

The chiral magnetic effect

in quark-gluon plasma and condensed matter

D. Kharzeev



Stony Brook University



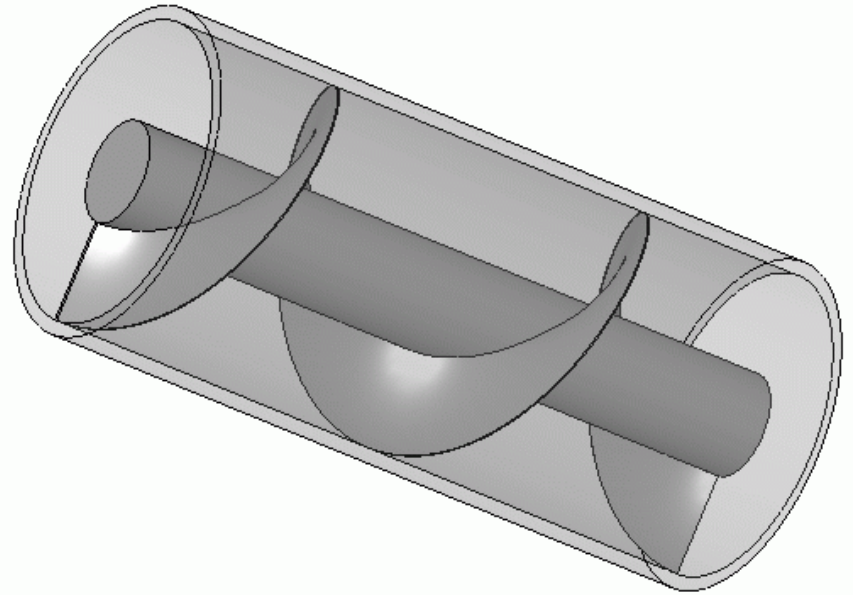
RIKEN BNL
Research Center

BROOKHAVEN
NATIONAL LABORATORY

Chirality and transport:

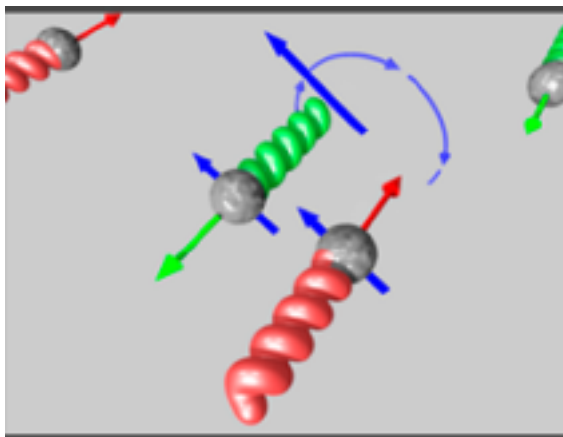
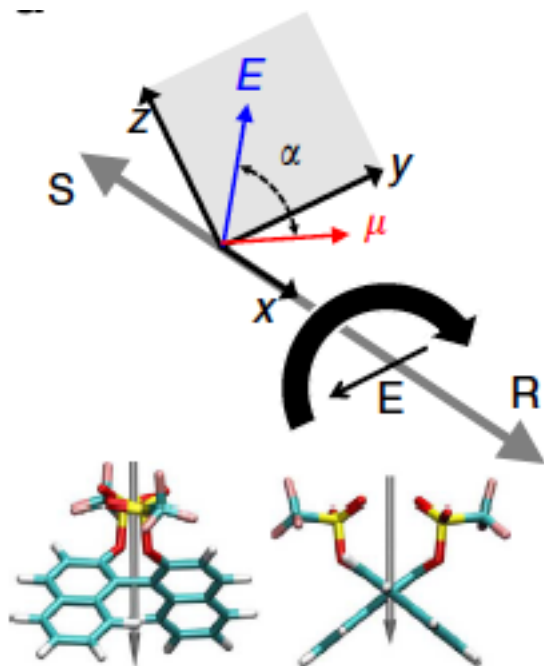
classical physics

Chirality and hydrodynamics 240 B.C.



The Archimedes screw

Propeller effect in a fluid

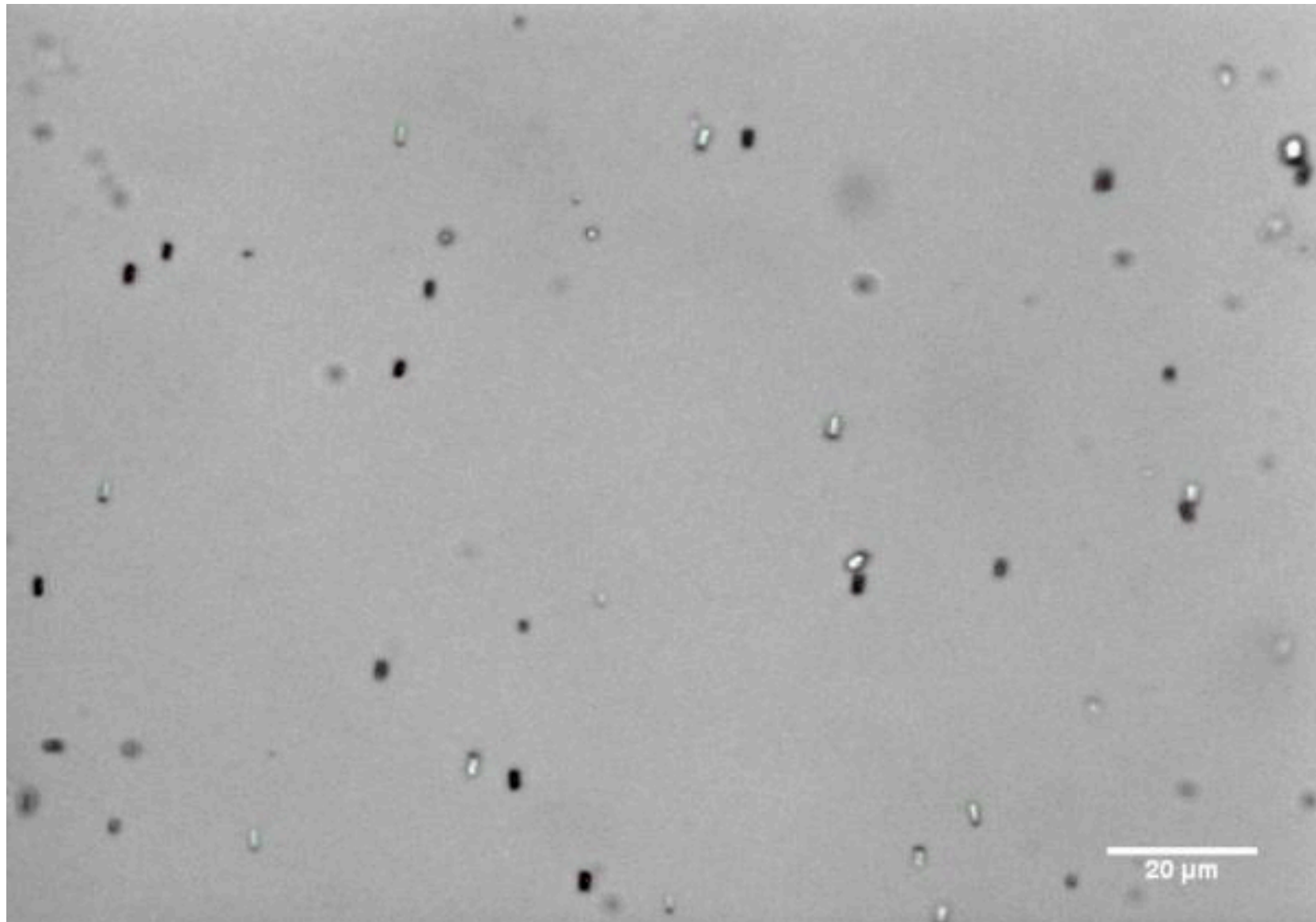


How to rotate the chiral molecule in a fluid?

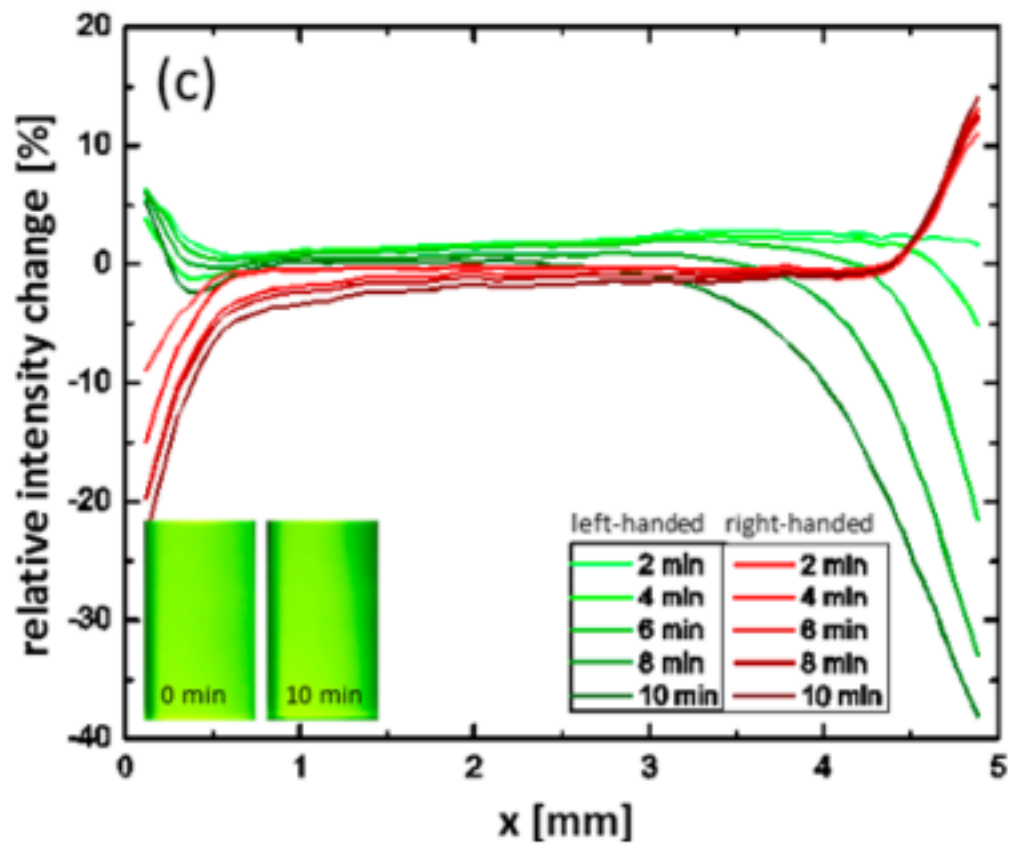
Use the coupling of an external electric field to the molecule's electric dipole moment!

Rotating electric field – rotating molecule

Baranova, Zel'dovich '78



D.Schamel et al, JACS 135, 12353 (2013)



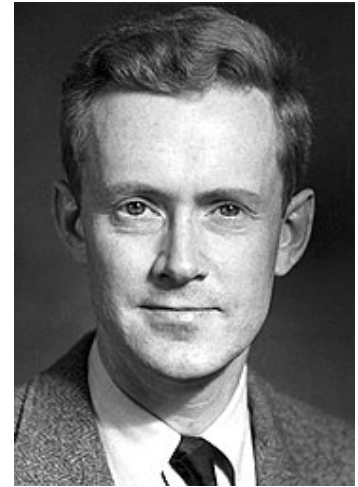
D.Schamel et al, JACS 135, 12353 (2013)

Life at low Reynolds number

E. M. Purcell

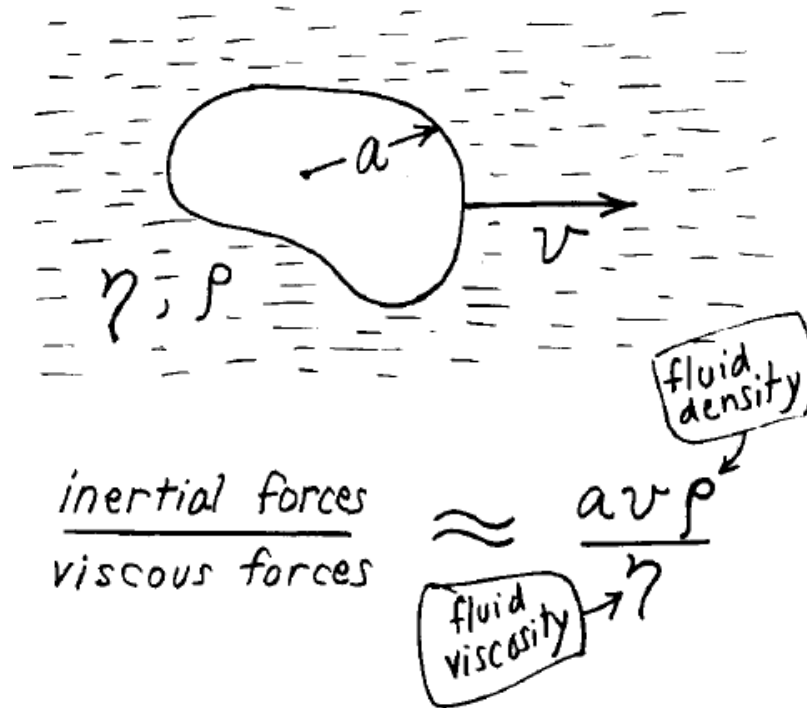
Lyman Laboratory, Harvard University, Cambridge, Massachusetts 02138

(Received 12 June 1976)



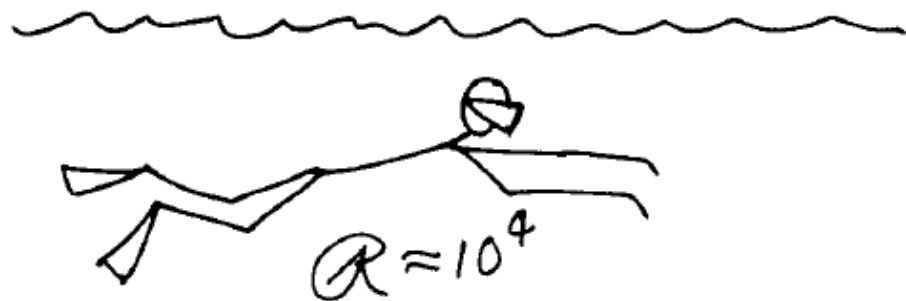
E.M.Purcell
(1912-1997)

Nobel prize, 1952
(Nuclear Magnetic Resonance)



$$R \equiv \frac{av\rho}{\eta} = \frac{av}{\nu}$$

$\nu = 10^{-2} \frac{\text{cm}^2}{\text{sec}}$ for water




$$R \approx 10^2$$



Navier - Stokes:

$$-\nabla p + \eta \nabla^2 \vec{v} = \cancel{\rho \frac{\partial \vec{v}}{\partial t}} + \cancel{\rho (\vec{v} \cdot \nabla) \vec{v}}$$

If $Q \ll 1$:

Time doesn't matter. The pattern of motion is the same, whether slow or fast, whether forward or backward in time.

The Scallop Theorem



Stokes equation
("creeping flow")

T-invariance!



