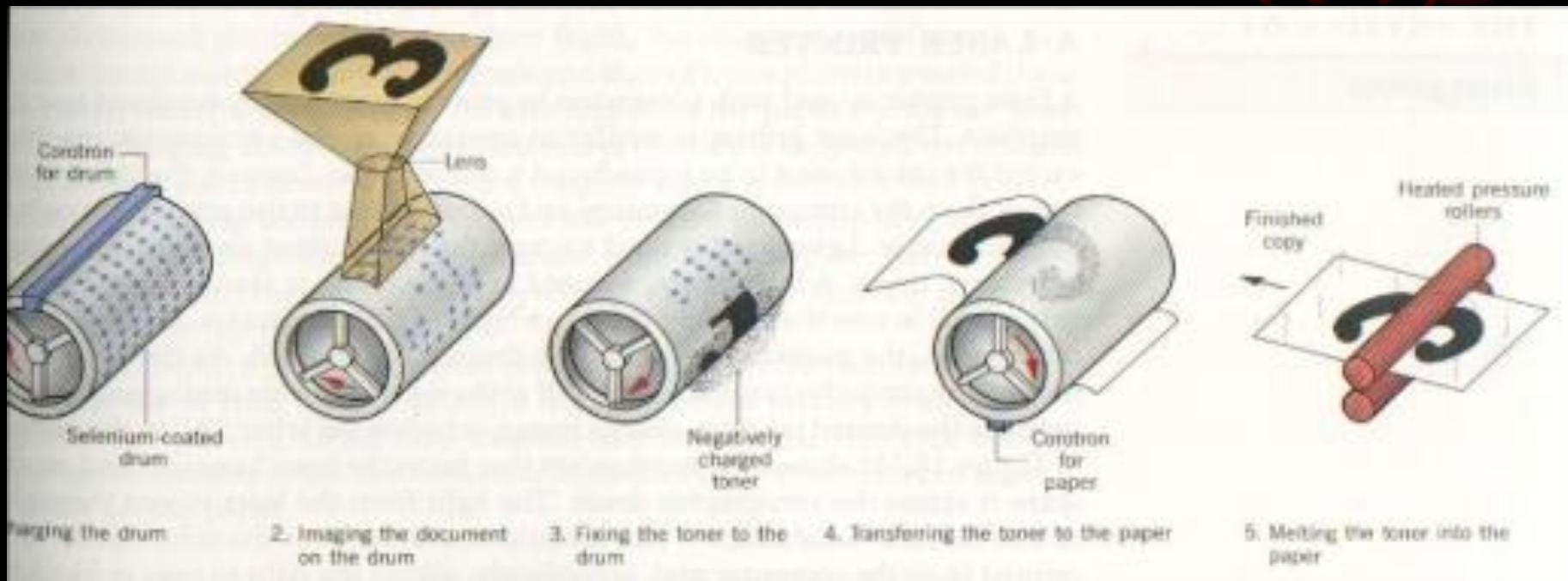
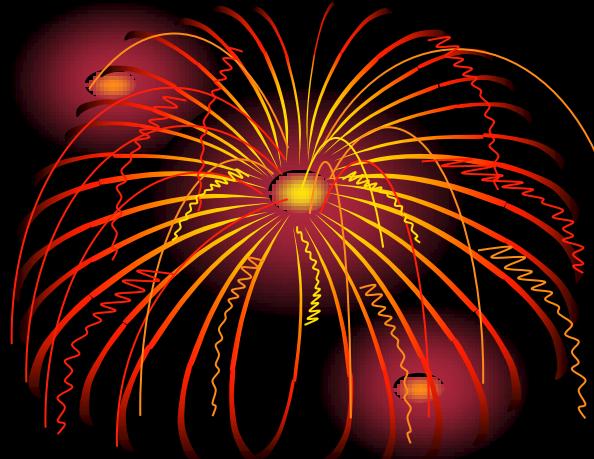


# 影印機

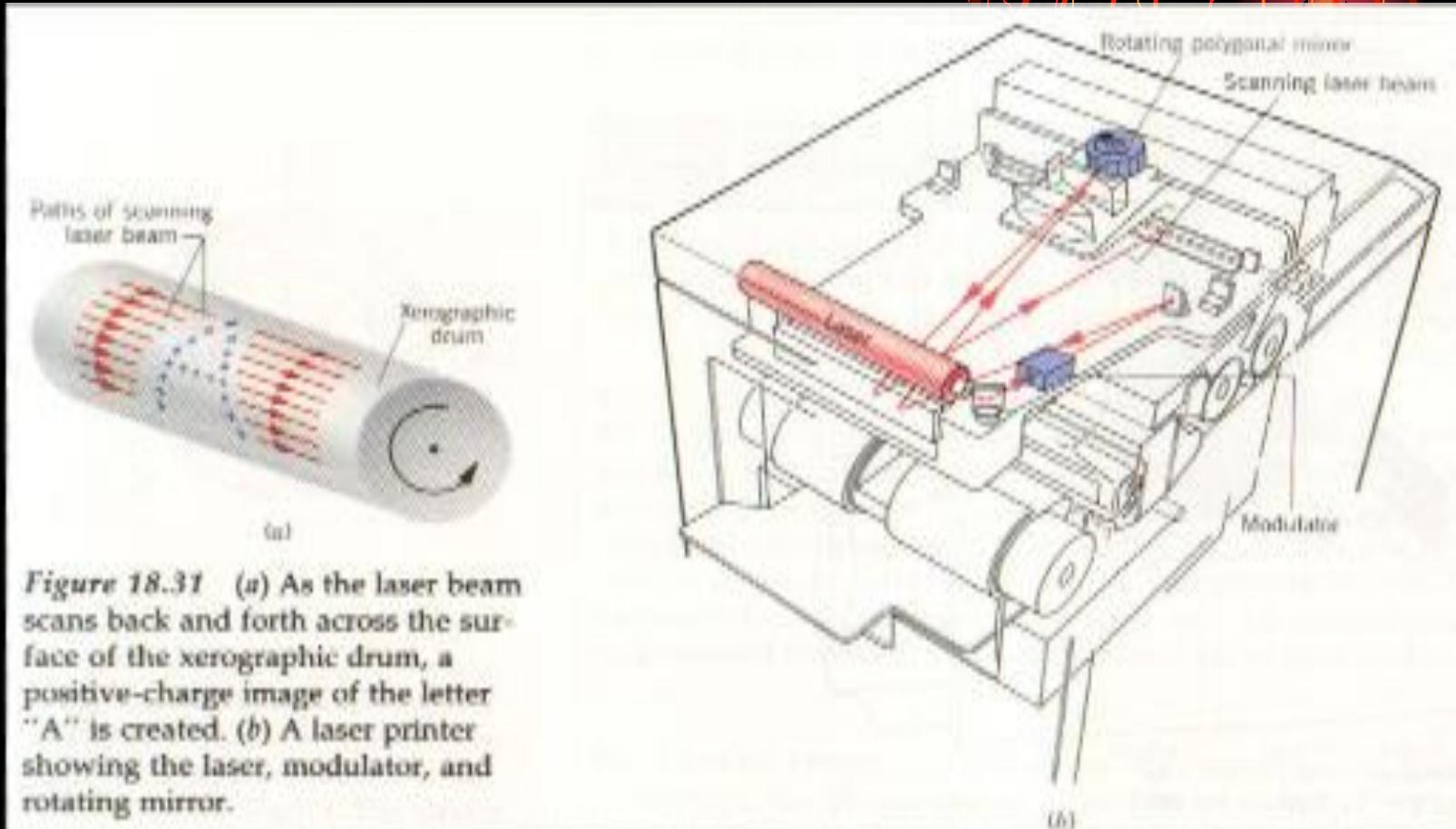
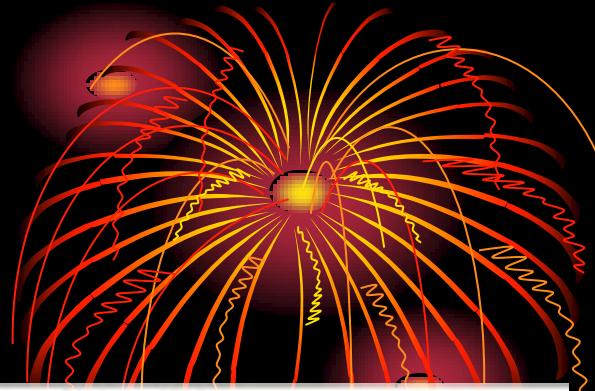


(a)

