

$0 \leq \theta < 2\pi$
 $0 < \rho < \infty$

$$x = \rho \cos \theta \quad x + iy$$

$$y = \rho \sin \theta$$

$$e^{i\theta} = \cos \theta + i \sin \theta$$

$$\frac{d e^{i\theta}}{d\theta} = \frac{d(\cos \theta + i \sin \theta)}{d\theta} = \frac{d \cos \theta}{d\theta} + i \frac{d \sin \theta}{d\theta}$$

$$= -\sin \theta + i \cos \theta$$

$$= i(\cos \theta + i \sin \theta) = i e^{i\theta}$$

$$\frac{d e^{ax}}{dx} = a e^{ax}$$

$$\frac{d^2 e^{ax}}{dx^2} = a^2 e^{ax}$$

$$\frac{d \cos a\theta}{d\theta} = -a \sin a\theta$$

$$\frac{d \sin a\theta}{d\theta} = a \cos a\theta$$

$$\frac{d^2 \sin a\theta}{d\theta^2} = -a^2 \sin a\theta$$

$$ma = F = -kx$$



$$ma + kx = 0$$

$$\begin{aligned} t=0, x &= A \\ \dot{x} &= 0 \end{aligned}$$

$$m \frac{d^2 x(t)}{dt^2} + kx(t) = 0$$

$$x(t) = A \cos \omega t$$

$$m(-\omega^2) A \cos \omega t + k A \cos \omega t = 0$$
$$[m(-\omega^2) + k] A \cos \omega t = 0$$

$$x(t) = A \cos \left(\sqrt{\frac{k}{m}} t \right) \quad T = \frac{2\pi}{\sqrt{k/m}}$$



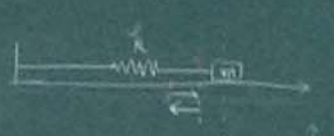
$$x(t) = A \cos\left(\sqrt{\frac{k}{m}} t\right) \quad T = \frac{2\pi}{\sqrt{\frac{k}{m}}} = 2\pi \sqrt{\frac{m}{k}} \quad \text{週期}$$

$$v(t) = \frac{dx(t)}{dt} = \frac{d(A \cos(\sqrt{\frac{k}{m}} t))}{dt} = -A \sqrt{\frac{k}{m}} \sin\left(\sqrt{\frac{k}{m}} t\right)$$



$$\vec{\tau} = \vec{r} \times \vec{F}$$

$$lmg \sin\theta$$



$$\frac{d^2x}{dt^2} + \frac{k}{m} x = 0$$

$$x(t) = A \cos \omega t$$

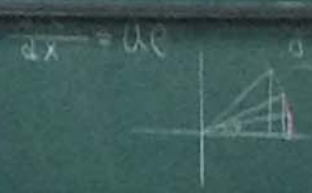
$$m(-\omega^2) A \cos \omega t + k A \cos \omega t = 0$$

$$[-m\omega^2 + k] A \cos \omega t = 0$$

$$\int_0^x kx' dx = \frac{1}{2} mv^2 = 0$$

$$ml \frac{d^2\theta}{dt^2} + \frac{g}{l} \theta = 0$$

$$\sin\theta \approx \theta$$

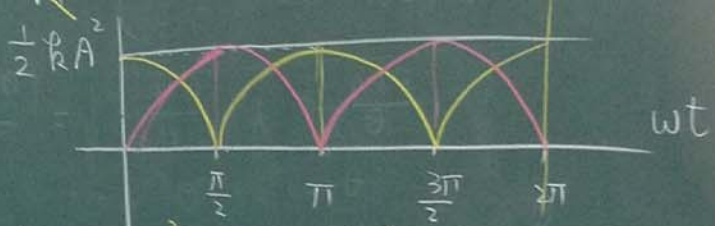


$$I \frac{d^2\theta}{dt^2} + mg l \sin\theta = 0$$

\downarrow ml^2 \downarrow g
 $\frac{d^2\theta}{dt^2} + \frac{g}{l} \sin\theta = 0$

$$\int_0^x kx' dx' = \frac{1}{2} k x(t)^2 = \frac{1}{2} k A^2 \cos^2\left(\sqrt{\frac{k}{m}} t\right)$$

$$\frac{1}{2} m v^2 = \frac{1}{2} \cancel{m} A^2 \frac{k}{m} \sin^2\left(\sqrt{\frac{k}{m}} t\right) \quad \omega$$



$\theta = 0$

$$\sin\theta = \cancel{\frac{1}{6}\theta^3} + \cos\theta \theta + \frac{1}{2}(-\sin\theta)\theta^2 + \frac{1}{3!}(-\cos\theta)\theta^3 + \dots$$

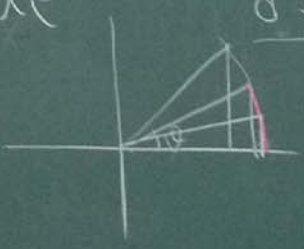
$$\frac{d e^{ax}}{dx} = a e^{ax}$$

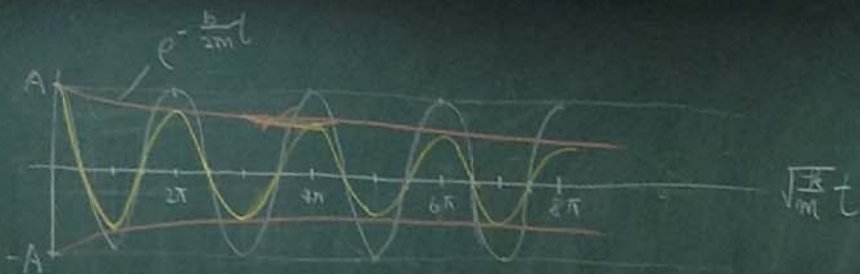
$$\frac{d^2 e^{ax}}{dx^2} = a^2 e^{ax}$$

$$\frac{d \cos a\theta}{d\theta} = -a \sin a\theta$$

$$\frac{d \sin a\theta}{d\theta} = a \cos a\theta$$

$$\frac{d^2 \sin a\theta}{d\theta^2} = -a^2 \sin a\theta$$





$$x = e^{-\frac{b}{2m} t} \left(C_1 \cos \omega t + C_2 \sin \omega t \right)$$

$$\alpha = \frac{-b \pm \sqrt{b^2 - 4m k}}{2m}$$

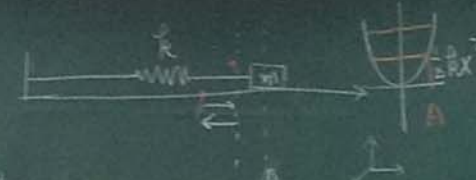
$$e^{i\theta} = \cos \theta + i \sin \theta$$

$$e^{-i\theta} = \cos \theta - i \sin \theta$$



$$\vec{\tau} = \vec{r} \times \vec{F}$$

$$lmg \sin \theta$$



$$m \frac{d^2 x}{dt^2} + kx = 0$$

$$x(t) = A \cos \omega t$$

$$m(-\omega^2) A \cos \omega t + k A \cos \omega t = 0$$

$$[m\omega^2 - k] A \cos \omega t = 0$$

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$$v(t) = \frac{dx(t)}{dt} = \frac{d(A \cos(\sqrt{\frac{k}{m}} t))}{dt} = -A \sqrt{\frac{k}{m}} \sin \left(\sqrt{\frac{k}{m}} t \right)$$