



$\vec{a} + \vec{b} = \vec{b} + \vec{a}$ 交换律
 $(\vec{a} + \vec{b}) + \vec{c} = \vec{a} + (\vec{b} + \vec{c})$ 结合律
 $\vec{A} = \alpha \vec{a}$
 $\vec{a} - \vec{b} = \vec{a} + (-1)\vec{b}$
 $\alpha \beta \vec{a} = \beta \alpha \vec{a} = \vec{a} + (-\vec{b})$

$\arcsin(\sin \theta) = \theta, -\pi/2 \leq \theta \leq \pi/2$
 $\arccos(\cos \theta) = \theta, 0 \leq \theta \leq \pi$
 $\arctan(\tan \theta) = \theta, -\pi/2 < \theta < \pi/2$

向量
 $\beta \leftarrow$ beta
 $\gamma \leftarrow$ gamma
 $\theta \leftarrow$ theta

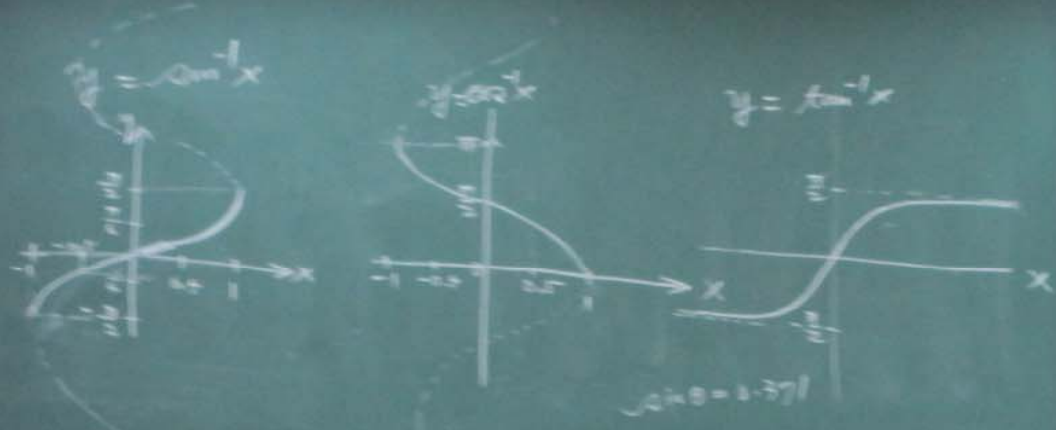
$\alpha \beta \gamma \delta \leftarrow$
 $\lambda \mu \nu \leftarrow$
 \uparrow lambda
 μ

$\vec{d} = \frac{1}{2}\vec{a} + \frac{1}{2}\vec{b}$
 $\vec{c} = \frac{1}{2}\vec{a} + \frac{1}{2}\vec{b}$
 $\vec{f} = \frac{1}{2}(\vec{b} + \vec{c})$
 $\vec{g} = \mu \vec{c} + (1-\mu)\vec{b} = \frac{1}{2}\mu \vec{a} + (1-\mu)\vec{b} + \frac{\mu}{2}\vec{c}$
 $= \lambda \vec{d} + (1-\lambda)\vec{c} = \frac{1}{2}\lambda \vec{a} + \frac{1}{2}\vec{b} + (1-\lambda)\vec{c}$
 $\vec{g} = \frac{1}{2}(\alpha \vec{a} + \vec{b} + \vec{c})$
 $\mu = \lambda, 1-\mu = \frac{1}{2}, \frac{\mu}{2} = 1-\lambda$
 $\mu = \lambda = \frac{2}{3}$

$\vec{GF} = \vec{f} - \vec{g}$
 $= -\frac{1}{3}\vec{a}$
 $\vec{AG} = \vec{g} - \vec{a}$
 $= -\frac{2}{3}\vec{a} + \frac{1}{3}\vec{b} + \frac{1}{3}\vec{c} = \frac{1}{3}(-2\vec{a} + \vec{b} + \vec{c})$

$\vec{a} \cdot \vec{b} = |\vec{a}| |\vec{b}| \cos \theta$

$\vec{p} = \frac{\vec{a} \cdot \vec{b}}{|\vec{b}|} \frac{\vec{b}}{|\vec{b}|}$
 $= \frac{\vec{a} \cdot \vec{b}}{|\vec{b}|^2} \vec{b}$
 $= \frac{\vec{a} \cdot \vec{b}}{|\vec{b}|^2} \vec{b}$

