

$$\sin(\alpha+\beta) = \sin\alpha \cos\beta + \cos\alpha \sin\beta$$

$$\cos(\alpha+\beta) = \cos\alpha \cos\beta - \sin\alpha \sin\beta$$

$$\alpha = \beta \Rightarrow \sin(2\alpha) = 2 \sin\alpha \cos\alpha$$

$$\alpha = \beta \Rightarrow \cos(2\alpha) = \cos^2\alpha - \sin^2\alpha$$

$$= 2\cos^2\alpha - 1$$

$$= 1 - 2\sin^2\alpha$$

$$\sin(-\alpha) = -\sin\alpha$$

$$\cos(-\alpha) = \cos\alpha$$

$$\cos(2\alpha) = \cos(2\alpha + \alpha)$$

$$= \cos(3\alpha) \cos\alpha - \sin(3\alpha) \sin\alpha$$

$$= (2\cos^2\alpha - 1) \cos\alpha - 2 \sin\alpha \cos\alpha \sin\alpha$$

$$\cos(3\alpha) = 4\cos^3\alpha - 3\cos\alpha$$

$$x^2 - x - 2 = 0$$

$$(x-2)(x+1) = 0$$

$$x = 2, -1$$

$$\sin\theta = 2 \cos\frac{\theta}{2} \sin\frac{\theta}{2}$$

$$= 2^2 \cos\frac{\theta}{4} \cos\frac{\theta}{4} \sin\frac{\theta}{4}$$

$$= 2^3 \cos\frac{\theta}{8} \cos\frac{\theta}{8} \cos\frac{\theta}{8} \sin\frac{\theta}{8}$$

$$\vdots$$

$$= 2^n \cos\frac{\theta}{2^n} \cos\frac{\theta}{2^n} \dots \cos\frac{\theta}{2^n} \sin\frac{\theta}{2^n}$$

$$1 \approx 2^n \cos\frac{\theta}{2^n} \cos\frac{\theta}{2^n} \dots \cos\frac{\theta}{2^n} \left(\frac{\theta}{2^n}\right), \theta = \frac{\pi}{2}$$

$\frac{\theta}{2^n} \approx \frac{\pi}{2^{n+1}}$
 $1 \gg 1$

Vista's formula

$$\frac{10^{-15} \text{ m}}{\pi} \approx \cos\frac{\pi}{2^2} \cos\frac{\pi}{2^3} \dots \cos\frac{\pi}{2^{n+1}}$$

$$10^{-12} \text{ m} \approx \left(\frac{1}{2}\sqrt{2}\right) \left(\frac{1}{2}\sqrt{2+\sqrt{2}}\right) \left(\frac{1}{2}\sqrt{2+\sqrt{2+\sqrt{2}}}\right) \dots \left(\frac{1}{2}\sqrt{2+\sqrt{2+\dots+\sqrt{2}}}\right)$$

$$10^{-9} \text{ m} \approx P$$

π	π
1	3.14159
2	3.06
4	3.140
10	3.14159

femto fermi

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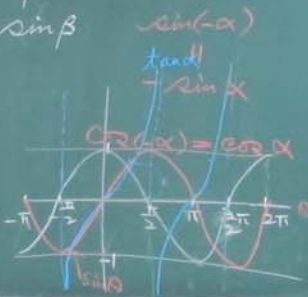
$$\sin(\alpha \pm \beta) = \sin \alpha \cos \beta \pm \cos \alpha \sin \beta$$

$$\cos(\alpha \pm \beta) = \cos \alpha \cos \beta \mp \sin \alpha \sin \beta$$

$$\alpha = \beta \Rightarrow \sin(2\alpha) = 2 \sin \alpha \cos \alpha$$

$$\alpha = \beta \Rightarrow \cos(2\alpha) = \cos^2 \alpha - \sin^2 \alpha$$

$$\tan(\alpha \pm \beta) = \frac{\tan \alpha \pm \tan \beta}{1 \mp \tan \alpha \tan \beta}$$



$$\sin \theta = 2 \cos \frac{\theta}{2} \sin \frac{\theta}{2}$$

$$= 2^2 \cos \frac{\theta}{4} \cos \frac{\theta}{4} \sin \frac{\theta}{4} \sin \frac{\theta}{4}$$

$$= 2^3 \cos \frac{\theta}{8} \cos \frac{\theta}{8} \cos \frac{\theta}{8} \cos \frac{\theta}{8} \sin \frac{\theta}{8} \sin \frac{\theta}{8} \sin \frac{\theta}{8} \sin \frac{\theta}{8}$$

$$\vdots = 2^n \cos \frac{\theta}{2^n} \cos \frac{\theta}{2^n} \dots \cos \frac{\theta}{2^n} \sin \frac{\theta}{2^n} \sin \frac{\theta}{2^n} \dots \sin \frac{\theta}{2^n} \sin \frac{\theta}{2^n}$$