# The copying process



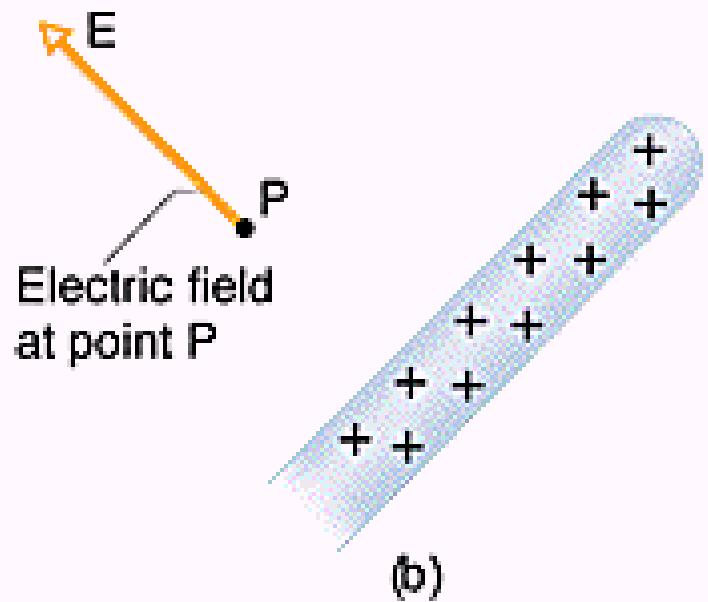
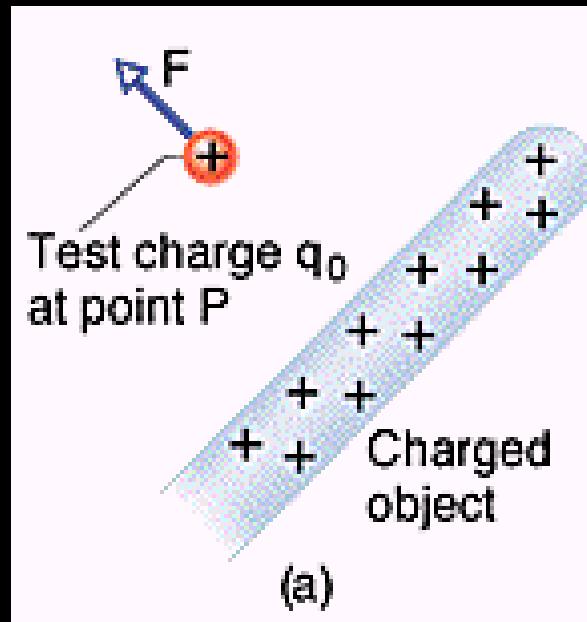
# Laser Printer



*Figure 18.31* (a) As the laser beam scans back and forth across the surface of the xerographic drum, a positive-charge image of the letter "A" is created. (b) A laser printer showing the laser, modulator, and rotating mirror.

## 2 電場

- ( electric field ) ( Lines of force )



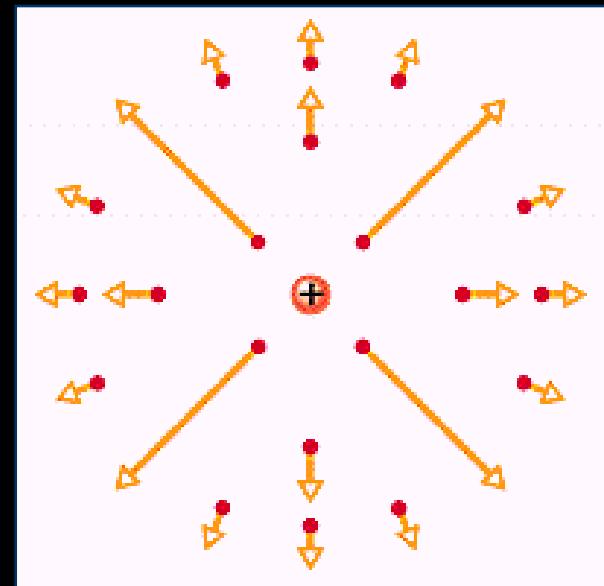
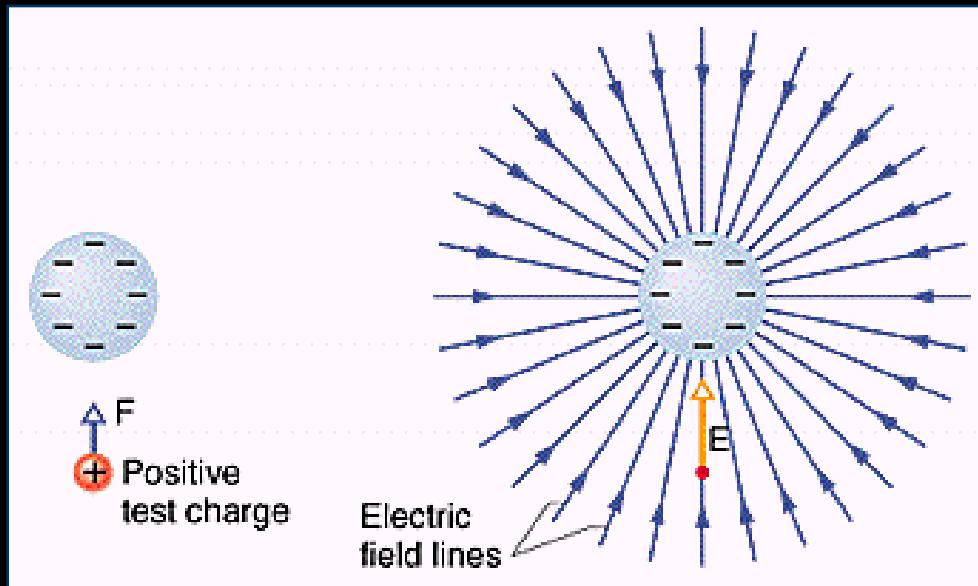
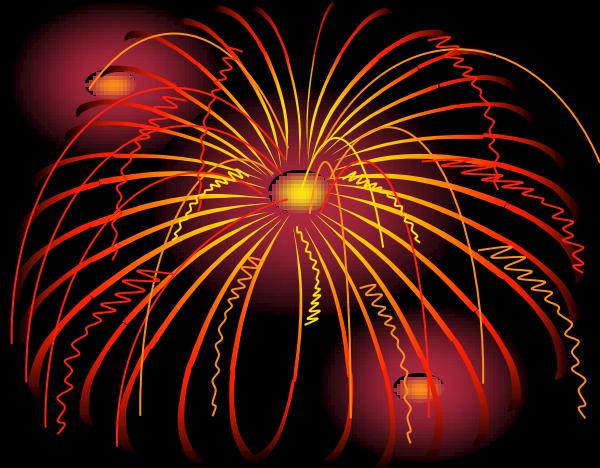
# 電場的定義