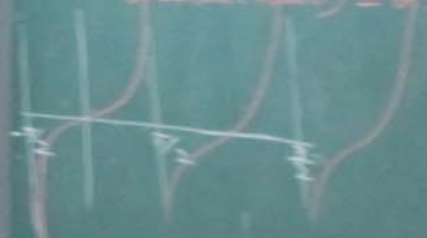


$\sin \theta = 0.571$

$\sin \theta = 0.512 \rightarrow \arcsin(x) = y = \sin^{-1} x$
 $\tan \theta = 1.2$
 $\arcsin(x) = y \rightarrow \sin y = x$
 数值 角度



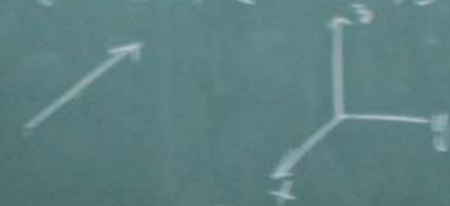
$\arcsin(\sin \theta) = \theta, -\frac{\pi}{2} \leq \theta \leq \frac{\pi}{2}$
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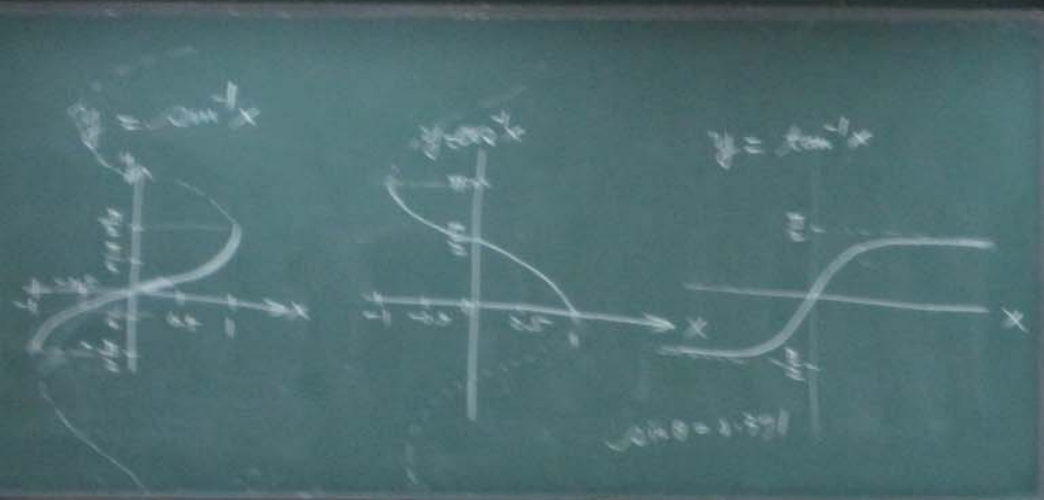


$\arcsin(\sin(\frac{\pi}{6})) = \frac{\pi}{6}$
 $\arcsin(-\frac{1}{2}) = -\frac{\pi}{6}$

* $\sin(22.5^\circ) = \frac{1}{2}\sqrt{2-\sqrt{2}}$
 * 求所有满足 $\cos \theta = \frac{4}{5}$ 之 θ .

向量 Vectors
 純量 Scalars



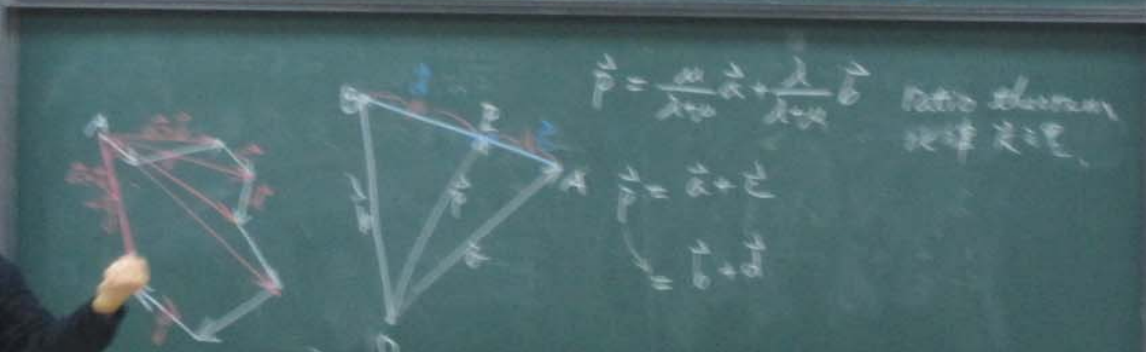
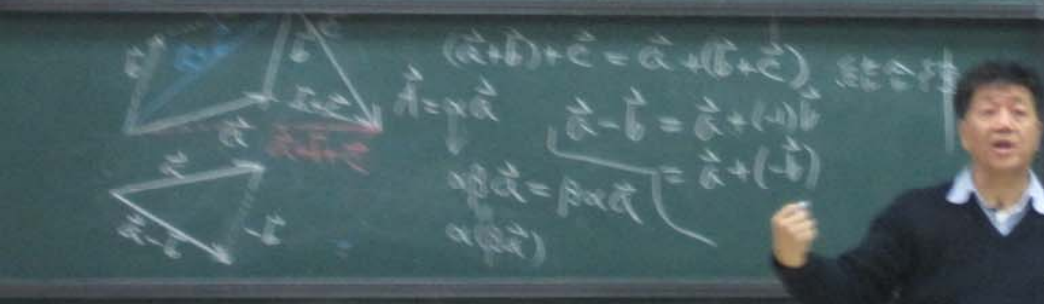