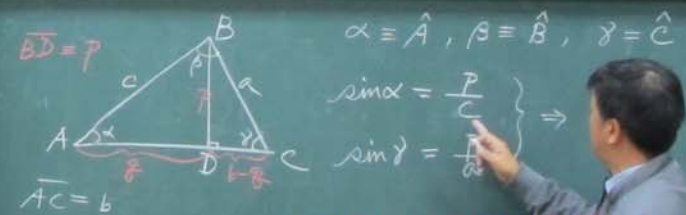
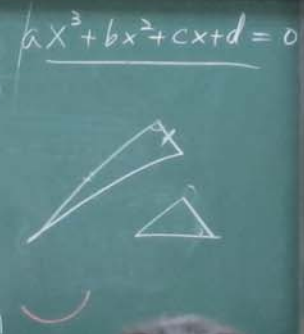
$\theta = \frac{\pi}{2}$ $n > 1$

$$t = \tan\left(\frac{\alpha}{2}\right)$$

$$\sin \alpha = \frac{2t}{1+t^2}$$

$$\cos \alpha = \frac{1-t^2}{1+t^2}$$

$$\tan \alpha = \frac{2t}{1-t^2}$$



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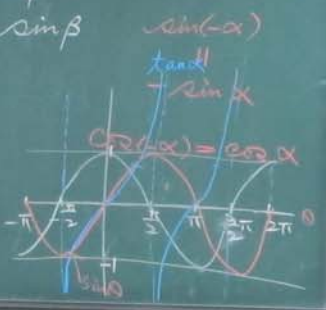
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$$\alpha = \beta \Rightarrow \cos(2\alpha) = \cos^2\alpha - \sin^2\alpha$$

$$\tan(\alpha+\beta) = \frac{\tan\alpha + \tan\beta}{1 - \tan\alpha \tan\beta}$$



$$\sin\theta = 2 \cos \frac{\theta}{2} \sin \frac{\theta}{2}$$

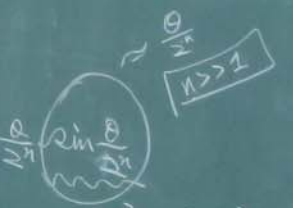
$$= 2^2 \cos \frac{\theta}{4} \sin \frac{\theta}{4} \cos \frac{\theta}{4} \sin \frac{\theta}{4}$$

$$= 2^3 \cos \frac{\theta}{8} \cos \frac{\theta}{8} \cos \frac{\theta}{8} \sin \frac{\theta}{8} \sin \frac{\theta}{8} \sin \frac{\theta}{8}$$

$$\vdots$$

$$= 2^{n-1} \cos \frac{\theta}{2^{n-1}} \cos \frac{\theta}{2^{n-1}} \dots \cos \frac{\theta}{2^{n-1}} \sin \frac{\theta}{2^{n-1}}$$

$$\theta = \frac{\pi}{2} \quad \theta = \frac{\pi}{2^n}$$



$$c^2 = a^2 + b^2 - 2ab \cos \theta$$

$$a^2 = b^2 + c^2 - 2bc \cos \alpha$$

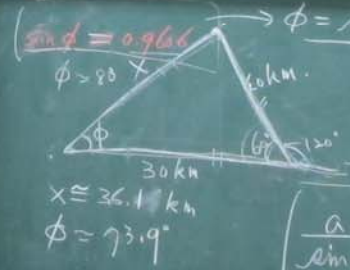
$$a^2 = b^2 + c^2 - 2bc \cos \alpha$$

$$c^2 = a^2 + b^2 - 2ab \cos \gamma$$

$$b^2 = c^2 + a^2 - 2ca \cos \beta$$

the law of cosines
餘弦定律

$$aX^2 + bX + c + d = 0$$



$$\phi = \sin^{-1}(0.966) \beta = \hat{B}, \gamma =$$

$$\frac{p}{c} \left. \begin{matrix} \frac{p}{a} \\ \frac{a}{c} \end{matrix} \right\} \Rightarrow p =$$

$$y = \sin^{-1}(x) \equiv \arcsin$$

$$x = \sin y.$$

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