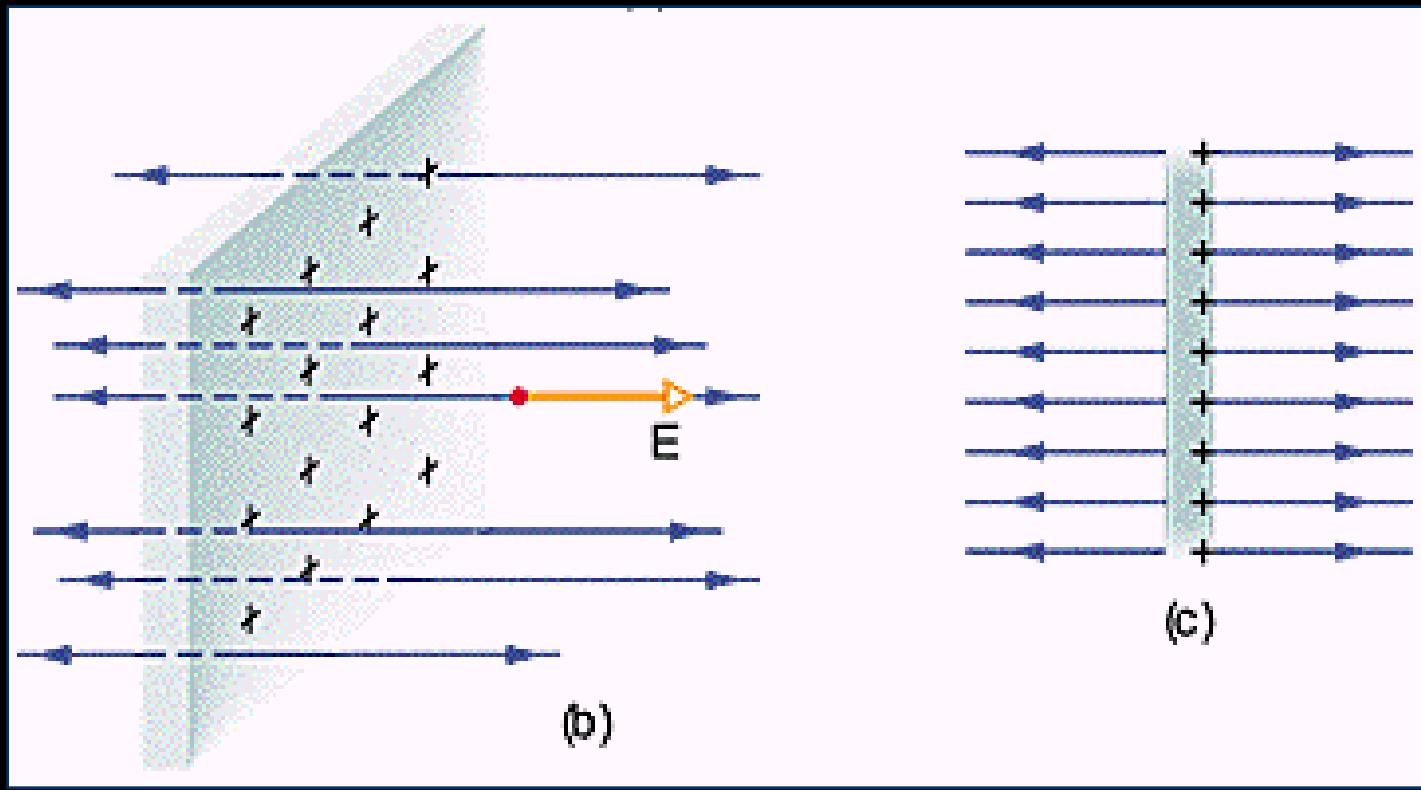
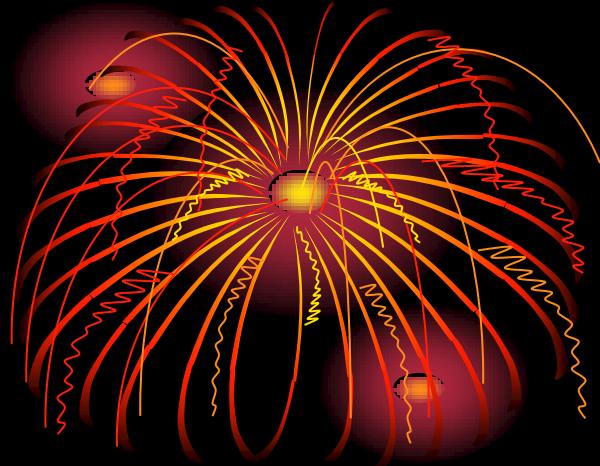
- 電力:  $q$  與  $q_0$  之間的電力 or  
 $q$  在  $q_0$  所建立的電場中受到的電力

$$\vec{E} = \frac{\vec{F}}{q_0} \text{ (N/C) (V} \cdot \text{m)}$$

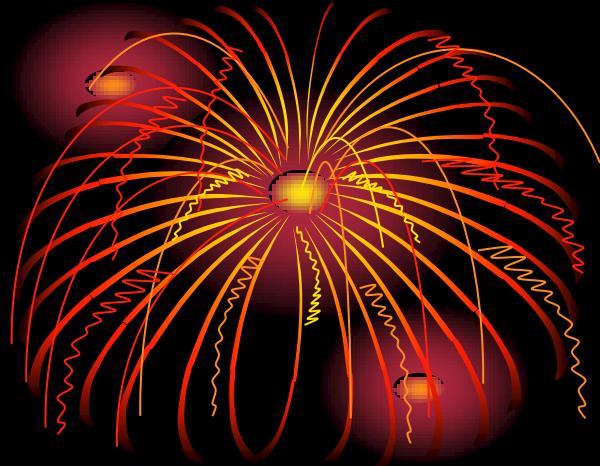
# 點電荷



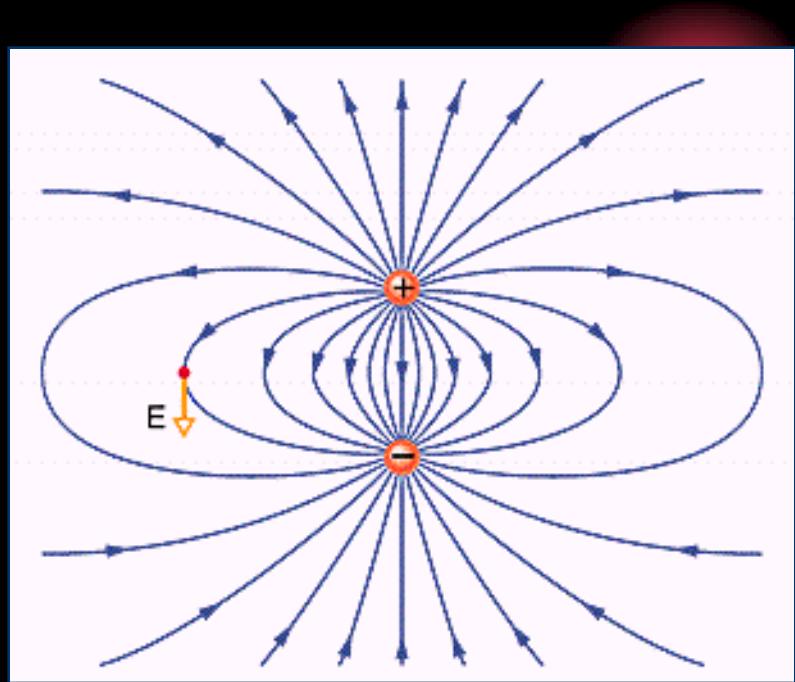
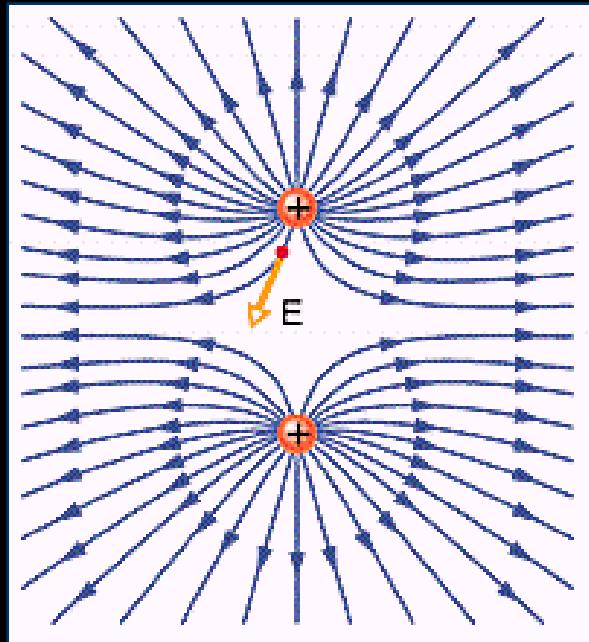
# 帶電平板