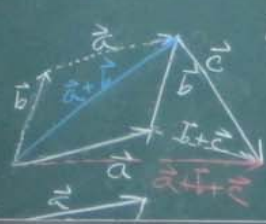
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关系
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 $\theta \leftarrow$ theta

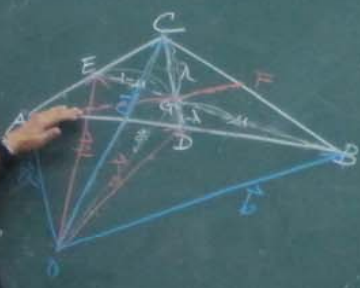
$\alpha \beta \gamma \delta \leftarrow$ alpha beta gamma delta
 $\lambda \mu \nu \leftarrow$ lambda mu nu

$\vec{a} + \vec{b} = \vec{b} + \vec{a}$
 $\alpha(\vec{b} + \vec{c}) = (\alpha\vec{b}) + \alpha\vec{c}$
 $\vec{a} - \vec{b} = \vec{a} + (-\vec{b})$
 $\lambda(\mu\vec{a}) = \lambda(\mu\vec{a}) = \mu(\lambda\vec{a})$
 $\lambda(\vec{a} + \vec{b}) = \lambda\vec{a} + \lambda\vec{b}$
 $(\lambda + \mu)\vec{a} = \lambda\vec{a} + \mu\vec{a}$





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 $(\vec{a} + \vec{b}) + \vec{c} = \vec{a} + (\vec{b} + \vec{c})$ 結合律
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 $\alpha \vec{a} = \vec{a}$



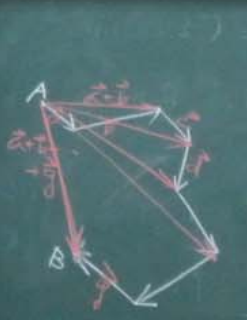
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 $\vec{e} = \frac{1}{2}\vec{a} + \frac{1}{2}\vec{c}$
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向量
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$\alpha \beta \gamma \delta \leftarrow$ delta
 $\lambda \mu \nu \leftarrow$ mu
 lambda

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 $\vec{a} + (\vec{b} + \vec{c}) = (\vec{a} + \vec{b}) + \vec{c}$ 結合律
 $\vec{a} - \vec{b} = \vec{a} + (-\vec{b})$
 $(\lambda \mu)\vec{a} = \lambda(\mu\vec{a}) = \mu(\lambda\vec{a})$
 $\lambda(\vec{a} + \vec{b}) = \lambda\vec{a} + \lambda\vec{b}$
 $(\lambda + \mu)\vec{a} = \lambda\vec{a} + \mu\vec{a}$ 分配律



$\vec{p} = \frac{\mu}{\lambda + \mu} \vec{a} + \frac{\lambda}{\lambda + \mu} \vec{b}$
 $\vec{p} = \vec{a} + \frac{\lambda(\vec{b} - \vec{a})}{\lambda + \mu}$
 $= \vec{a} + \frac{\lambda(\vec{b} - \vec{a})}{\lambda + \mu}$
 $= \frac{\mu}{\lambda + \mu} \vec{a} + \frac{\lambda}{\lambda + \mu} \vec{b}$

ratio theorem 比例定理