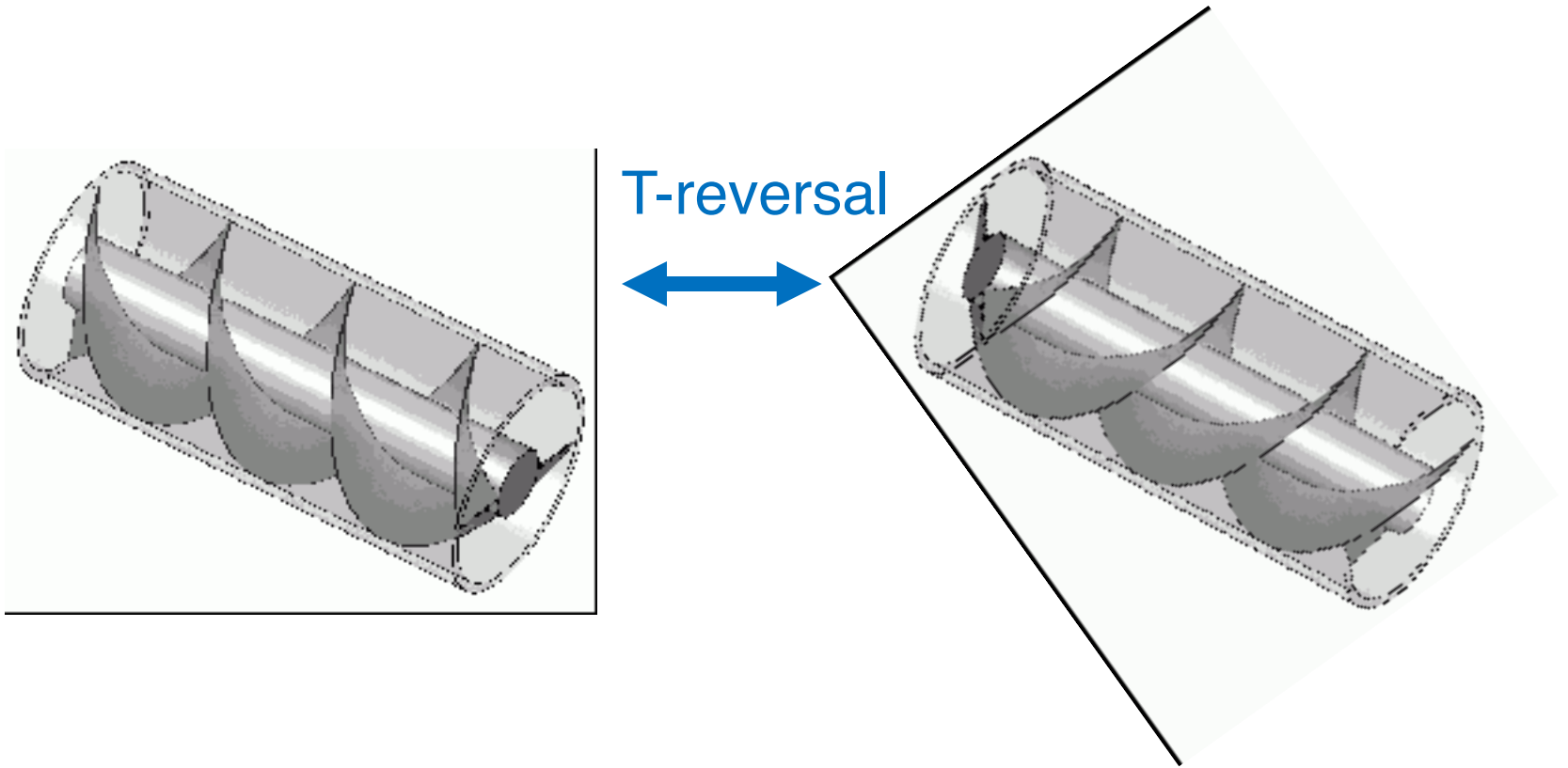
Sir G. Stokes
(1819-1903)

Geometry of the gauge field
on the space of shapes

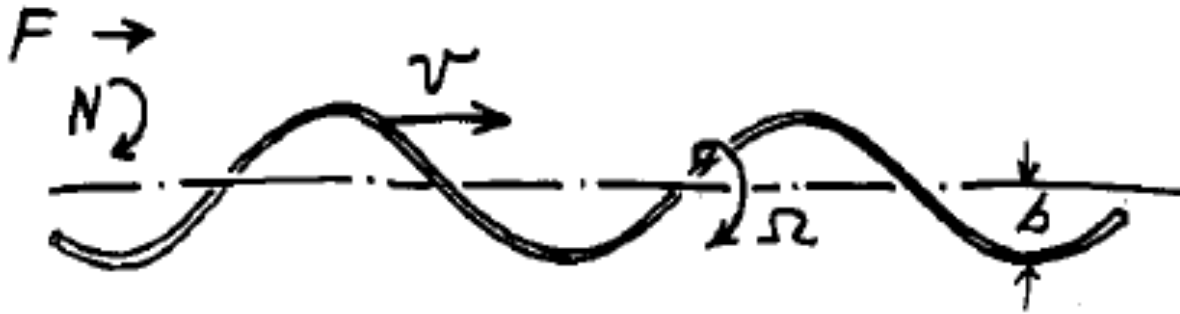
A. Shapere, F. Wilczek '88

Need to break T-invariance to move – chirality!

Left-handed screw



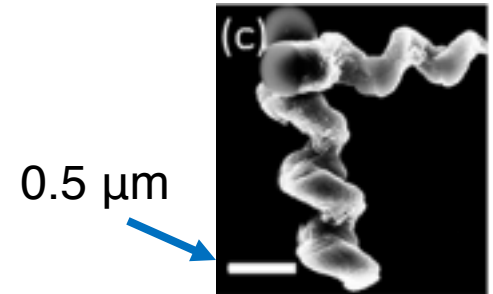
The propulsion matrix



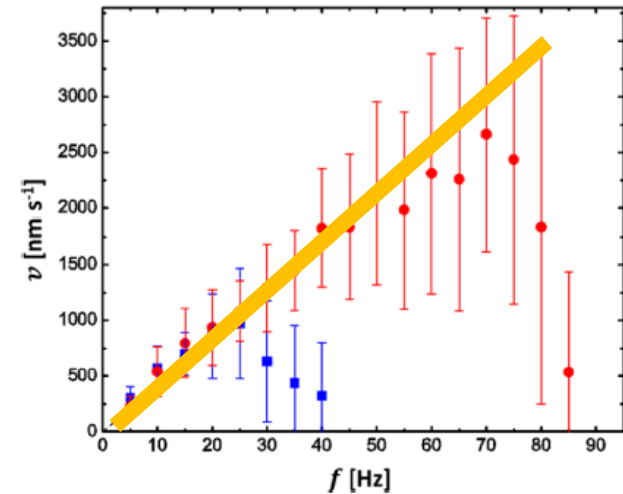
(force) $F = A v + B \Omega$

(torque) $N = C v + D \Omega$

$$|P| \equiv \begin{vmatrix} A & B \\ C & D \end{vmatrix}$$



B=20 G
B=50 G

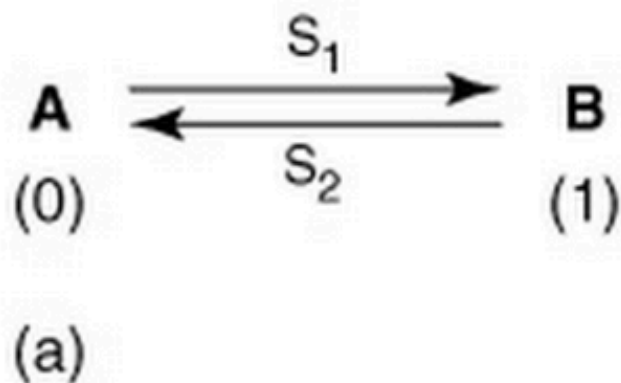


Chiral propellers at
low Reynolds number

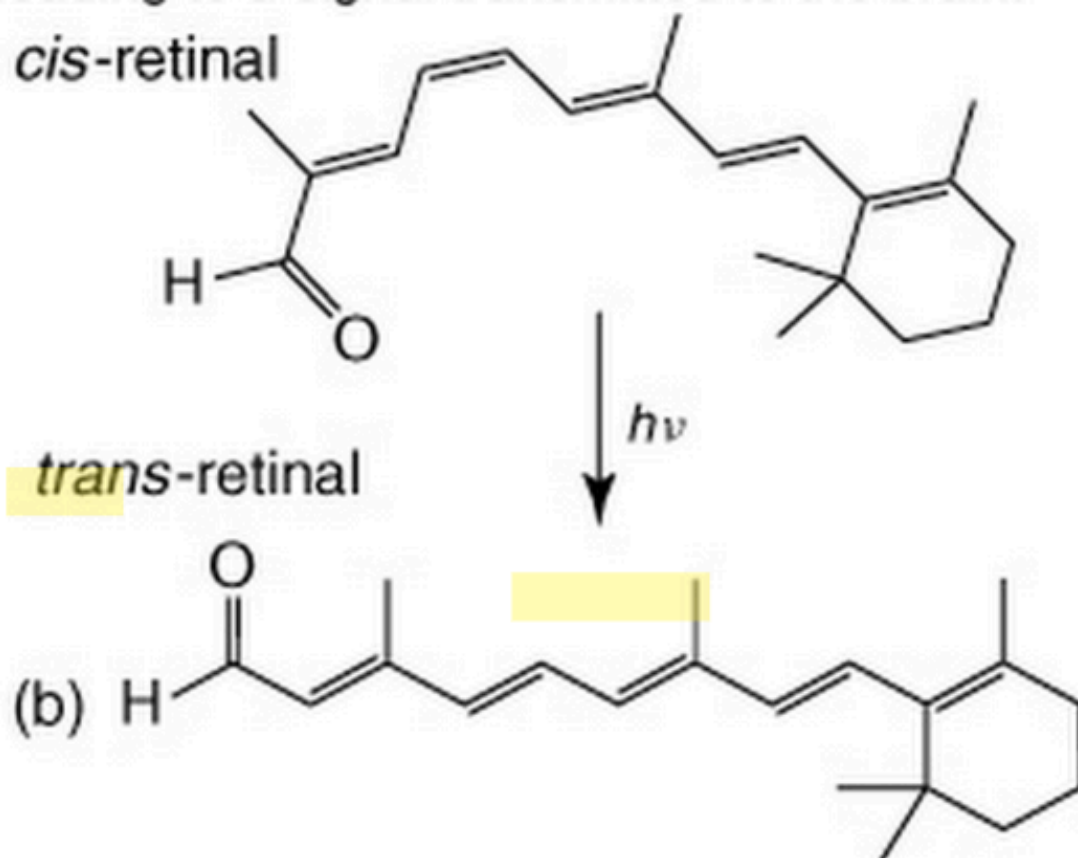
S.Ayf, I.Cook, DK, to appear

Chirality imbalance = transport

Chirality and vision



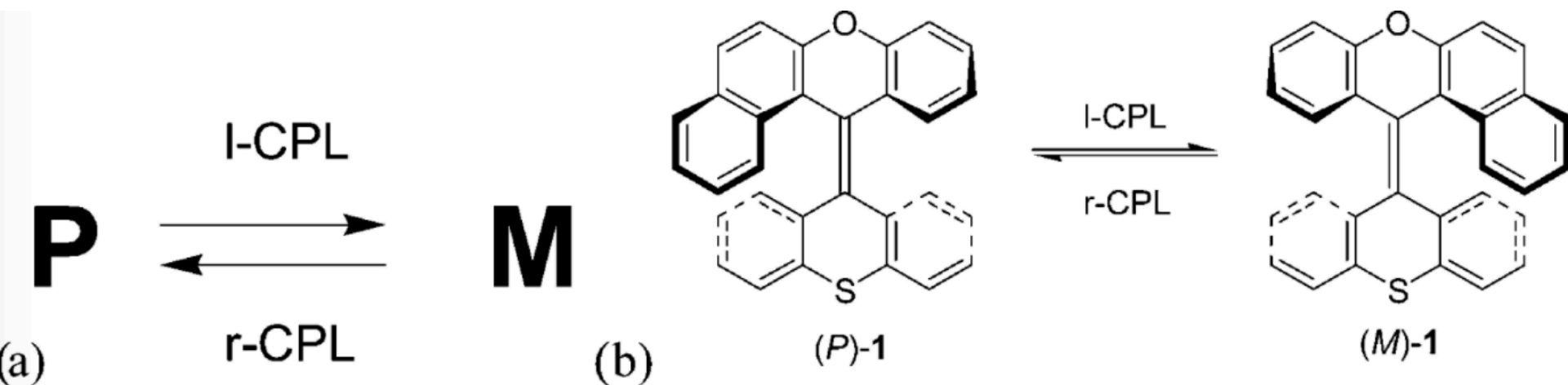
B. Feringa, W. Browne,
"Molecular switches", 2011



Protein-bound retinal molecule as a chiroptical switch:
the mechanism of **vision** **chiral photo-pharmacology**

Chiroptical switching of chiral molecules

Need circularly polarized light (CPL), with frequency optimized for inducing the tunnel transition between the enantiomers.



Review: B.Feringa, *J. Org. Chem.*, **2007**, 72 (18), pp 6635–6652

Applications: pharmaceuticals, “chiral photomedicine”, optical data storage and processing, ...



Scientific Background on the Nobel Prize in Chemistry 2016

MOLECULAR MACHINES



J.-P. Sauvage



Sir J.F. Stoddart



B.L. Feringa

Chirality and quantum transport

Chiral anomaly

For massless fermions, the axial current

$$J_{\mu}^A = \bar{\Psi} \gamma_{\mu} \gamma_5 \Psi = J_{\mu}^R - J_{\mu}^L$$

is conserved classically due to the global $U_A(1)$ symmetry:

$$\partial^{\mu} J_{\mu}^A = 0$$

However this conservation law is destroyed by quantum effects

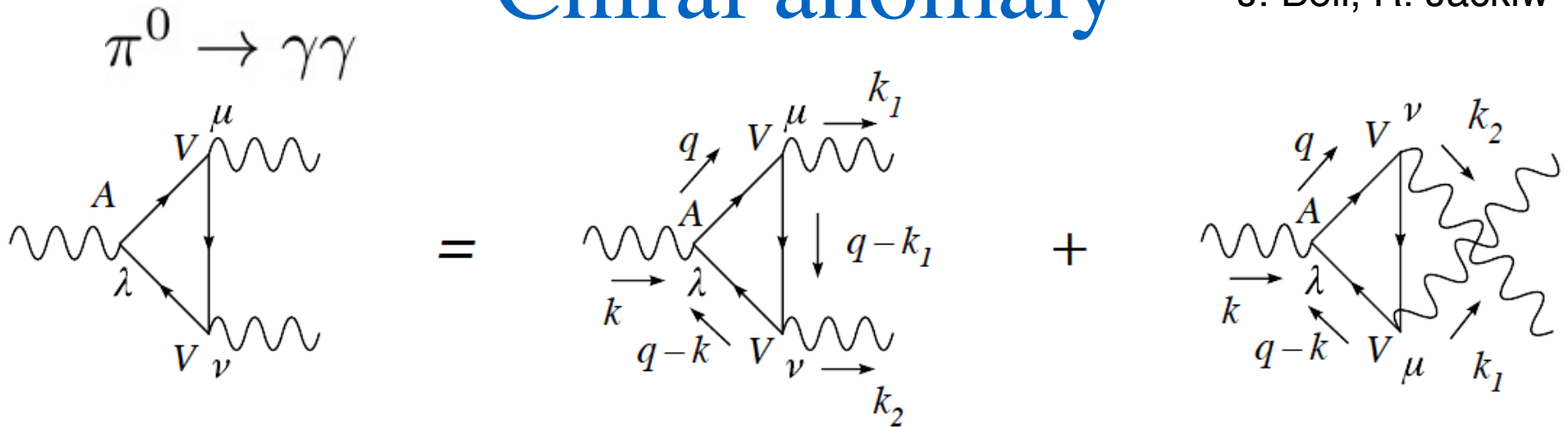
S. Adler '69

J. Bell, R. Jackiw '69

Chiral anomaly

S. Adler '69

J. Bell, R. Jackiw '69



$$k_\lambda \Delta^{\lambda\mu\nu}(k_1, k_2) = a_n \epsilon^{\mu\nu\alpha\beta} k_{1\alpha} k_{2\beta} \quad a_n = -i/2\pi^2$$

$$\Delta^{\lambda\mu\nu} = a_n \frac{k^\lambda}{k^2} \epsilon^{\mu\nu\alpha\beta} k_{1\alpha} k_{2\beta}$$

The chiral anomaly does not vanish at finite mass,
and mass corrections have been evaluated, see e.g. 

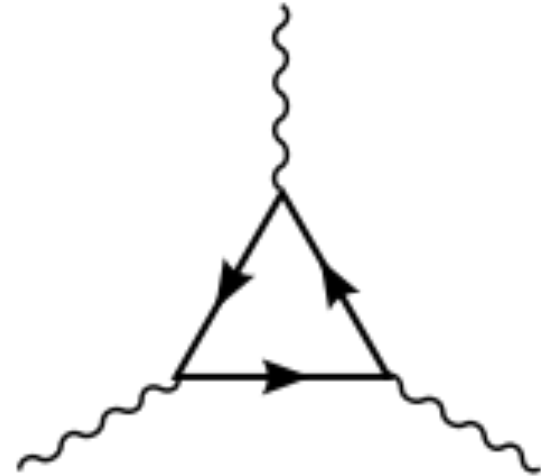
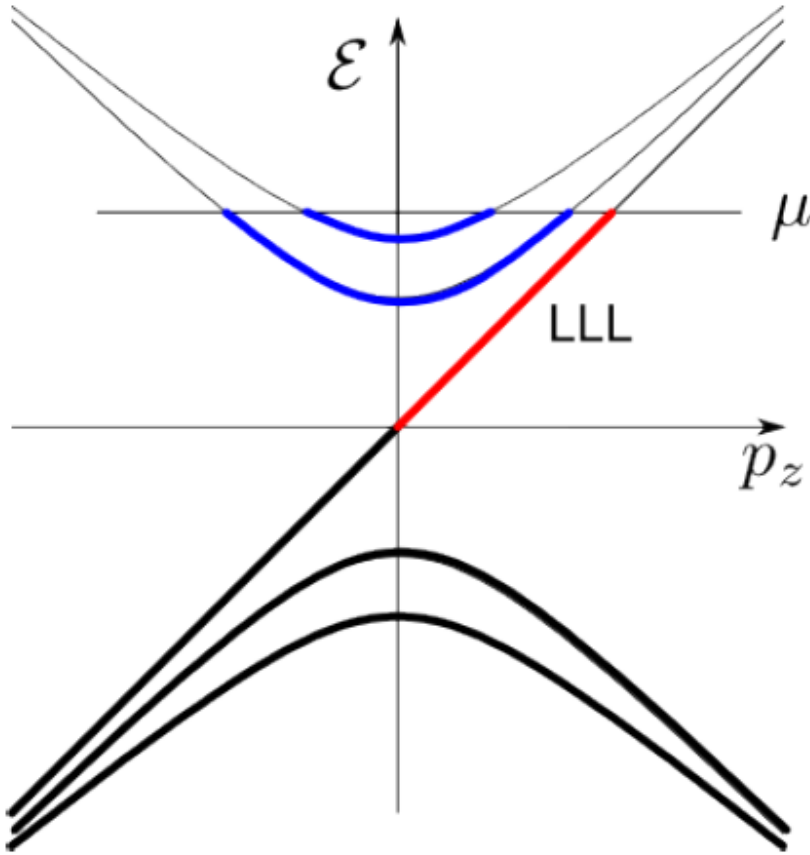
Possibility of anomalous
transport in systems with
a finite gap (strange quarks,
semiconductors)?