# 二正電荷與電雙極

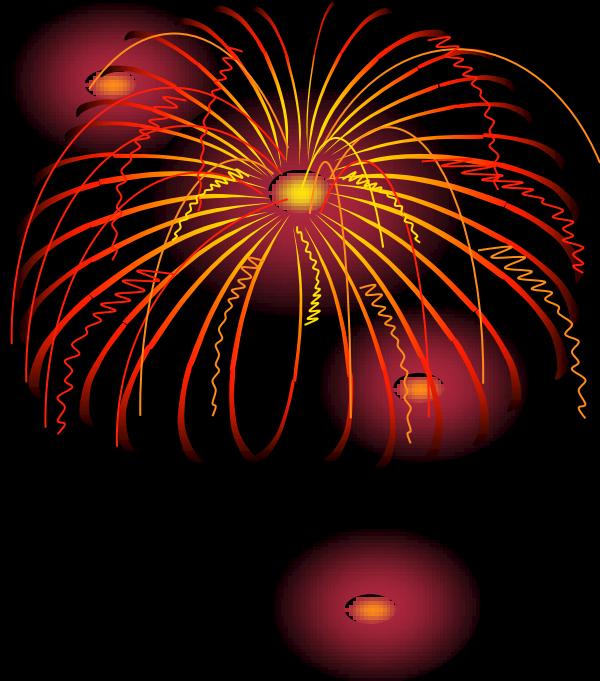


$q_0$

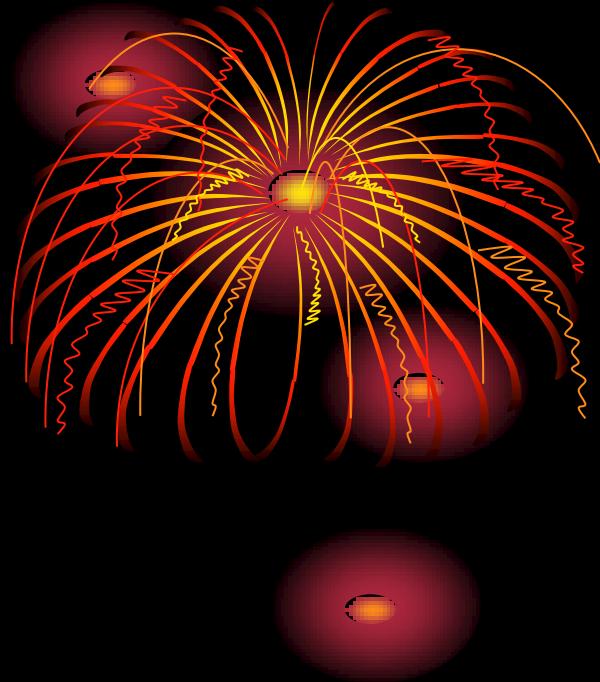
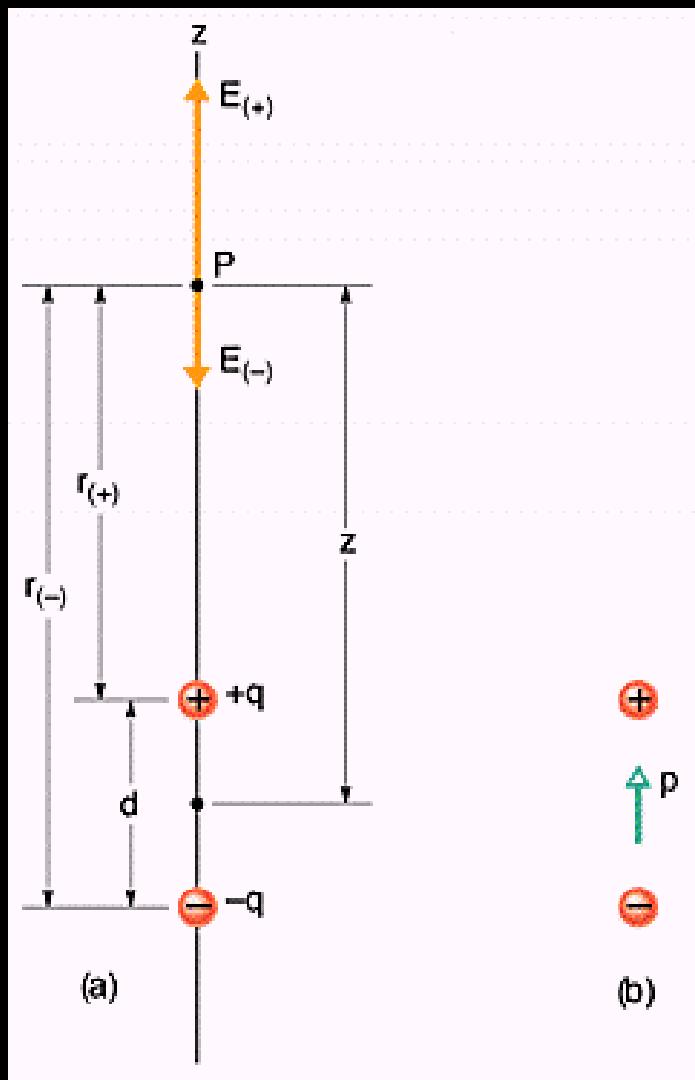


# 電場的計算

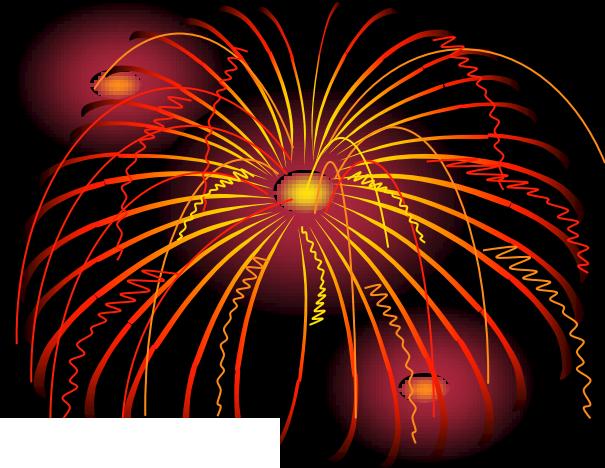
- 電雙極
- 均勻帶電圓環
- 均勻帶電圓盤



# 電雙極



# 兩電荷的電場相加



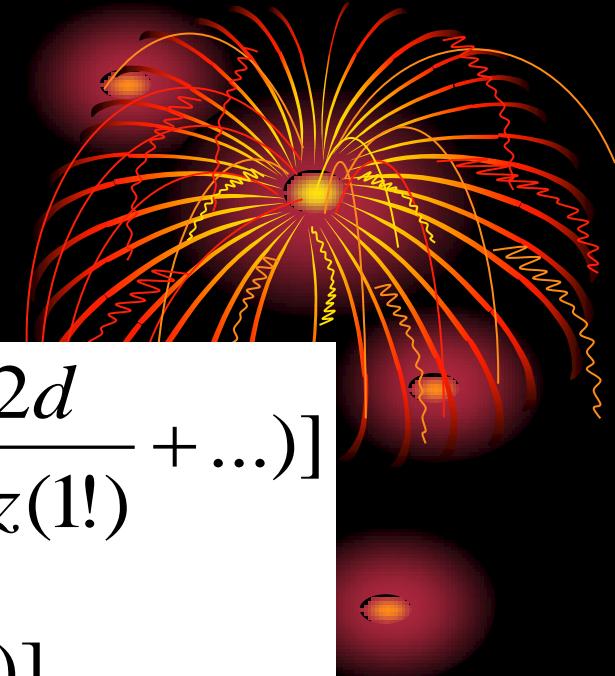
$$E = E_+ - E_-$$

$$= \frac{1}{4\pi\epsilon_0} \frac{q}{r_+^2} - \frac{1}{4\pi\epsilon_0} \frac{q}{r_-^2}$$

$$= \frac{1}{4\pi\epsilon_0} \frac{q}{(z - d/2)^2} - \frac{1}{4\pi\epsilon_0} \frac{q}{(z + d/2)^2}$$

$$= \frac{q}{4\pi\epsilon_0 z^2} \left[ \left(1 - \frac{d}{2z}\right)^{-2} - \left(1 + \frac{d}{2z}\right)^{-2} \right]$$

# 電雙極的電場



$$= \frac{q}{4\pi\epsilon_0 z^2} \left[ \left(1 + \frac{2d}{2z(1!)} + \dots\right) - \left(1 - \frac{2d}{2z(1!)} + \dots\right) \right]$$

$$= \frac{q}{4\pi\epsilon_0 z^2} \left[ \left(1 + \frac{d}{z} + \dots\right) - \left(1 - \frac{d}{z} + \dots\right) \right]$$

$$= \frac{q}{4\pi\epsilon_0 z^2} \frac{2d}{z} = \frac{1}{2\pi\epsilon_0} \frac{qd}{z^3}$$

$$E = \frac{1}{2\pi\epsilon_0} \frac{p}{z^3} \quad (\text{electric dipole})$$

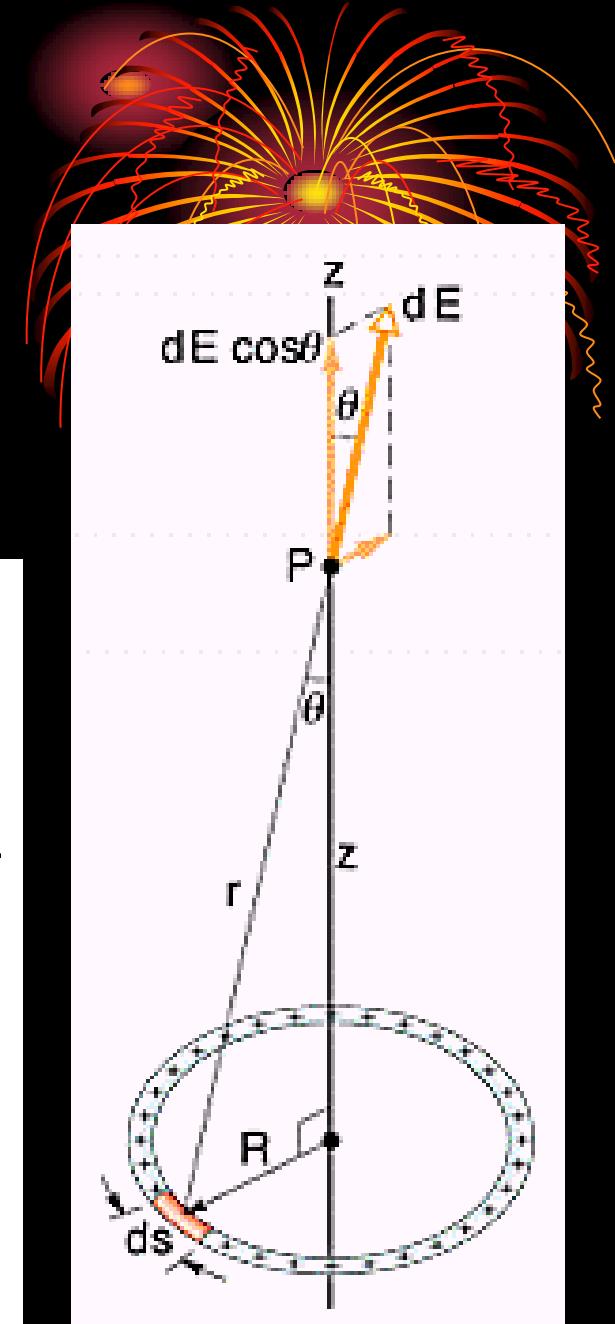
$\vec{p}$  = electric dipole moment (電雙極矩)

# 均勻帶電圓環

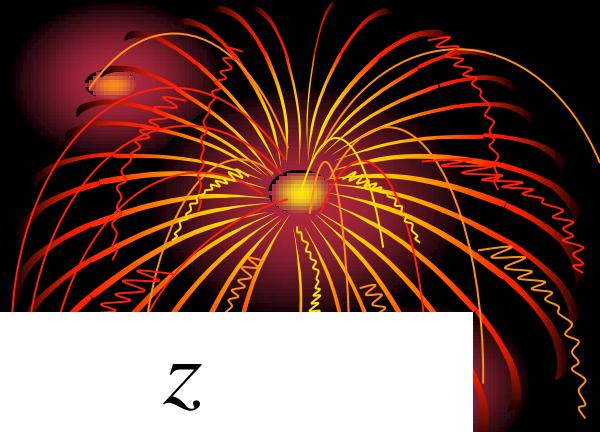
$$dq = \lambda ds$$

$$dE = \frac{1}{4\pi\epsilon_0} \frac{dq}{r^2} = \frac{1}{4\pi\epsilon_0} \frac{\lambda ds}{r^2}$$

$$dE = \frac{1}{4\pi\epsilon_0} \frac{\lambda ds}{(z^2 + R^2)}$$



# 均勻帶電圓環的電場



$$dE \rightarrow dE \cos \theta, \cos \theta = \frac{z}{r} = \frac{z}{(z^2 + R^2)^{1/2}}$$

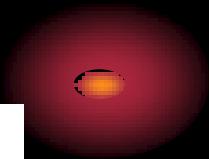
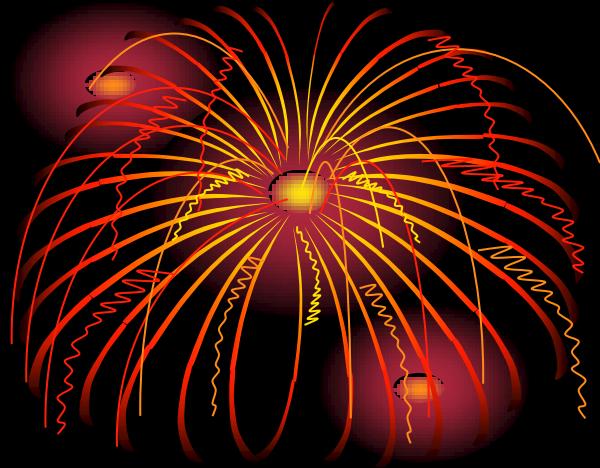
$$dE \cos \theta = \frac{z\lambda}{4\pi\epsilon_0(z^2 + R^2)^{3/2}} ds$$

$$E = \int dE \cos \theta = \frac{z\lambda}{4\pi\epsilon_0(z^2 + R^2)^{3/2}} \int_0^{2\pi R} ds$$

$$= \frac{z\lambda(2\pi R)}{4\pi\epsilon_0(z^2 + R^2)^{3/2}} = \frac{qz}{4\pi\epsilon_0(z^2 + R^2)^{3/2}}$$

# 極限情形

- If  $z \gg R$ ,  $z^2 + R^2 \rightarrow z^2$



$$E = \frac{qz}{4\pi\epsilon_0(z^2 + R^2)^{3/2}}$$

$$\rightarrow \frac{1}{4\pi\epsilon_0} \frac{q}{z^2} \text{ (like a point charge)}$$

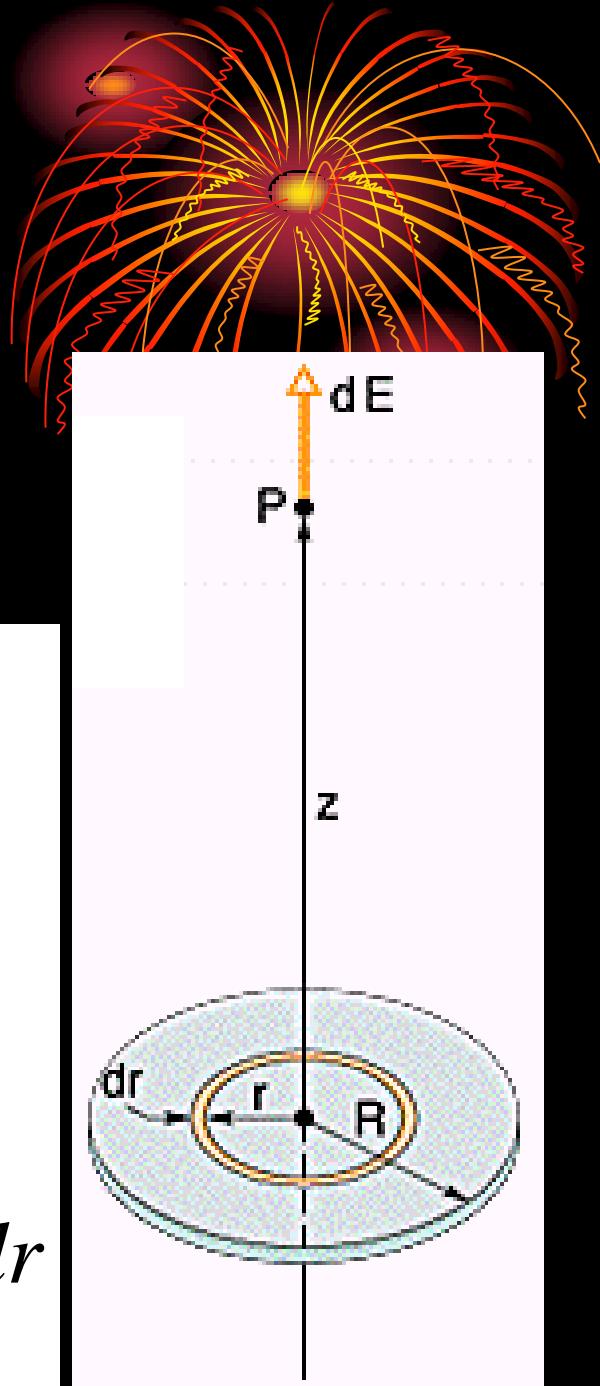
# 均勻帶電圓盤

$$dq = \sigma dA = \sigma 2\pi r dr$$

$$dE = \frac{z\sigma 2\pi r dr}{4\pi\epsilon_0(z^2 + r^2)^{3/2}}$$

$$dE = \frac{\sigma z}{4\epsilon_0} \frac{2r dr}{(z^2 + r^2)^{3/2}}$$

$$E = \int dE = \frac{\sigma z}{4\epsilon_0} \int_0^R (z^2 + r^2)^{-3/2} (2r) dr$$



# 均勻帶電圓盤的電場



$$E = \int dE = \frac{\sigma z}{4\epsilon_0} \int_0^R (z^2 + r^2)^{-3/2} (2r) dr$$

$$= \frac{\sigma z}{4\epsilon_0} \left[ \frac{(z^2 + r^2)^{-1/2}}{-1/2} \right]_0^R$$

$$= \frac{\sigma}{2\epsilon_0} \left( 1 - \frac{z}{\sqrt{z^2 + R^2}} \right) \rightarrow \frac{\sigma}{2\epsilon_0}$$

# The electric field on an oil drop

A drop of  $R = 2.76\mu\text{m}$  has 3 excess electrons,  $\rho = 920\text{kg/m}^3$