A.D. Dolgov, V.I. Zakharov, Nucl. Phys. B27 (1971) 525

R. Armillis et al, JHEP 0912 (2009) 029

$$w_L = -\frac{4i}{s} - \frac{4im^2}{s^2} \log\left(-\frac{s}{m^2}\right) + O(m^3) \quad s \equiv k^2$$

Chiral anomaly



In classical background fields (E and B), chiral anomaly induces a collective motion in the Dirac sea

Chiral Magnetic Effect

K.Fukushima, DK, H.Warringa, PRD'08;
Review and list of refs: DK, arXiv:1312.3348

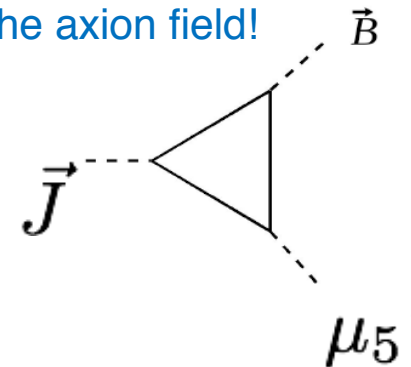
Chiral chemical potential is formally equivalent to a background chiral gauge field:

$$\mu_5 = A_5^0$$

Time derivative
of the axion field!

In this background, and in the presence of $\vec{B}$,
vector e.m. current is generated:

$$\partial_\mu J^\mu = \frac{e^2}{16\pi^2} \left(F_L^{\mu\nu} \tilde{F}_{L,\mu\nu} - F_R^{\mu\nu} \tilde{F}_{R,\mu\nu} \right)$$



Compute the current through

$$J^\mu = \frac{\partial \log Z[A_\mu, A_\mu^5]}{\partial A_\mu(x)}$$

The result:

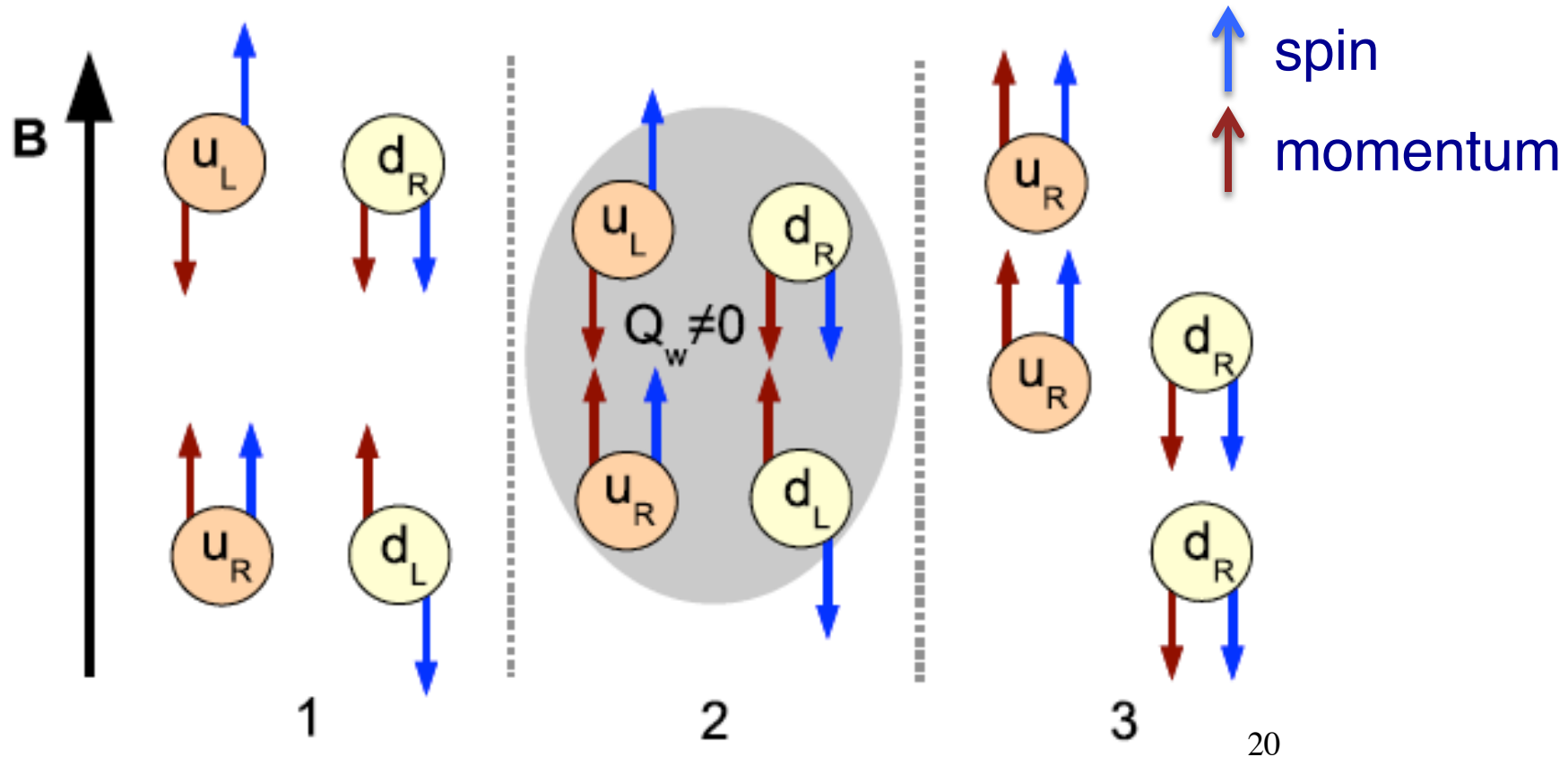
$$\vec{J} = \frac{e^2}{2\pi^2} \mu_5 \vec{B}$$

Absent in Maxwell theory!

Coefficient is fixed by
the axial anomaly, no
corrections

Chirality in 3D: the Chiral Magnetic Effect

chirality + magnetic field = current



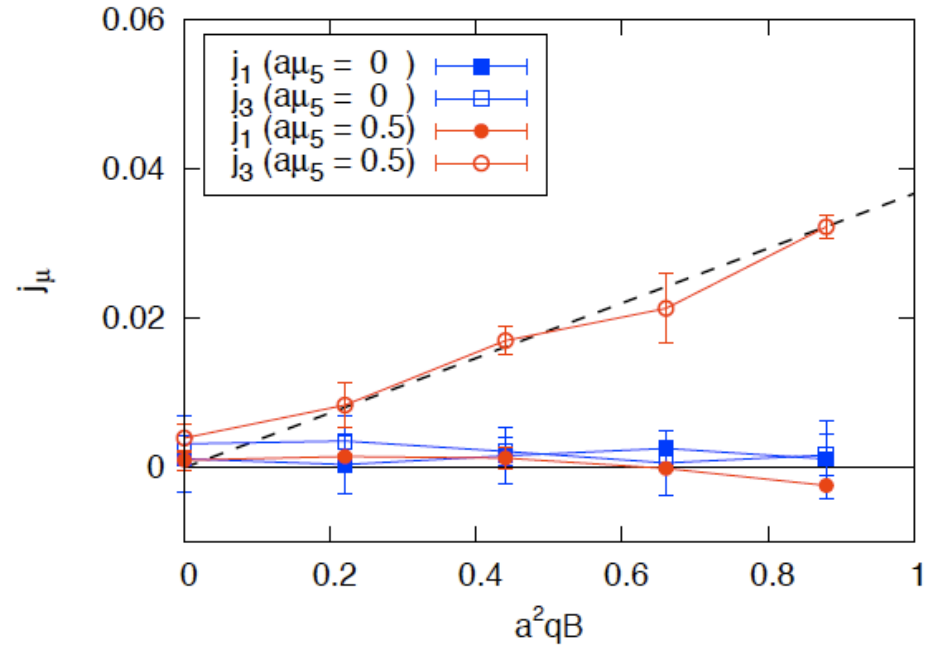
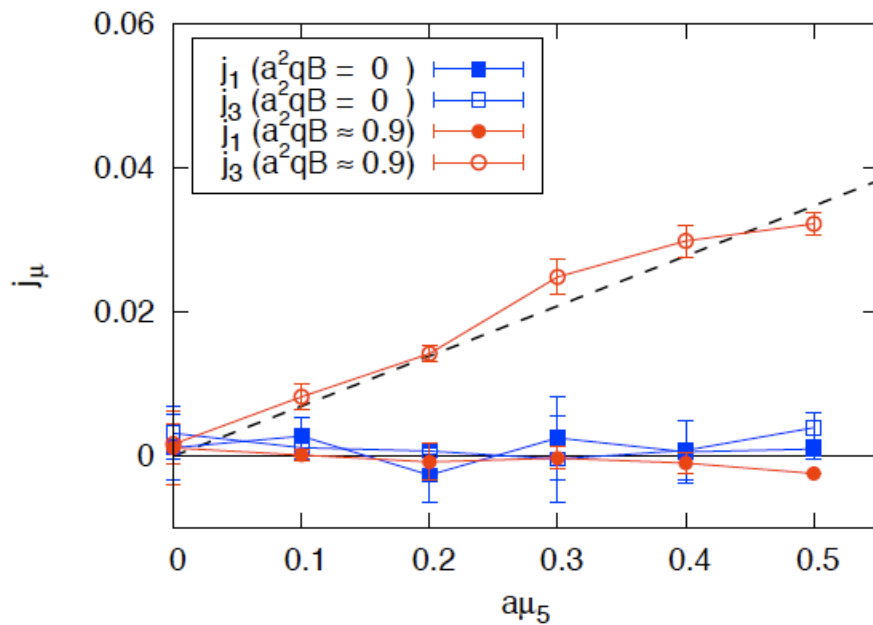
Chiral magnetic effect in lattice QCD with chiral chemical potential

Arata Yamamoto

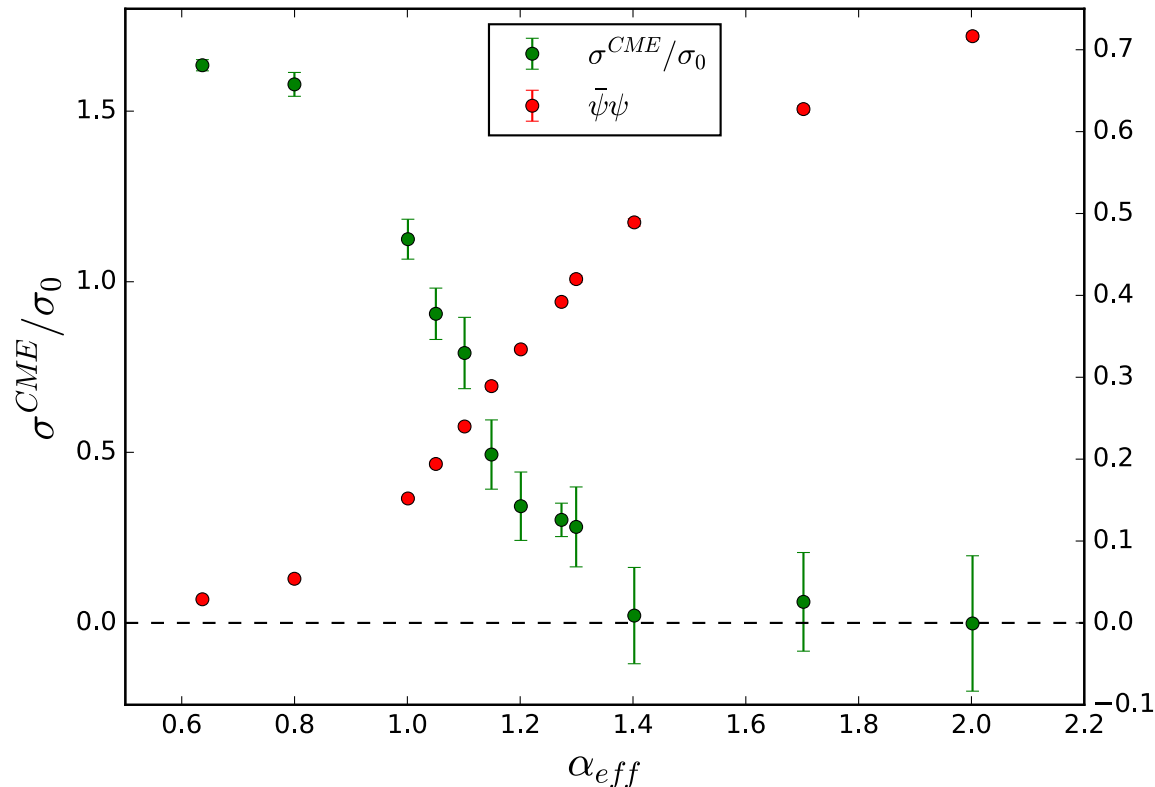
Department of Physics, The University of Tokyo, Tokyo 113-0033, Japan

(Dated: May 3, 2011)

We perform a first lattice QCD simulation including two-flavor dynamical fermion with chiral chemical potential. Because the chiral chemical potential gives rise to no sign problem, we can exactly analyze a chirally asymmetric QCD matter by the Monte Carlo simulation. By applying an external magnetic field to this system, we obtain a finite induced current along the magnetic field, which corresponds to the chiral magnetic effect. The obtained induced current is proportional to the magnetic field and to the chiral chemical potential, which is consistent with an analytical prediction.



Chiral magnetic effect as a signature of chiral symmetry restoration



DK'04
DK, McLerran,
Warringa'07
Fukushima, DK,
Warringa '08

V.Braguta et al,
arxiv:1704.07132,
and to appear

The spontaneous breaking of chiral symmetry does not allow the chiral magnetic current to propagate

Chiral magnetic conductivity: discrete symmetries

P – parity

T – time reversal

$$\vec{J} = \frac{e^2}{2\pi^2} \mu_5 \vec{B}$$

P-odd

T-odd

P-even

T-odd

P-odd

P-odd effect!

T-even

Non-dissipative current!
(topologically protected)

Effect persists in
hydrodynamics!

cf Ohmic
conductivity:

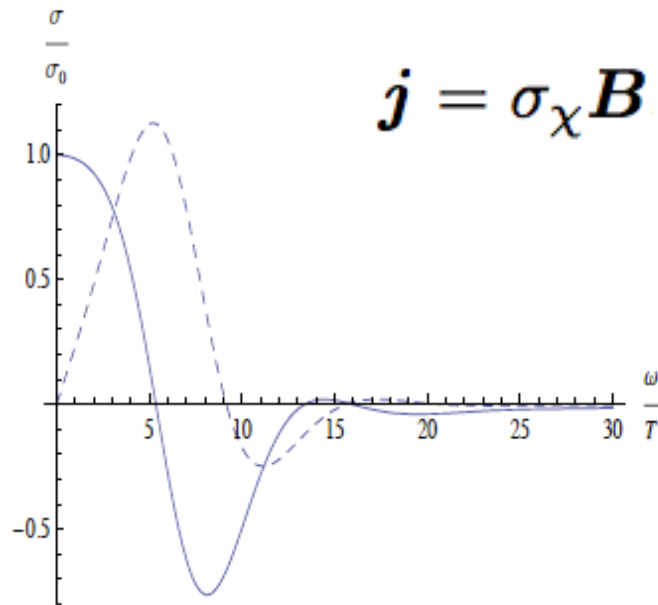
$$\vec{J} = \sigma \vec{E}$$

T-odd,
dissipative

Dynamical chiral magnetic effect

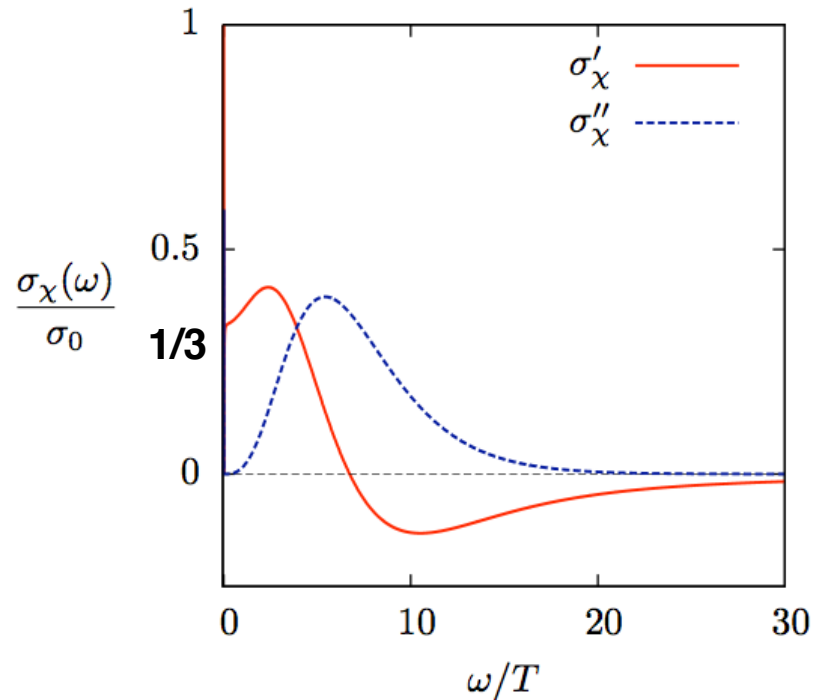
Strong coupling

$\mu/T=0.1$



H.-U. Yee, arXiv:0908.4189,
JHEP 0911:085, 2009;

Weak coupling



D.K., H. Warringa
Phys Rev D80 (2009) 034028

A.Rebhan, A.Schmitt, S.Stricker JHEP 0905, 084 (2009), G.Lifshytz, M.Lippert, arXiv:0904.4772;.A. Gorsky, P. Kopnin, A. Zayakin, arXiv:1003.2293, A.Gynther, K. Landsteiner, F. Pena Benitez, JHEP 1102 (2011) 110; V. Rubakov, arXiv:1005.1888, C. Hoyos, T. Nishioka, A. O'Bannon, JHEP1110 (2011) 084; ...

CME persists at strong coupling - **hydrodynamical formulation?**

CME out of equilibrium: chiral kinetic theory

CKT:

M. Stephanov, Y. Yin, PRL109(2012)162001;

J.W. Chen, S. Pu, Q. Wang, X.-N.Wang,

PRL110(2013)262301;

J.W. Chen, T. Ishii, S. Pu, N. Yamamoto,

PRD93(2016)125023; ...

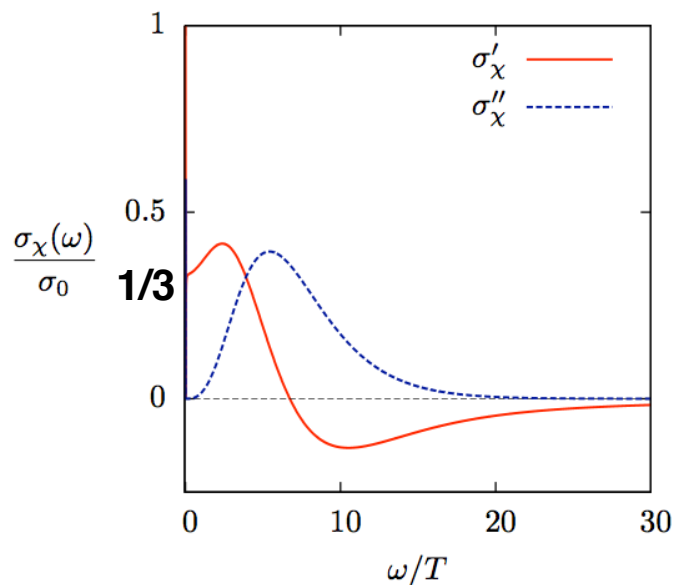
AC CME conductivity: why 1/3?

2/3 from Berry phase, 1/3 from energy shift – so
at finite frequency expect 2/3 – what is the missing -1/3?

Magnetization current!

DK, M.Stephanov, H.-U.Yee.

arXiv:1612.01674; PRD'17



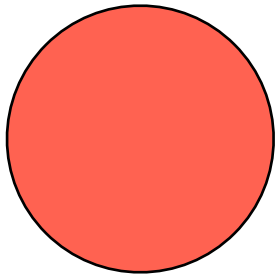
Hydrodynamics and symmetries

- Hydrodynamics: an effective low-energy TOE. States that the response of the fluid to slowly varying perturbations is completely determined by conservation laws (energy, momentum, charge, ...)
- Conservation laws are a consequence of symmetries of the underlying theory
- What happens to hydrodynamics when these symmetries are broken by quantum effects (anomalies of QCD and QED)?

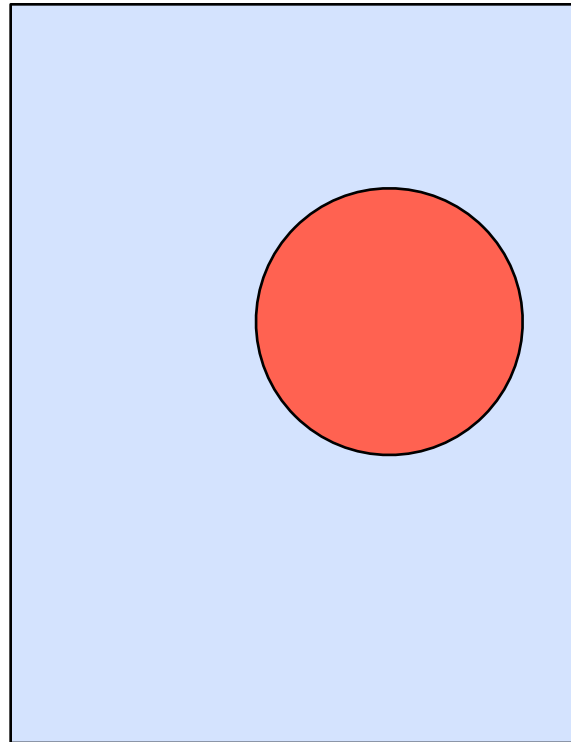
No entropy production from P-odd anomalous terms

DK and H.-U. Yee, 1105.6360; PRD

Entropy grows



$$\partial_{\mu} s^{\mu} \geq 0$$



Mirror reflection:
entropy decreases ?

$$\partial_{\mu} s^{\mu} \leq 0$$

Decrease is ruled
out by 2nd law of
thermodynamics



$$\partial_{\mu} s^{\mu} = 0_{27}$$

Allows to compute analytically 13 out of 18
anomalous transport coefficients in 2nd order
relativistic hydrodynamics

Systematics of anomalous conductivities

Magnetic field

Vorticity

Vector
current

$$\frac{\mu_A}{2\pi^2}$$

$$\frac{\mu\mu_A}{2\pi^2}$$

Axial
current

$$\frac{\mu}{2\pi^2}$$

$$\frac{\mu^2 + \mu_A^2}{4\pi^2} + \frac{T^2}{12}$$

The CME in relativistic hydrodynamics:

The Chiral Magnetic Wave

DK, H.-U. Yee,
arXiv:1012.6026 [hep-th];
PRD

$$\vec{j}_V = \frac{N_c e}{2\pi^2} \mu_A \vec{B}; \quad \vec{j}_A = \frac{N_c e}{2\pi^2} \mu_V \vec{B},$$

CME Chiral separation

$$\begin{pmatrix} \vec{j}_V \\ \vec{j}_A \end{pmatrix} = \frac{N_c e \vec{B}}{2\pi^2} \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix} \begin{pmatrix} \mu_V \\ \mu_A \end{pmatrix}$$

Propagating chiral wave: (if chiral symmetry
is restored)

$$\left(\partial_0 \mp \frac{N_c e B \alpha}{2\pi^2} \partial_1 - D_L \partial_1^2 \right) j_{L,R}^0 = 0$$

Gapless collective mode is the carrier of CME current in MHD:

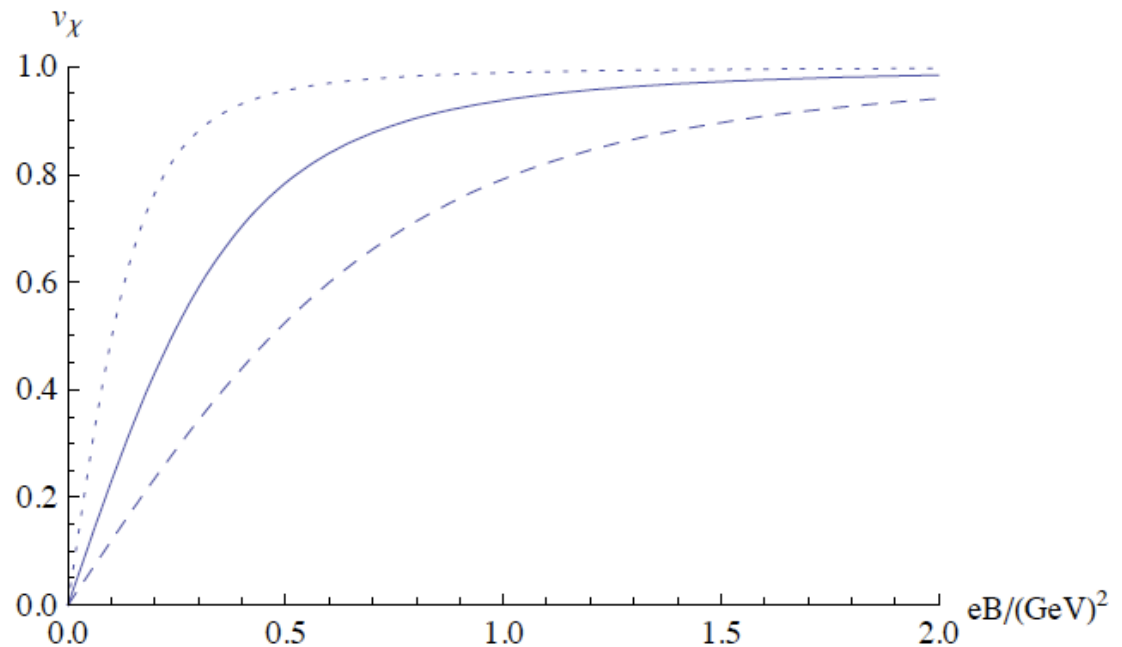
$$\omega = \mp v_\chi k - i D_L k^2 + \dots$$



The Chiral Magnetic Wave:

oscillations of electric and chiral charges
coupled by the chiral anomaly

In strong magnetic field, CMW
propagates with the speed of light!

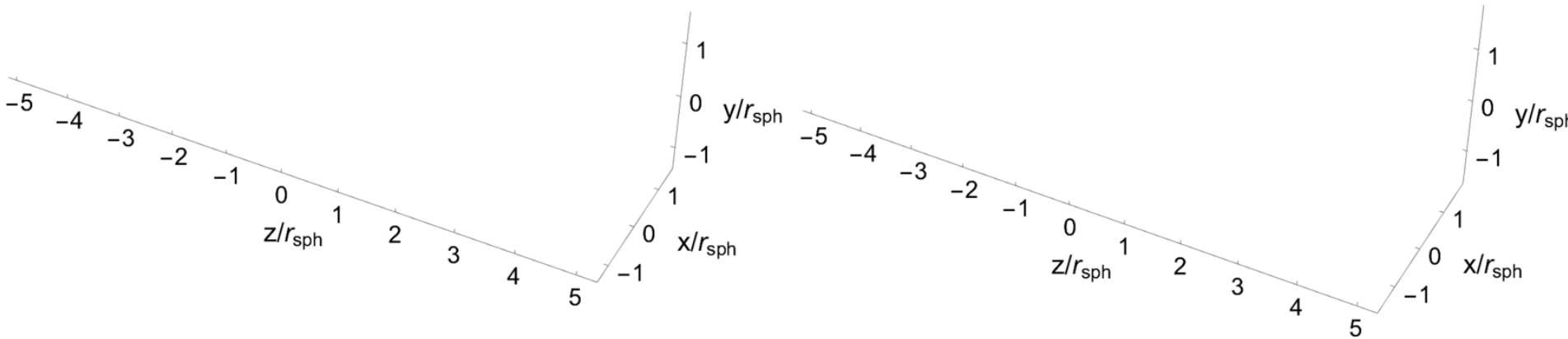


Anomalous transport in real time

j_a^0 :axial charge $\xrightarrow{\text{B}}$ j_v^0 :vector charge

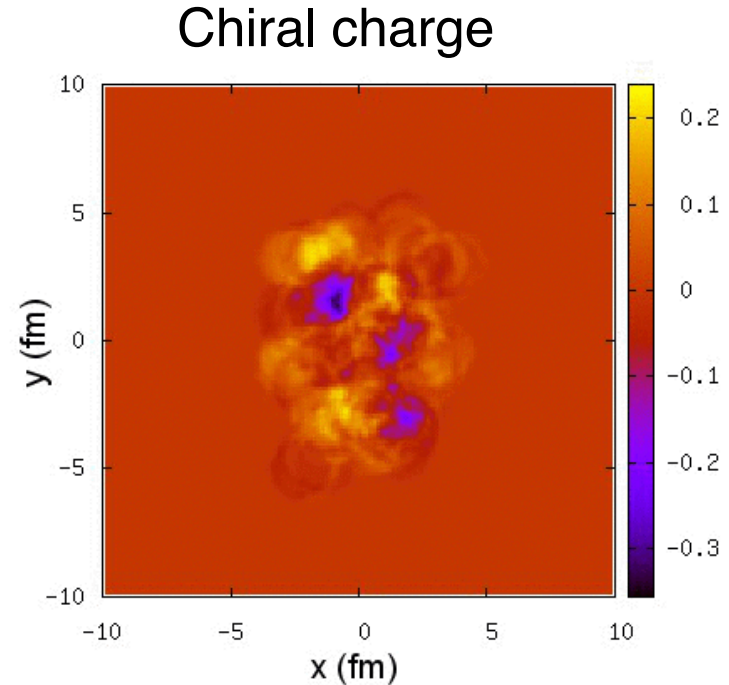
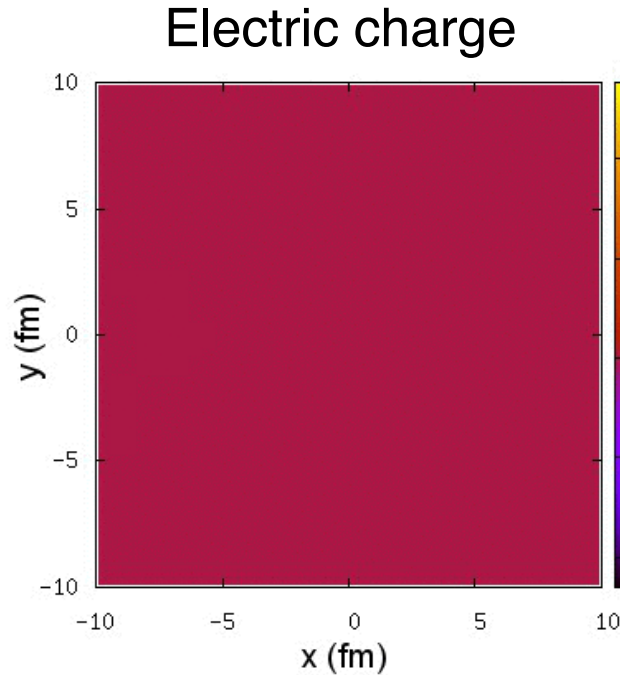
$t/t_{\text{sph}}=0$

$t/t_{\text{sph}}=0$



Static U(1) magnetic field in z-dir

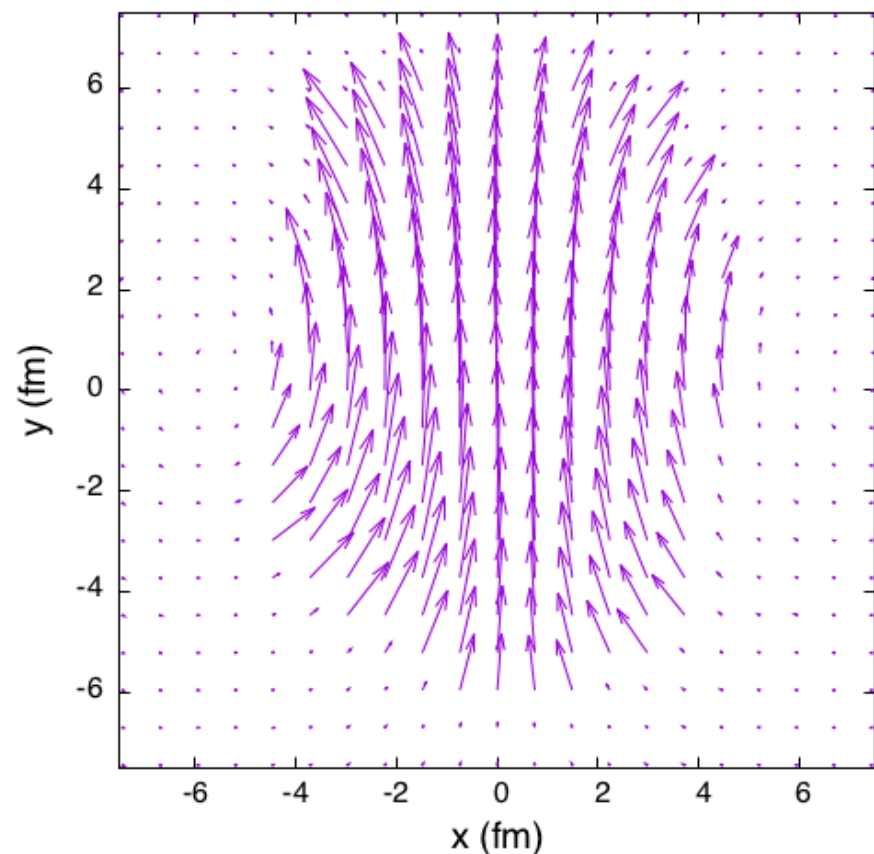
Chiral Magnetohydrodynamics (CMHD)