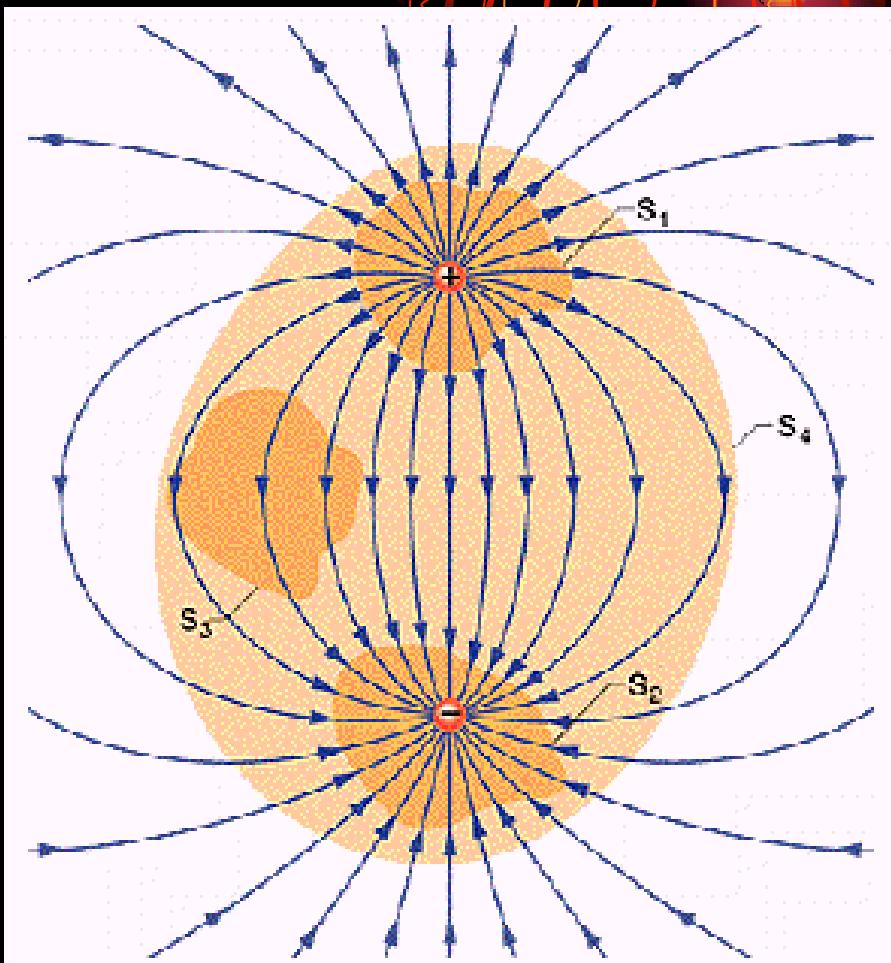
$$F_g = \frac{4}{3}\pi R^3 \rho g = (3e)E = F_e$$

$$E = \frac{4\pi R^3 \rho g}{9e} = 1.65 \times 10^6 \text{ N/C}$$

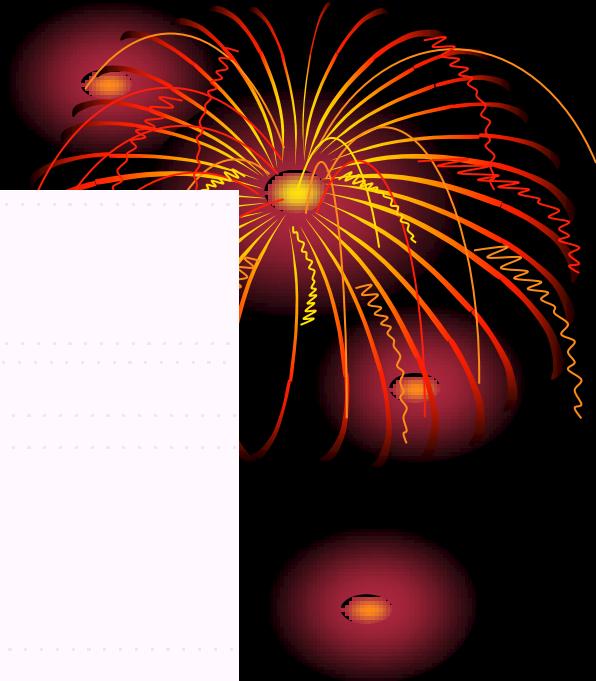
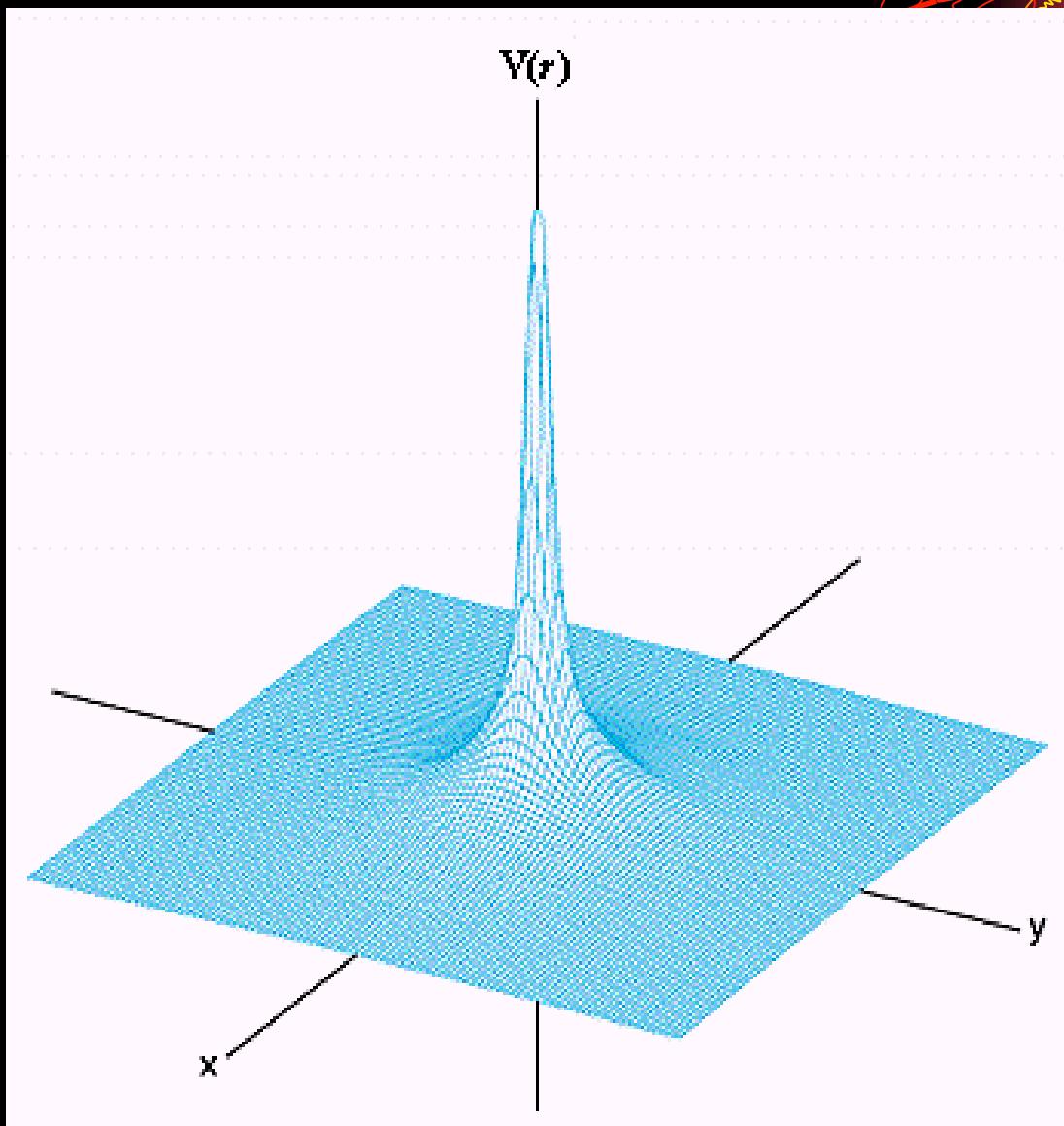
### 3 高斯定律 Gauss' Law

- Flux  $\leftrightarrow$  enclosed charge

$$\begin{aligned}\varepsilon_0 \Phi \\ = \varepsilon_0 \oint \vec{E} \cdot d\vec{A} \\ = q_{enc}\end{aligned}$$