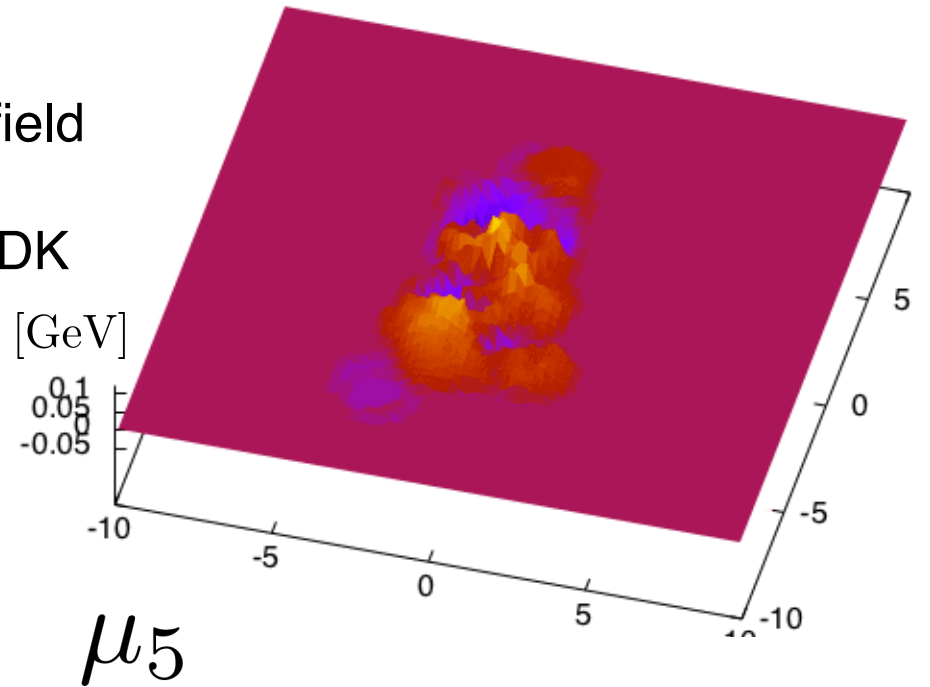
Y.Hirono, T.Hirano, DK, (Stony Brook – Tokyo), arxiv:1412.0311
(3+1) ideal CMHD (Chiral MagnetoHydroDynamics)

BEST Theory Collaboration (DOE)

CMHD with dynamical MHD magnetic field
 from ECHO-QGP: Y. Hirono, M. Mace,
 G. Inghirami, F. Becattini, L. Del Zanna, DK

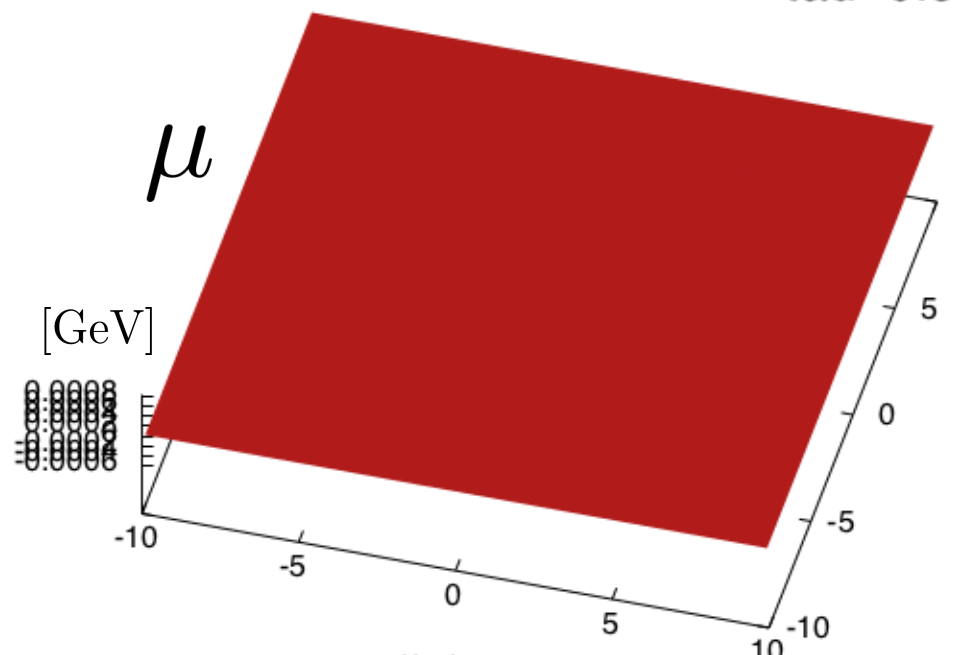


B field evolution
 in transverse plane



μ_5

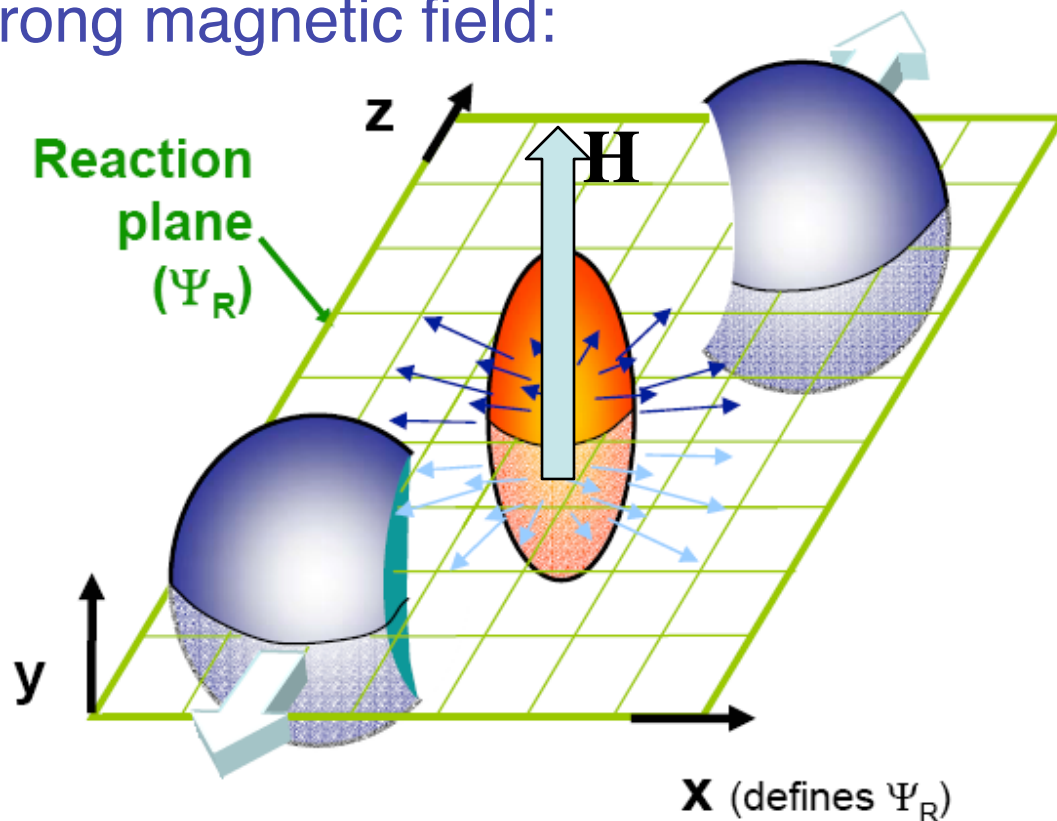
$\tau = 0.5$



μ

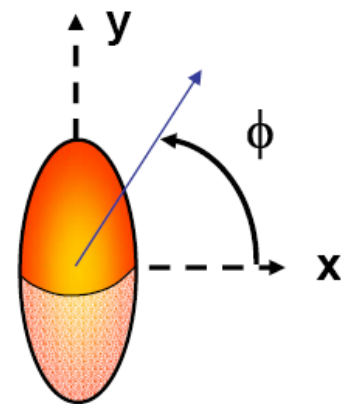
Is there a way to observe CME in nuclear collisions at RHIC and LHC?

Relativistic ions create
a strong magnetic field:

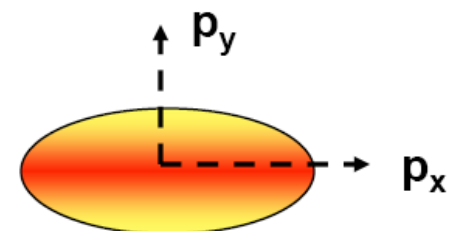


DK, McLerran, Warringa '07

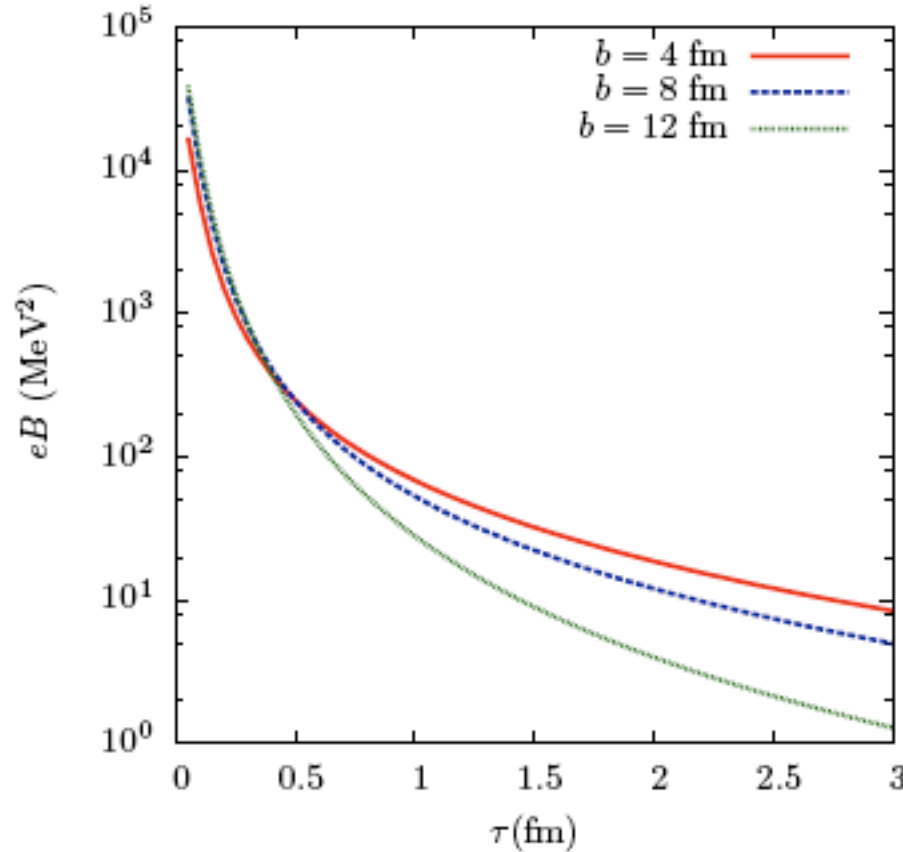
Initial spatial anisotropy



Final momentum anisotropy



Heavy ion collisions as a source of the strongest magnetic fields available in the Laboratory



DK, McLerran, Warringa,
Nucl Phys A803(2008)227

Fig. A.2. Magnetic field at the center of a gold-gold collision, for different impact parameters. Here the center of mass energy is 200 GeV per nucleon pair ($Y_0 = 5.4$).

Comparison of magnetic fields



The Earth's magnetic field

0.6 Gauss

A common, hand-held magnet

100 Gauss



The strongest steady magnetic fields achieved so far in the laboratory

4.5×10^5 Gauss

The strongest man-made fields ever achieved, if only briefly

10^7 Gauss



Typical surface, polar magnetic fields of radio pulsars

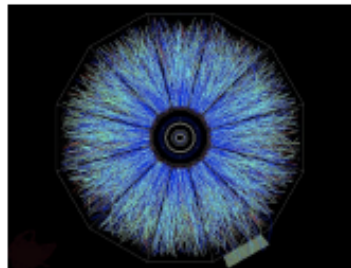
10^{13} Gauss

Surface field of Magnetars

10^{15} Gauss

<http://solomon.as.utexas.edu/~duncan/magnetar.html>

Heavy ion collisions: the strongest magnetic field ever achieved in the laboratory

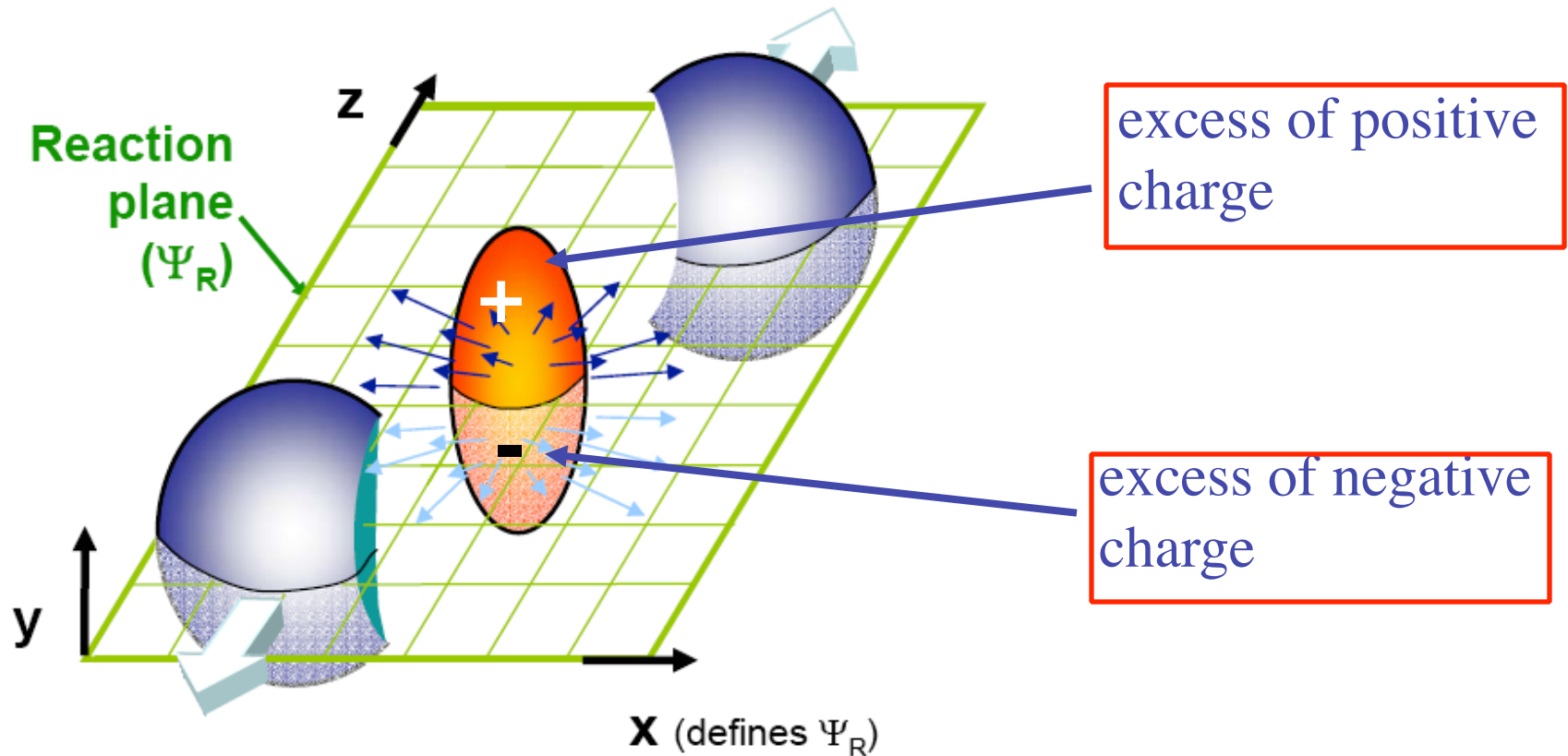


Off central Gold-Gold Collisions at 100 GeV per nucleon

$$eB(\tau=0.2 \text{ fm}) = 10^3 \sim 10^4 \text{ MeV}^2 \sim 10^{17} \text{ Gauss}$$

Charge asymmetry w.r.t. reaction plane as a signature of chirality imbalance

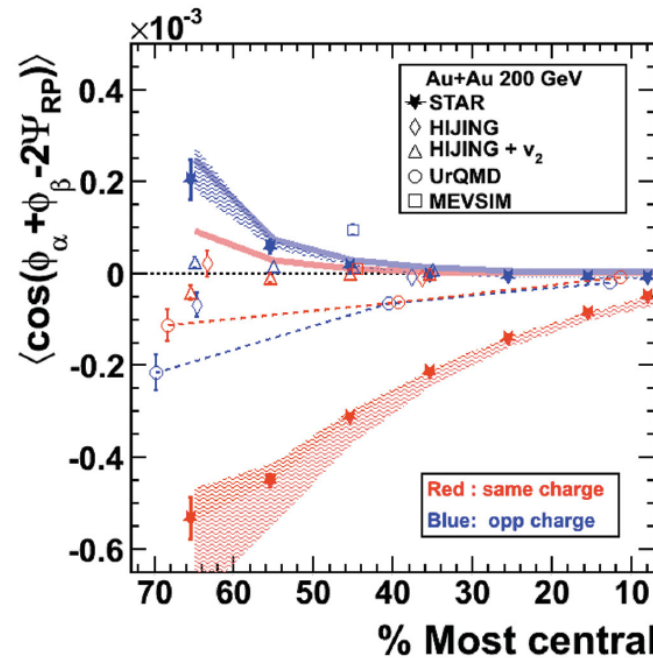
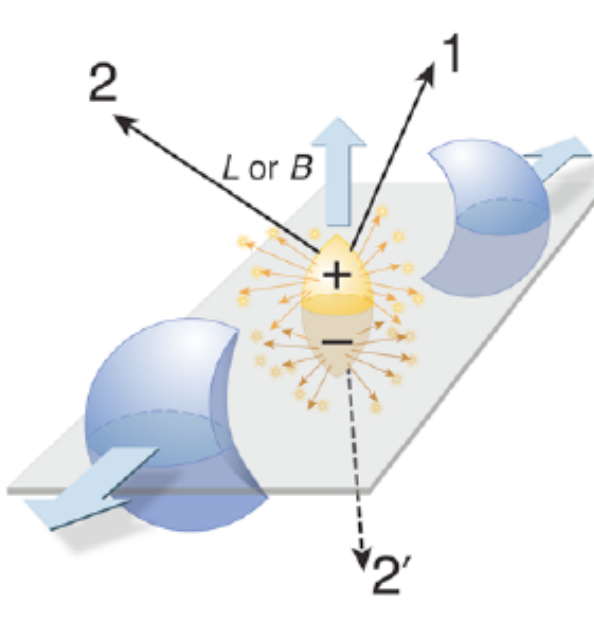
Electric dipole moment due to chiral imbalance





Azimuthal Charged-Particle Correlations and Possible Local Strong Parity Violation

(STAR Collaboration)



S. Voloshin '04

$$\begin{aligned} \gamma &\equiv \langle \cos(\phi_\alpha + \phi_\beta - 2\Psi_{RP}) \rangle = \langle \cos \Delta\phi_\alpha \cos \Delta\phi_\beta \rangle - \langle \sin \Delta\phi_\alpha \sin \Delta\phi_\beta \rangle \\ &= [\langle v_{1,\alpha} v_{1,\beta} \rangle + B_{IN}] - [\langle a_\alpha a_\beta \rangle + B_{OUT}] \approx -\langle a_\alpha a_\beta \rangle + [B_{IN} - B_{OUT}], \end{aligned}$$

NB: P-even quantity (strength of P-odd fluctuations)

– subject to large background contributions

Observation of charge-dependent azimuthal correlations in pPb collisions and its implication for the search for the chiral magnetic effect



The CMS Collaboration*

arxiv:1610.00263
October 2, 2016

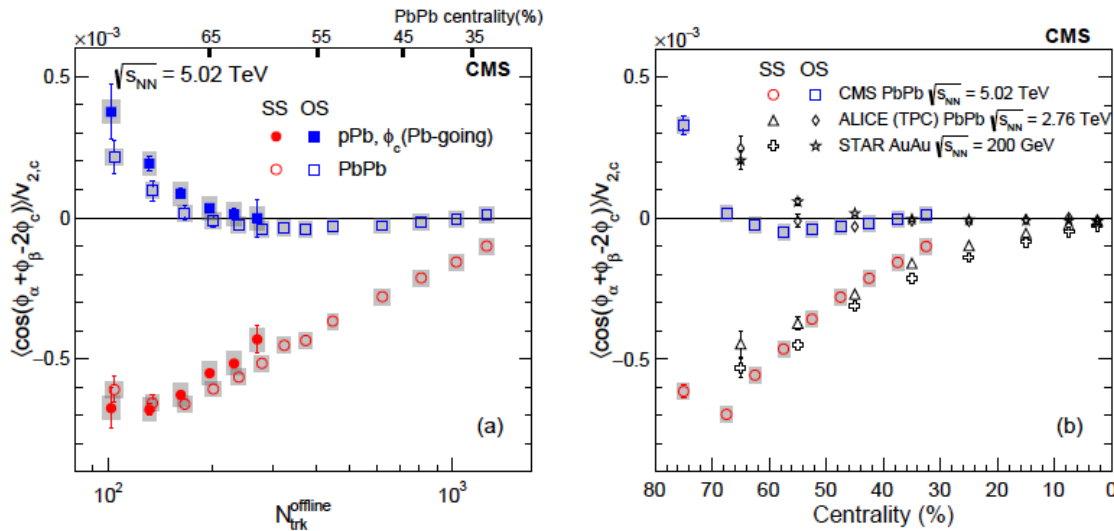


Figure 2: In (a), the same sign (SS) and opposite sign (OS) three-particle correlator averaged over $|\eta_\alpha - \eta_\beta| < 1.6$ as a function of $N_{\text{trk}}^{\text{offline}}$ in pPb and PbPb collisions at $\sqrt{s_{\text{NN}}} = 5.02$ TeV are shown. In (b), the same correlation as a function of centrality is presented in PbPb collisions at $\sqrt{s_{\text{NN}}} = 5.02$ TeV from CMS, at $\sqrt{s_{\text{NN}}} = 2.76$ TeV from ALICE, and in AuAu collisions at $\sqrt{s_{\text{NN}}} = 0.2$ TeV from STAR. Statistical and systematic uncertainties are indicated by the error bars and shaded regions, respectively.

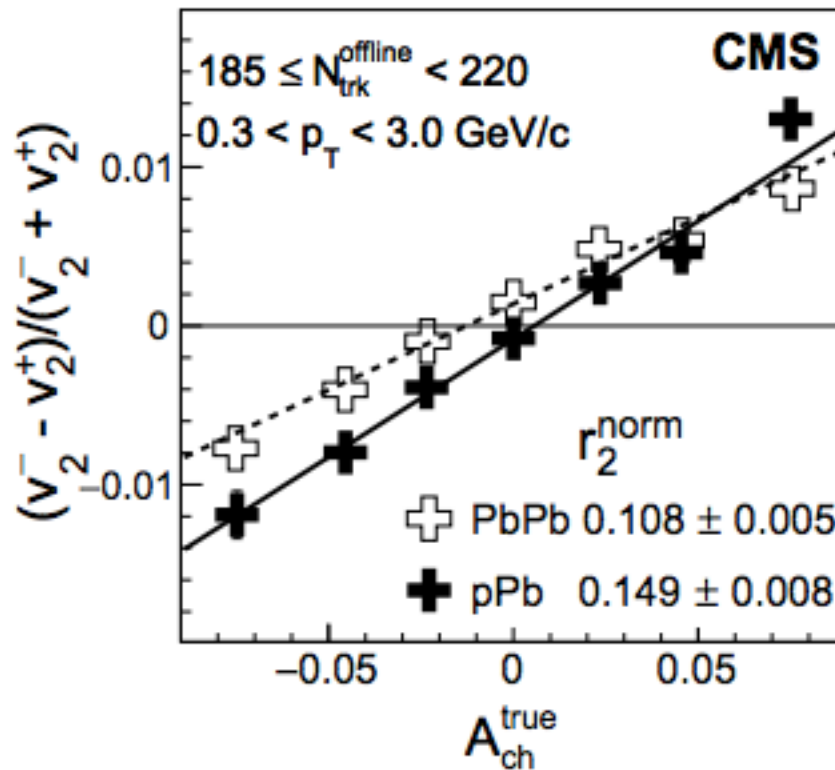
Background everywhere?
(dAu at RHIC!)

Magnetic field in pA?

Challenges to the chiral magnetic wave using charge-dependent azimuthal anisotropies in pPb and PbPb collisions at $\sqrt{s_{NN}} = 5.02$ TeV

The CMS Collaboration*

arXiv:1708.08901



Important data that challenges all existing theoretical models!

Is there a way to get a conclusive answer?

Chiral Magnetic Effect Task Force Report

Vladimir Skokov (co-chair),^{1,*} Paul Sorensen (co-chair),^{2,†} Volker Koch,³
Soeren Schlichting,² Jim Thomas,³ Sergei Voloshin,⁴ Gang Wang,⁵ and Ho-Ung Yee^{6,1}

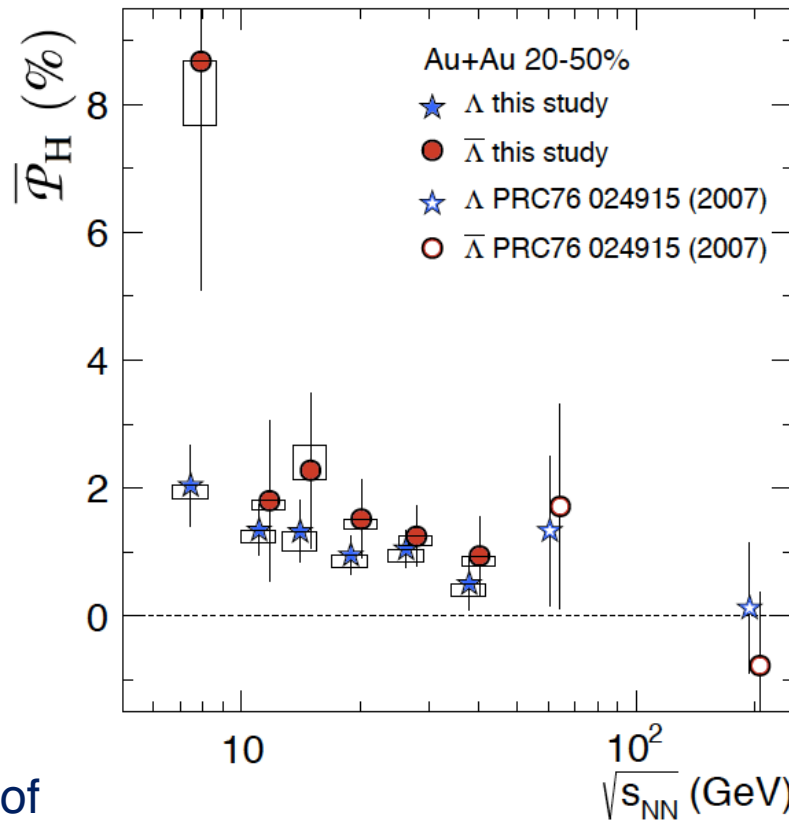
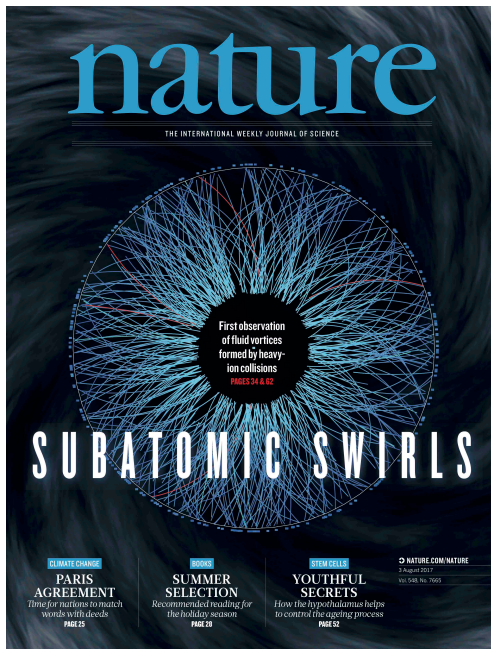
arxiv:1608.00982

The unique identification of the chiral magnetic effect in heavy-ion collisions would represent one of the highlights of the RHIC physics program and would provide a lasting legacy for the field. The current plan for completing the RHIC mission envisions a second phase of RHIC. We have specifically investigated the case for colliding nuclear isobars (nuclei with the same mass but different charge) and find the case compelling. We recommend that a program of nuclear isobar collisions to isolate the chiral magnetic effect from background sources be placed as a high priority item in the strategy for completing the RHIC mission.

Approved dedicated Spring 2018 CME run at RHIC with Zr (Z=40), Ru (Z=44) isobars – a clear, “yes or no” answer

The effect of vorticity: Λ polarization

STAR Coll., Nature 2017



The vorticity has to survive till hadronization.

The difference in the polarization of Λ and anti- Λ ?

Hint at magnetic field $B \sim 0.01 (M_\pi)^2$ at hadronization

e.g. F.Beccatini et al, arXiv:1610.02506, PRC'17

Vortical susceptibility of QCD matter:

$$\langle \sigma_z \rangle = \frac{\langle \bar{\Psi} \sigma_{xy} \gamma_5 \Psi \rangle}{\langle \bar{\Psi} \Psi \rangle} = \frac{N_c}{\pi^2 f_\pi^2} \mu \Omega_z$$

A.Aristova, D.Frenklakh,
A.Gorsky, DK, 1606.05882; JHEP

Chiral fermions in Dirac & Weyl semimetals



SOVIET PHYSICS JETP

VOLUME 32, NUMBER 4

APRIL, 1971

POSSIBLE EXISTENCE OF SUBSTANCES INTERMEDIATE BETWEEN METALS AND DIELECTRICS

A. A. ABRIKOSOV and S. D. BENESLAVSKIĬ

L. D. Landau Institute of Theoretical Physics

Submitted April 13, 1970

Zh. Eksp. Teor. Fiz. 59, 1280—1298 (October, 1970)

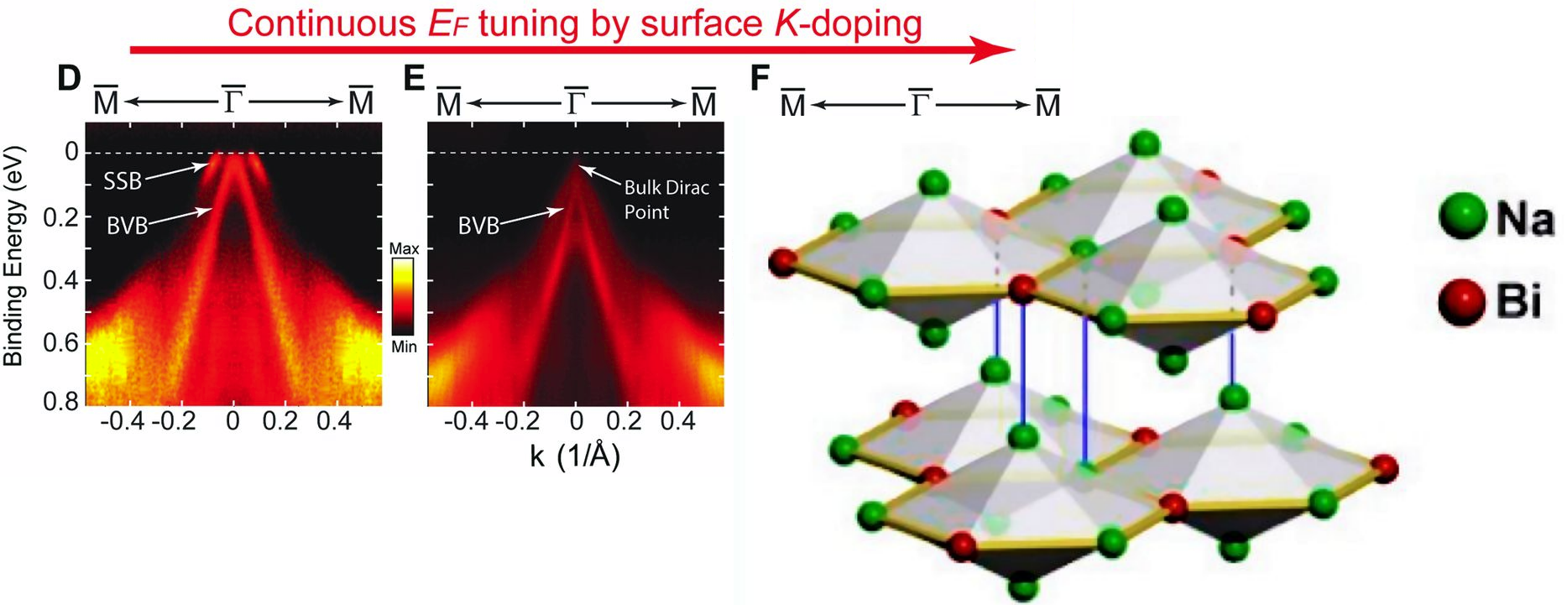
The question of the possible existence of substances having an electron spectrum without any energy gap and, at the same time, not possessing a Fermi surface is investigated. First of all the question of the possibility of contact of the conduction band and the valence band at a single point is investigated within the framework of the one-electron problem. It is shown that the symmetry conditions for the crystal admit of such a possibility. A complete investigation is carried out for points in reciprocal lattice space with a little group which is equivalent to a point group, and an example of a more complicated little group is considered. It is shown that in the neighborhood of the point of contact the spectrum may be linear as well as quadratic.