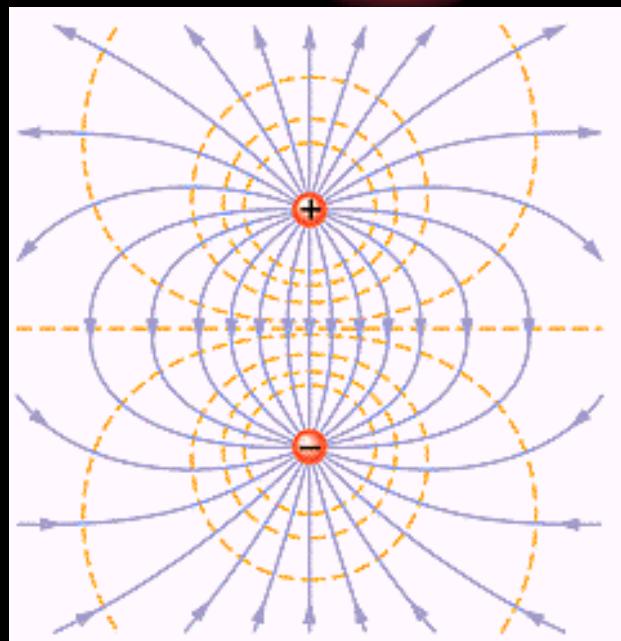
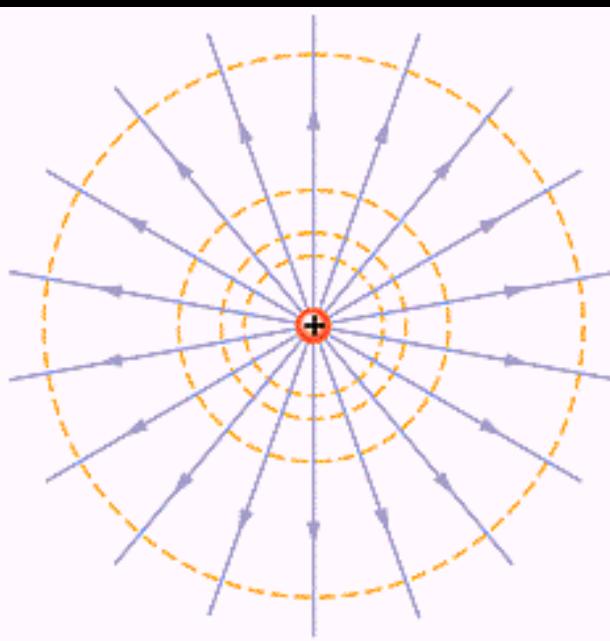
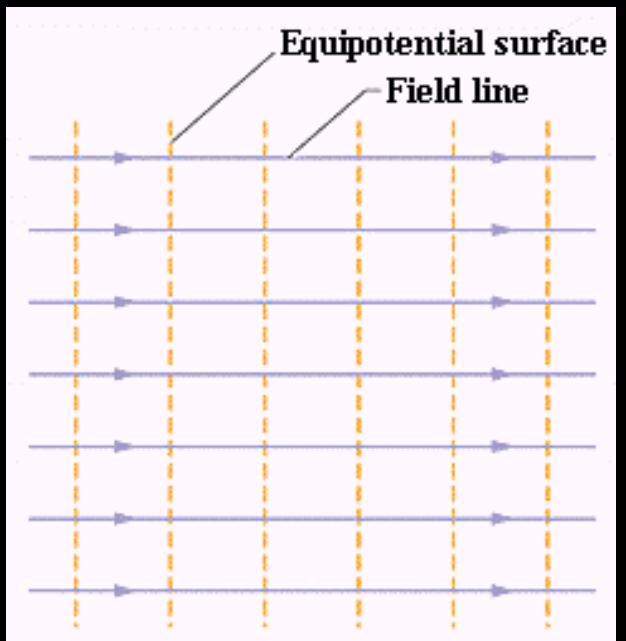


# 4點電荷的電位圖

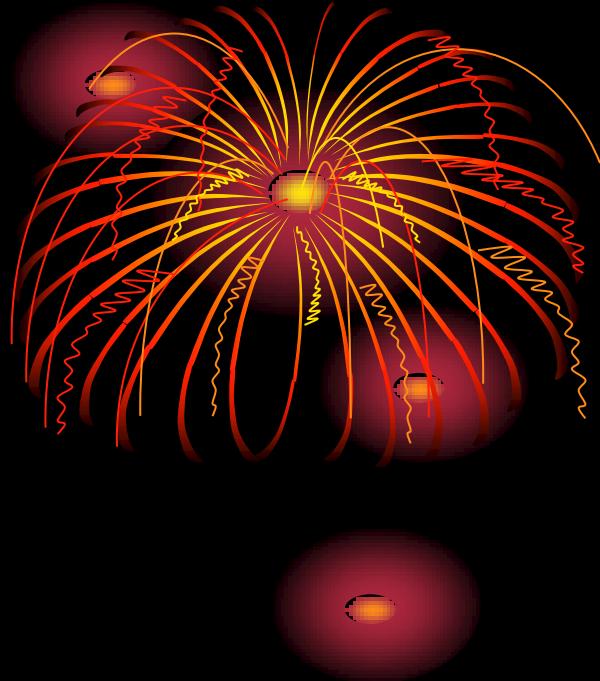


# 等位面3例

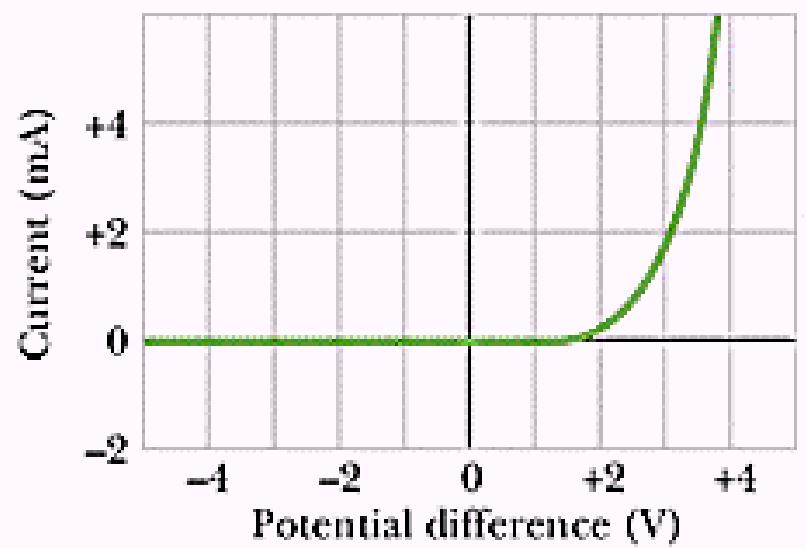
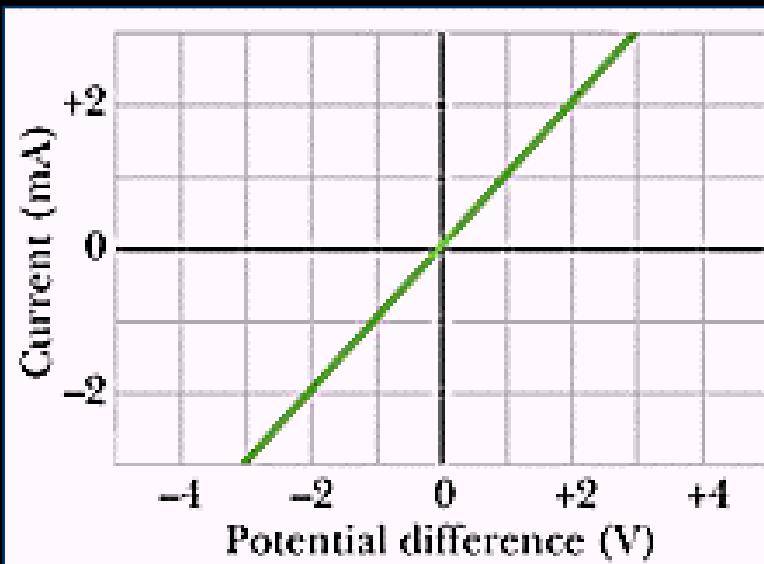
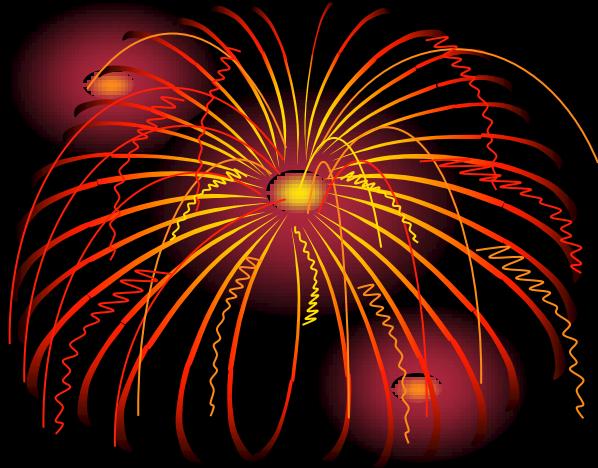
- E.S. for a uniform field, a point charge, and an electric dipole