Scientific Background on the Nobel Prize in Physics 2016

TOPOLOGICAL PHASE TRANSITIONS AND TOPOLOGICAL PHASES OF MATTER

The discovery of Dirac and Weyl semimetals – 3D chiral materials



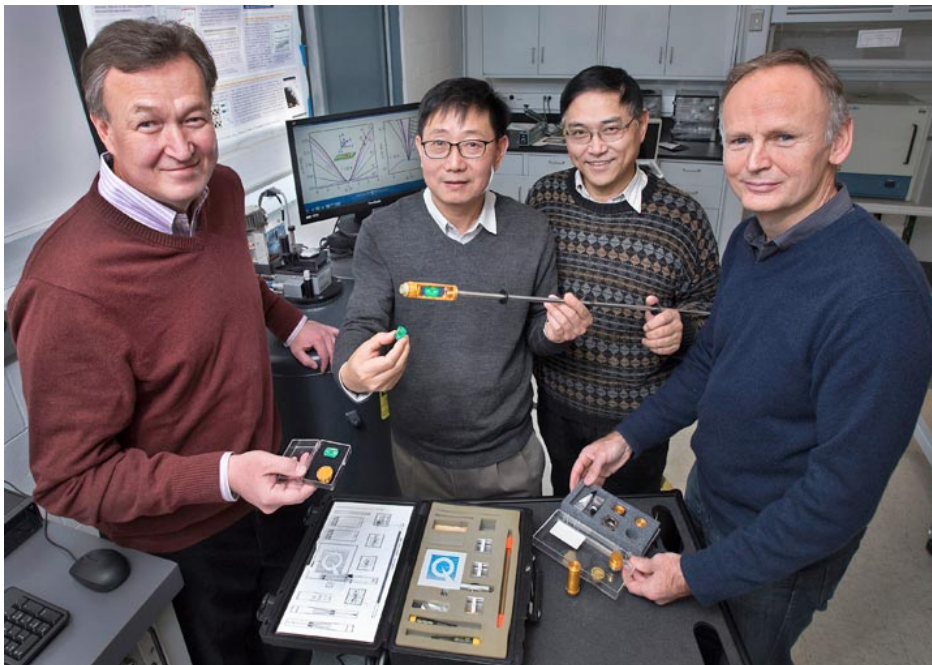
Z.K.Liu et al., Science 343 p.864 (Feb 21, 2014)

CME in condensed matter:

Observation of the chiral magnetic effect in ZrTe_5

Qiang Li,¹ Dmitri E. Kharzeev,^{2,3} Cheng Zhang,¹ Yuan Huang,⁴ I. Pletikosić,^{1,5}
A. V. Fedorov,⁶ R. D. Zhong,¹ J. A. Schneeloch,¹ G. D. Gu,¹ and T. Valla¹

BNL - Stony Brook - Princeton - Berkeley



Nature Phys.
12 (2016) 550

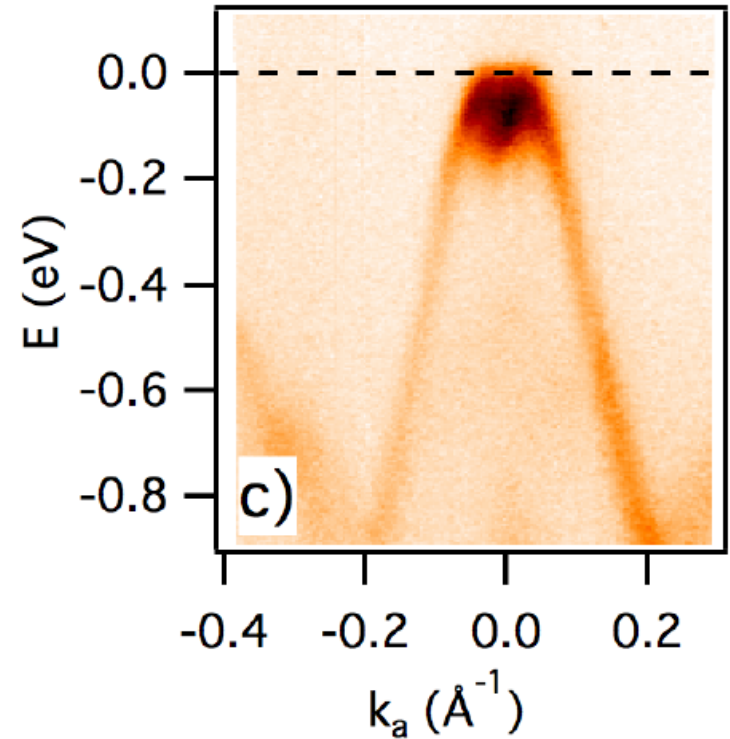
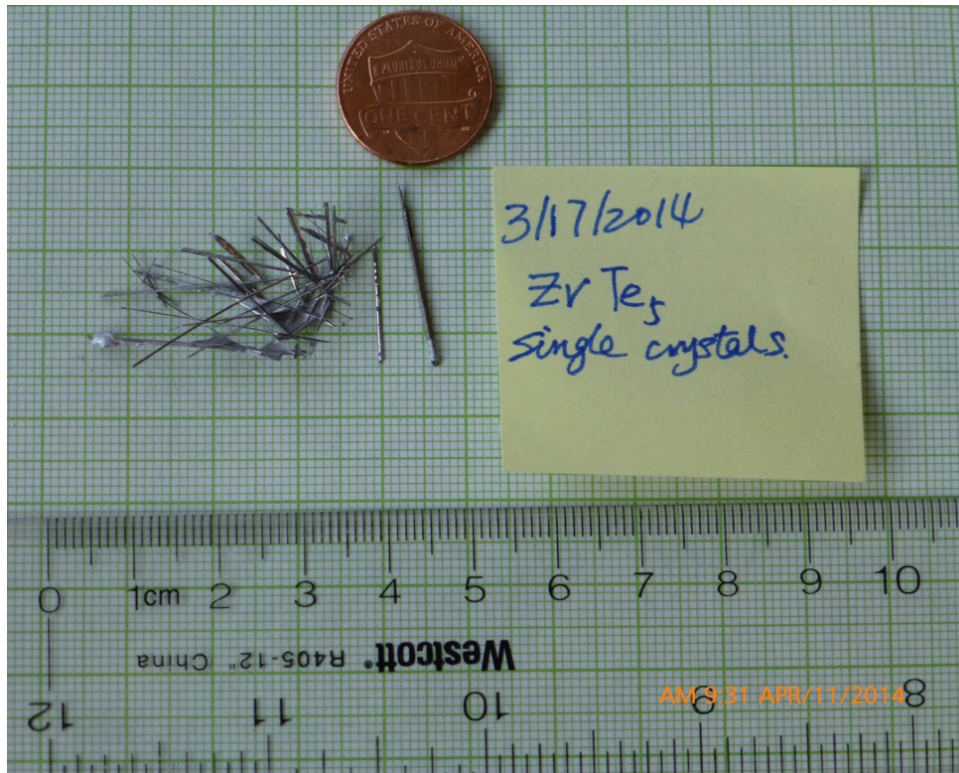


DIRAC SEMIMETALS
Chiral magnetic effect observed

arXiv:1412.6543 [cond-mat.str-el]

Observation of the chiral magnetic effect in ZrTe_5

Qiang Li,¹ Dmitri E. Kharzeev,^{2,3} Cheng Zhang,¹ Yuan Huang,⁴ I. Pletikosić,^{1,5}
A. V. Fedorov,⁶ R. D. Zhong,¹ J. A. Schneeloch,¹ G. D. Gu,¹ and T. Valla¹



arXiv:1412.6543 (December 2014); Nature Physics **12**, 550 (2016)

Observation of the chiral magnetic effect in ZrTe_5

Qiang Li,¹ Dmitri E. Kharzeev,^{2,3} Cheng Zhang,¹ Yuan Huang,⁴ I. Pletikosić,^{1,5}
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Put the crystal in parallel $\mathbf{E}$, $\mathbf{B}$ fields – the anomaly generates chiral charge:

$$\frac{d\rho_5}{dt} = \frac{e^2}{4\pi^2\hbar^2c} \vec{E} \cdot \vec{B} - \frac{\rho_5}{\tau_V}.$$

and thus the chiral chemical potential:

$$\mu_5 = \frac{3}{4} \frac{v^3}{\pi^2} \frac{e^2}{\hbar^2c} \frac{\vec{E} \cdot \vec{B}}{T^2 + \frac{\mu^2}{\pi^2}} \tau_V.$$

Observation of the chiral magnetic effect in ZrTe_5

Qiang Li,¹ Dmitri E. Kharzeev,^{2,3} Cheng Zhang,¹ Yuan Huang,⁴ I. Pletikosić,^{1,5}
A. V. Fedorov,⁶ R. D. Zhong,¹ J. A. Schneeloch,¹ G. D. Gu,¹ and T. Valla¹

so that there is a chiral magnetic current:

$$\vec{J}_{\text{CME}} = \frac{e^2}{2\pi^2} \mu_5 \vec{B}.$$

resulting in the quadratic dependence of CME conductivity on B:

$$J_{\text{CME}}^i = \frac{e^2}{\pi\hbar} \frac{3}{8} \frac{e^2}{\hbar c} \frac{v^3}{\pi^3} \frac{\tau_V}{T^2 + \frac{\mu^2}{\pi^2}} B^i B^k E^k \equiv \sigma_{\text{CME}}^{ik} E^k.$$

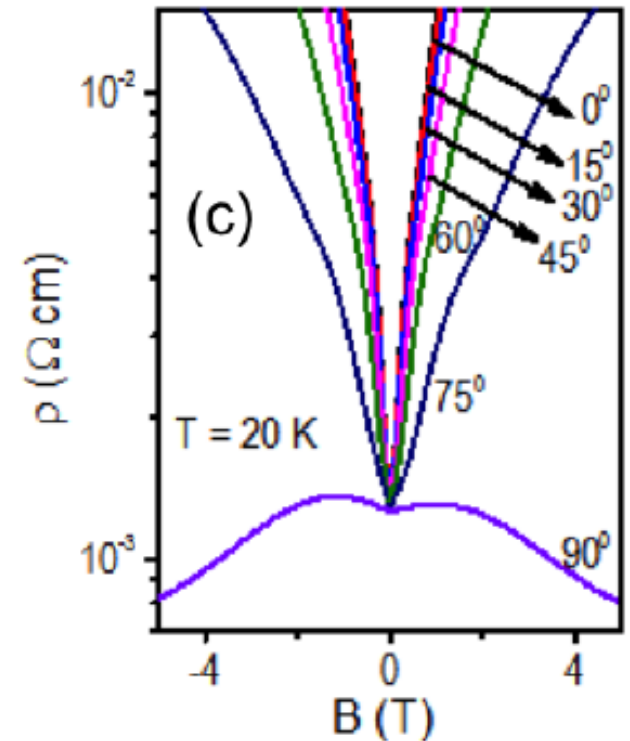
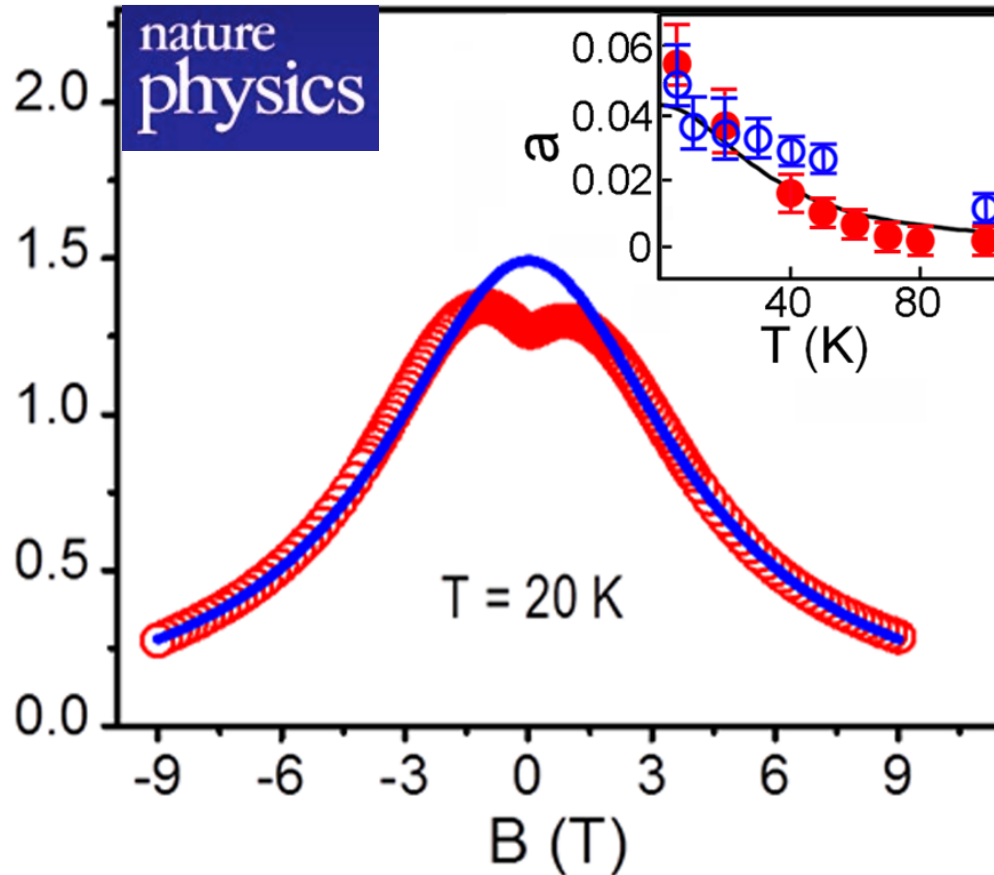
adding the Ohmic one – negative magnetoresistance

Chiral Magnetic Effect Generates Quantum Current

Separating left- and right-handed particles in a semi-metallic material produces anomalously high conductivity

February 8, 2016

Nature Physics **12**, 550 (2016)

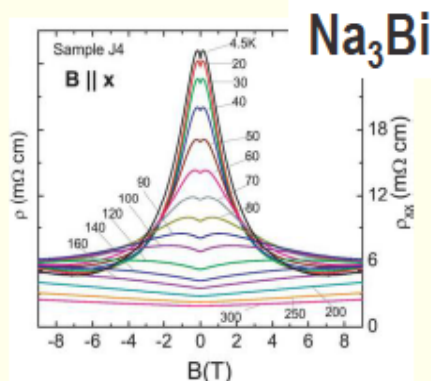


Qiang Li's Distinguished CQM lecture at Simons Center, Feb 19, 2016
on video:

http://scgp.stonybrook.edu/video_portal/video.php?id=2458

Chiral magnetic effect in Dirac/Weyl semimetals

Dirac semimetals:

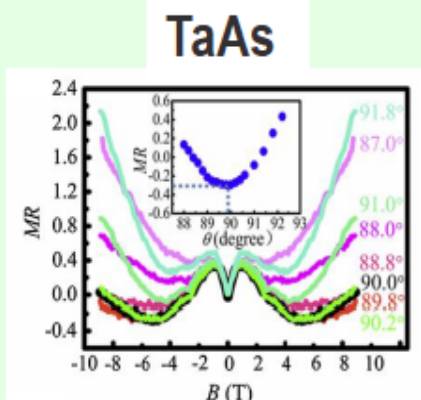


ZrTe₅ - Q. Li, D. Kharzeev, et al (BNL and Stony Brook Univ.)
arXiv:[1412.6543](#); doi:10.1038/NPHYS3648

Na₃Bi - J. Xiong, N. P. Ong et al (Princeton Univ.)
arxiv:[1503.08179](#); Science 350:413,2015

Cd₃As₂ - C. Li et al (Peking Univ. China)
arxiv:[1504.07398](#); Nature Commun. 6, 10137 (2015).

Weyl semimetals



TaAs - X. Huang et al (IOP, China)
arxiv:[1503.01304](#); Phys. Rev. X 5, 031023

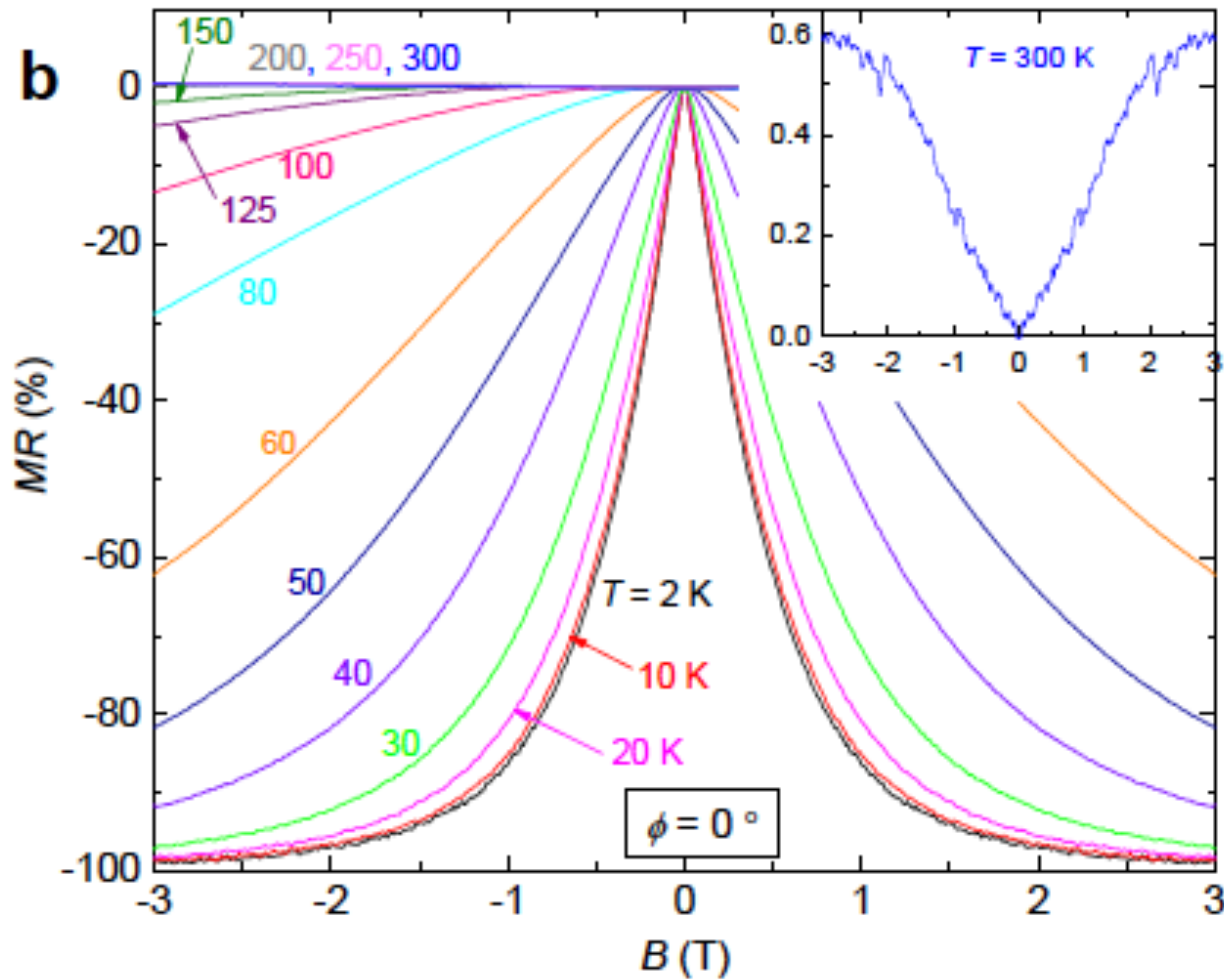
NbAs - X. Yang et al (Zhejiang Univ. China)
arxiv:[1506.02283](#)

NbP - Z. Wang et al (Zhejiang Univ. China)
arxiv:[1504.07398](#)

TaP - Shekhar, C. Felser, B. Yang et al (MPI-Dresden)
arxiv:[1506.06577](#)

Bi_{1-x}Sb_x at x ≈ 0.03 - Kim, et al. "Dirac versus Weyl Fermions in Topological Insulators: Adler-Bell-Jackiw Anomaly in Transport Phenomena. Phys. Rev. Lett., 111, 246603 (2013).

Negative MR in TaAs₂



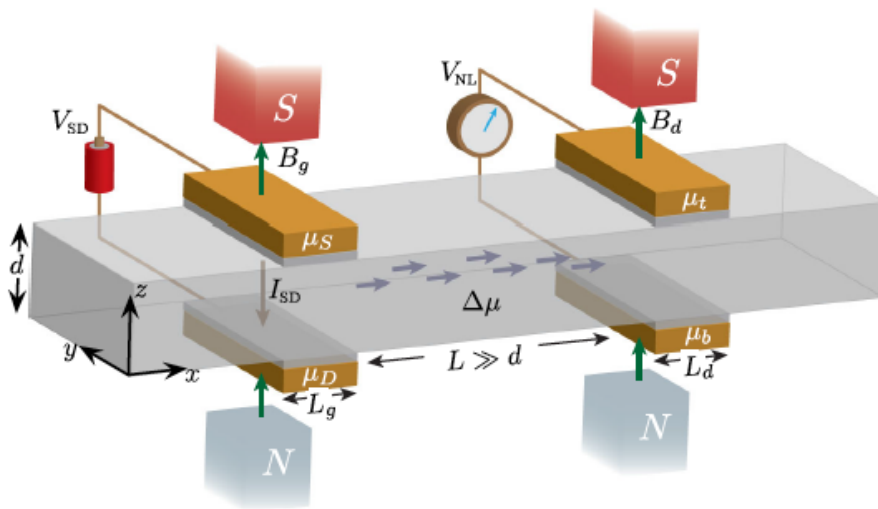
Y.Luo et al, 1601.05524

Towards the room temperature CME

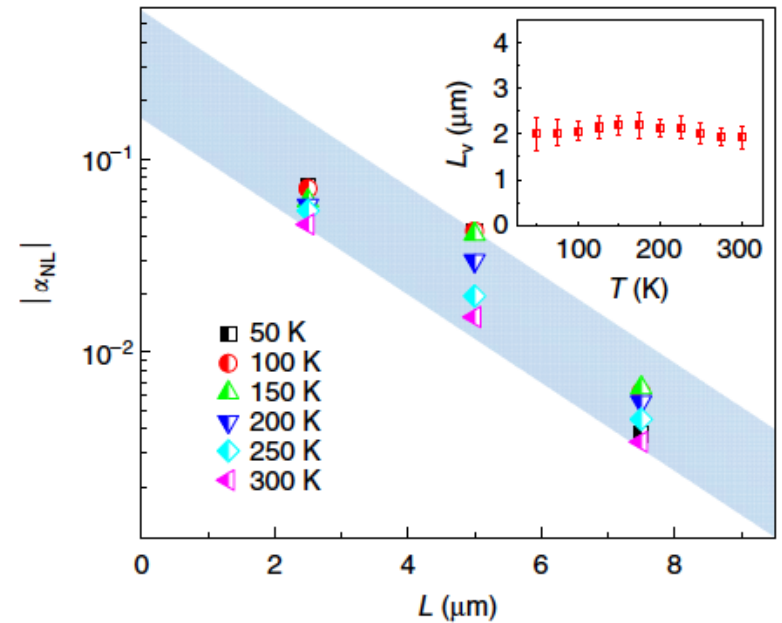
Nonlocal chiral transport

C.Zhang et al, Nature Comm.'17
DOI: 10.1038/ncomms13741

S.Parameswaran, T.Grover,
D.Abanin, D.Pesin, A.Vishwanath
PRX4, 031035 (2014)



$$|V_{NL}(x)| \propto V_{SD} e^{-\frac{L}{L_v}}$$



CME as a new type of superconductivity

London theory of superconductors, '35:

$$\vec{J} = -\lambda^{-2} \vec{A} \quad \nabla \cdot \vec{A} = 0$$

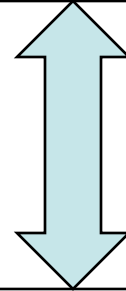
$$\vec{E} = -\dot{\vec{A}}$$

CME:

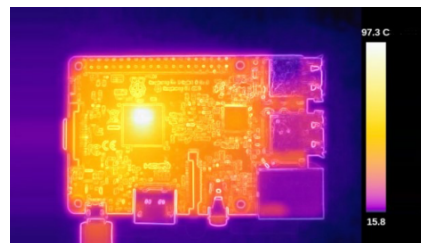
$$\vec{J} \sim \mu_5 \vec{B}$$

for $\vec{E} \parallel \vec{B}$

$$\vec{E} = \lambda^2 \dot{\vec{J}}$$



$$\vec{E} \sim B^{-2} \dot{\vec{J}}$$



Fritz and Heinz London

consider a micro-device of $O(\mu\text{m})$ size, so that Chirality is conserved; then

$$\mu_5 \sim \vec{E} \vec{B} t$$

superconducting current, tunable by magnetic field!

Chiral photonics

Faraday rotation due to surface states in $(\text{Bi}_{1-x}\text{Sb}_x)_2\text{Te}_3$ topological insulator

Y. M. Shao^{1,*}, K. W. Post,¹ J. S. Wu¹, S. Dai¹, A. J. Frenzel¹, A. R. Richardella², J. S. Lee²,
N. Samarth², M. M. Fogler¹, A. V. Balatsky^{3,4}, D. E. Kharzeev^{5,6} and D. N. Basov¹

¹*Physics Department, University of California-San Diego, La Jolla, California 92093, USA*

²*Department of Physics, The Pennsylvania State University, University Park, Pennsylvania 16802, USA*

³*Nordita, KTH Royal Institute of Technology and Stockholm University,
Roslagstullsbacken 23, SE-106 91 Stockholm, Sweden*

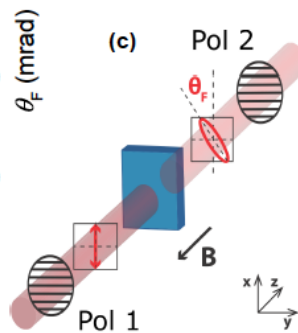
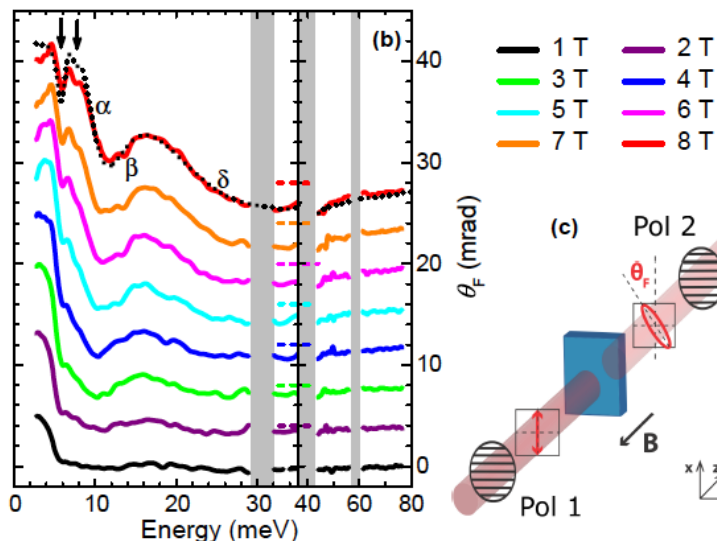
⁴*Institute for Materials Science, Los Alamos National Laboratory, Los Alamos, New Mexico 87545, USA*

⁵*Department of Physics and Astronomy, Stony Brook University, Stony Brook, New York 11794-3800, USA*

⁶*Department of Physics, Brookhaven National Laboratory, Upton, New York 11973, USA*

NANO LETTERS

Nano Letters, 2017



Response of surface states
grows linearly in B (chiral anomaly)

$$\vec{\nabla} \cdot \vec{E} = \rho + c\vec{P} \cdot \vec{B}$$

Rotation of light polarization on
axion domain walls in the Universe?
currents from time-dependent axion fields?

Detection of sub-MeV Dark Matter with Three-Dimensional Dirac Materials

Yonit Hochberg^{1,2}, Yonatan Kahn³, Mariangela Lisanti³, Kathryn M. Zurek^{4,5}, Adolfo G. Grushin^{6,7}, Roni Ilan⁸, Sinéad M. Griffin^{6,9}, Zhen-Fei Liu^{6,9}, Sophie F. Weber^{6,9}, and Jeffrey B. Neaton^{6,9,10,11}

arXiv:1708.08929

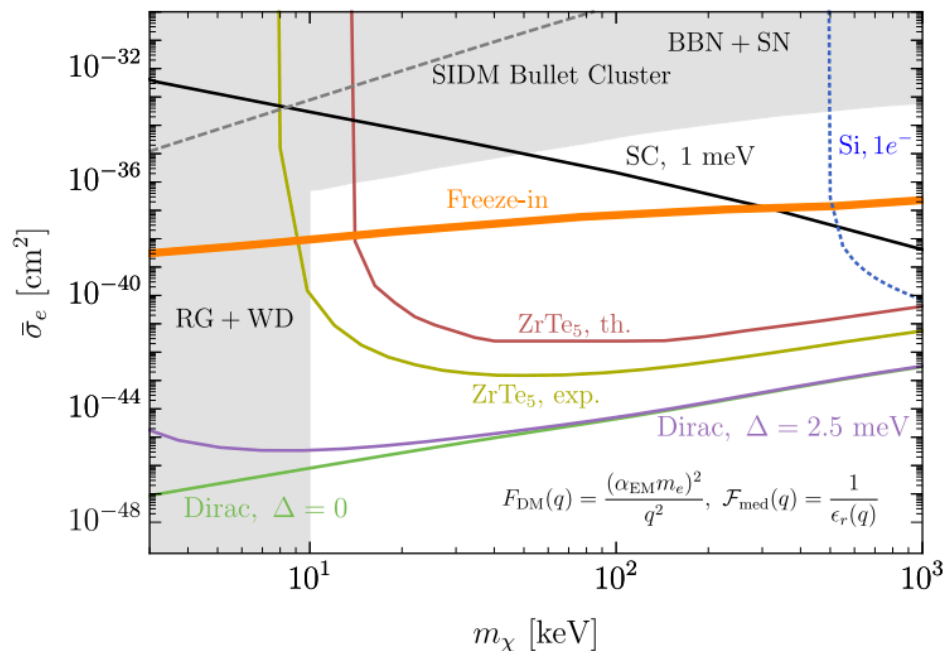
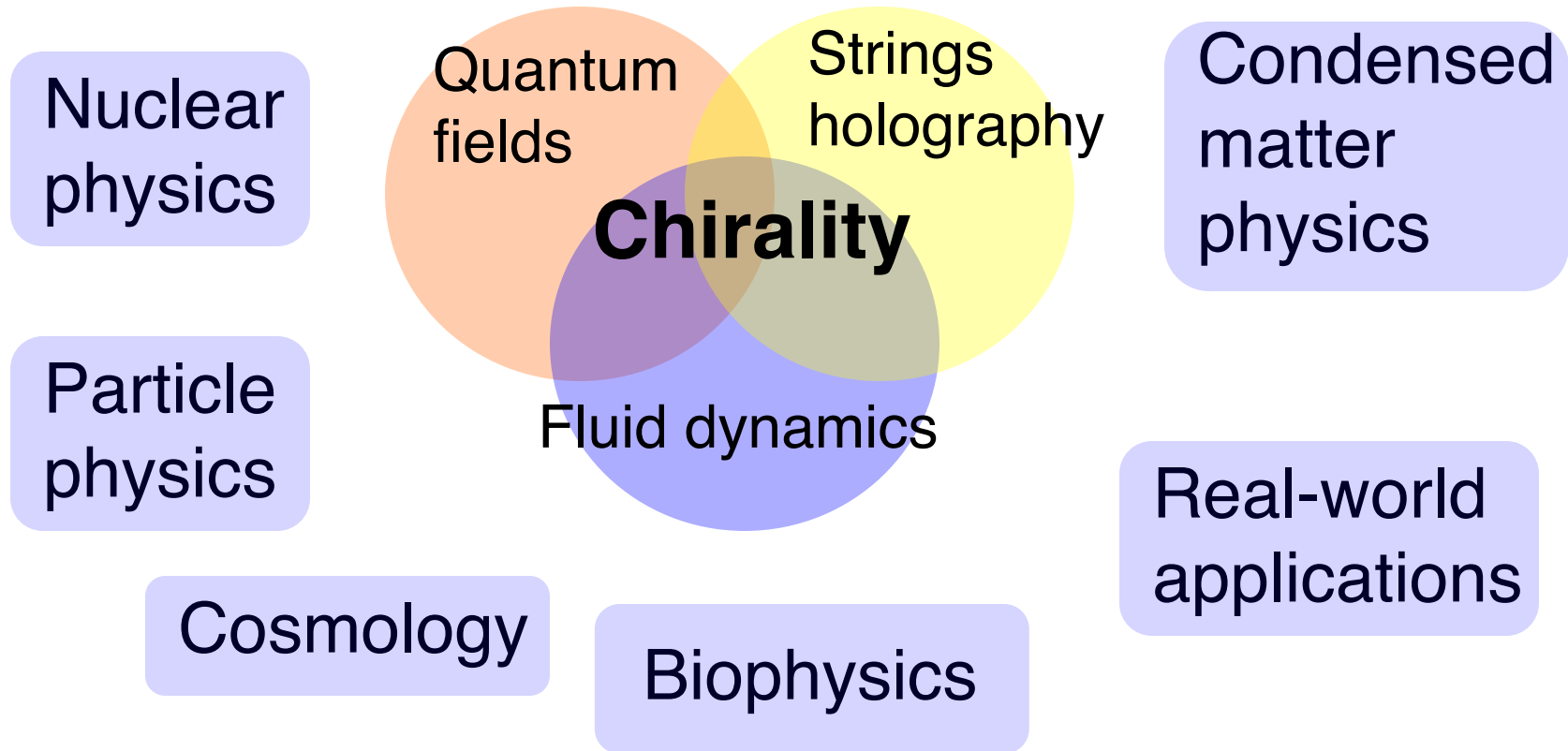


Figure 4: Projected reach of dark matter scattering in Dirac materials through a light kinetically mixed dark photon mediator with in-medium effects included. We show the expected background-free 95% C.L. sensitivity (3.0 events) that can be obtained with 1 kg-yr exposure. For the two

Summary



Reviews:

DK, K. Landsteiner, A. Schmitt, H.U.Yee (Eds),
“Strongly interacting matter in magnetic fields”,
Springer, 2013; arxiv:1211.6245

DK, “The chiral magnetic effect and anomaly-induced transport”,
Prog.Part.Nucl.Phys. 75 (2014) 133; arxiv: 1312.3348

DK, “Topology, magnetic field and strongly interacting matter”,
arxiv: 1501.01336; Ann. Rev. Nucl. Part. Science (2015)

DK, J.Liao, S.Voloshin, G.Wang, “Chiral magnetic and vortical effects
in high-energy nuclear collisions: A status report” Prog. Part. Nucl.
Phys. 88 (2016) 1