# 電容器



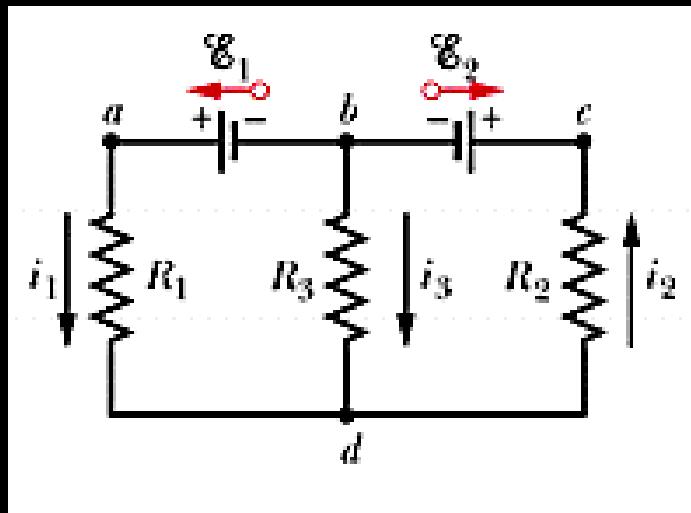
# 6 I-V curves



conductor

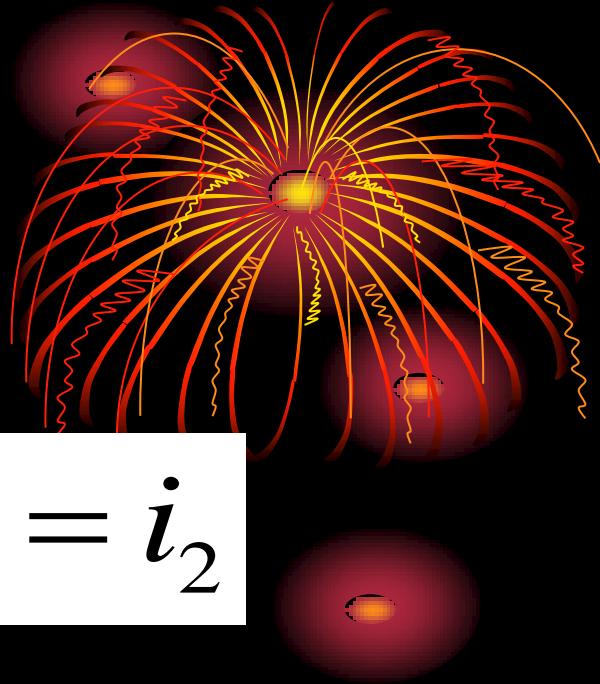
semiconductor

# 7 Multiloop Circuits



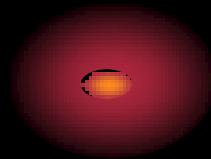
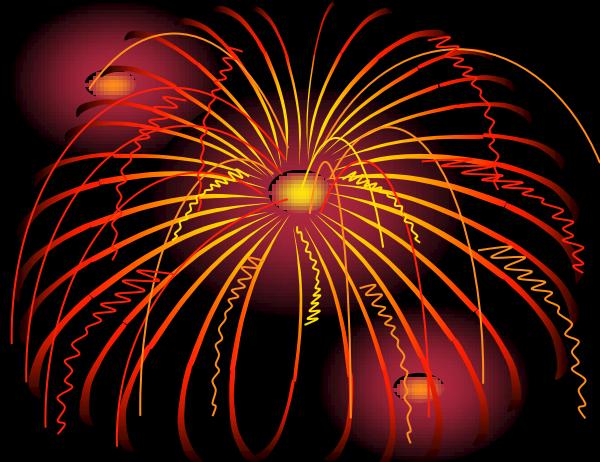
$$i_1 + i_3 = i_2$$

- The Junction rule: 流入接點之電流必等於流出者  
(Kirchhoff's junction/current rule)

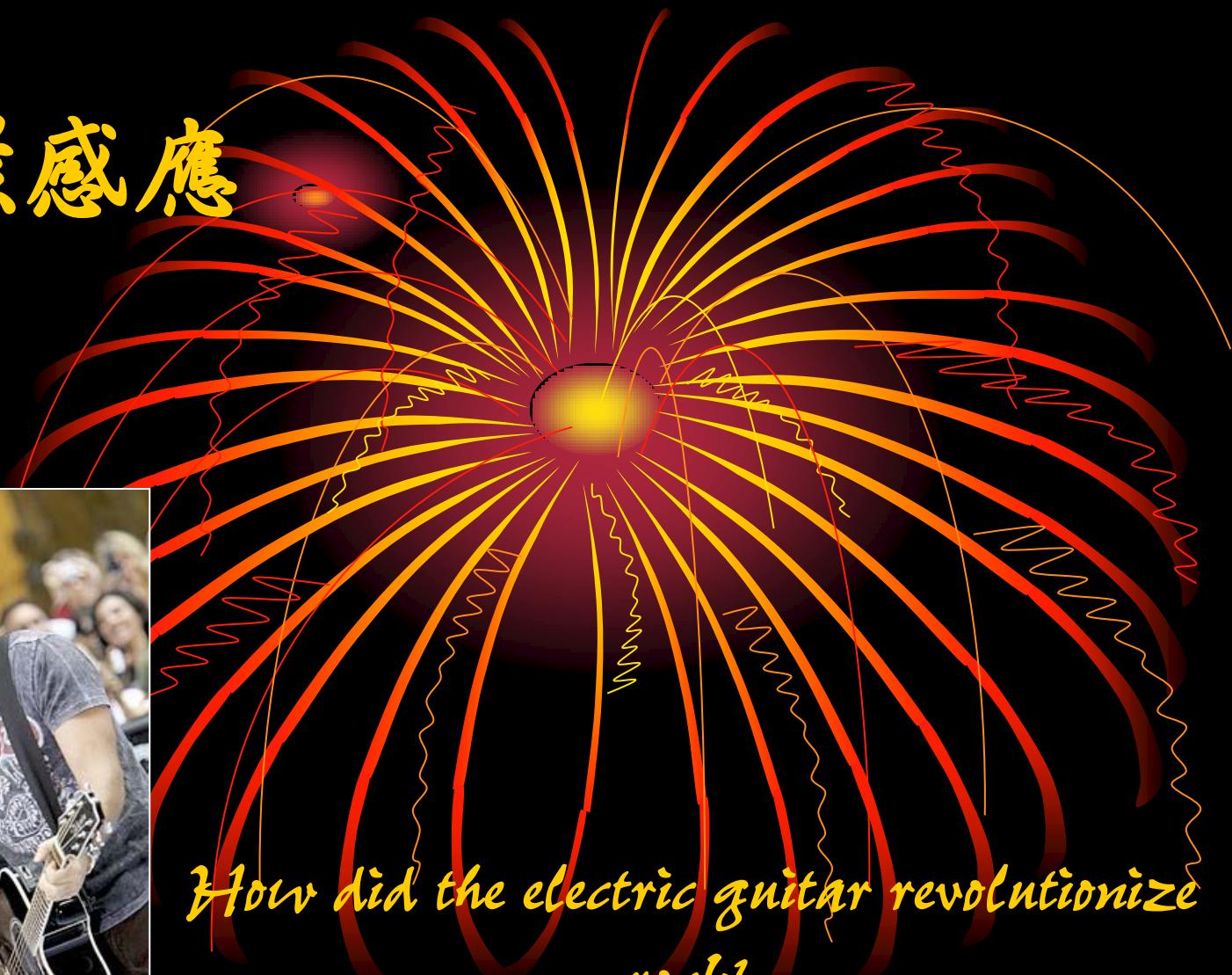


# 8 電流與磁場

- ❖ The electric field and the magnetic field
- ❖ Electromagnets and permanent magnets



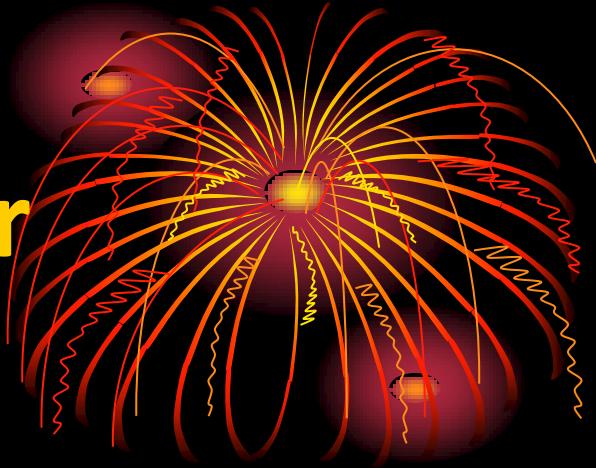
# 9 電磁感應



*How did the electric guitar revolutionize  
rock?*

*From acoustic to electric guitars*

# 10 Magnetism of Matter



**How can a clay-walled kiln reveal Earth's magnetic field of the past?**

# 11 反射、折射、干涉、繞射



# 12 量子物理

