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Quantum Hall Effect in Vanishing Magnetic Fields

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Sandia is a multi-mission laboratory operated by Sandia Corporation, a Lockheed Martin Company, for the United States Department of Energy's National Nuclear Security Administration under contract DE-AC04-94AL85000.

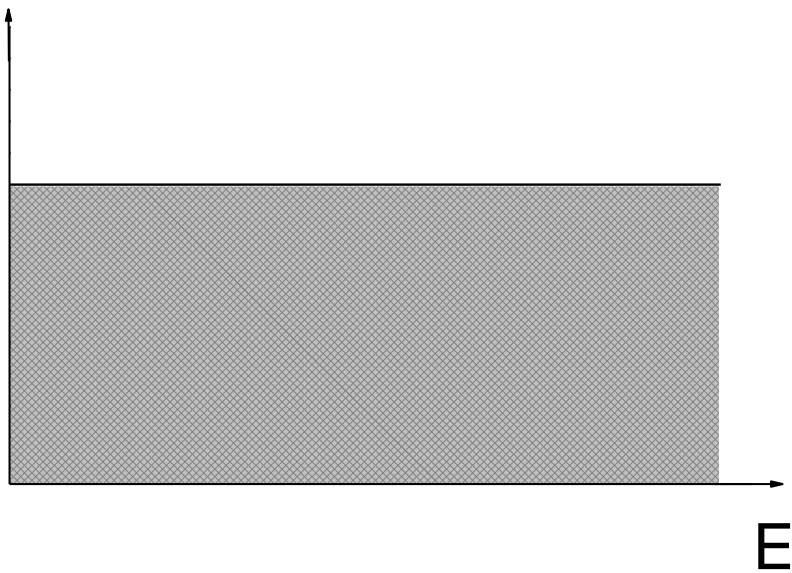


Part I: Anti-levitation of Landau levels in vanishing magnetic fields (Pan et al, PRB (2016))

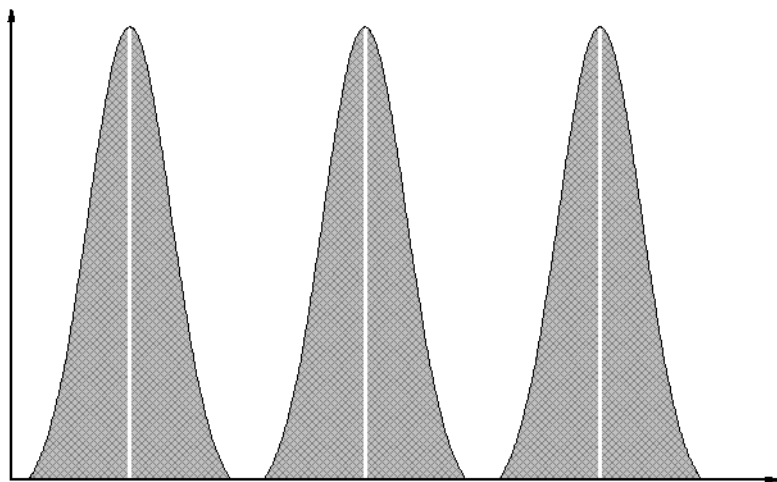
Part II: Collapse of spin splitting in the quantum Hall regime (Pan et al, PRB (2011))

part I outline

- Background
- Sample
 - HIGFET (**H**eterojunction **I**nsulated-**G**ate **F**ield-**E**ffect **T**ransistor)
- Results
 - Anti-levitation is observed at low Landau level fillings $\nu=4,5,6$.
 - This observation is in good agreement with a recent theoretical prediction (C. Wang et al, PRB **89**, 045314 (2014)).

$$\frac{dN}{d\varepsilon}$$


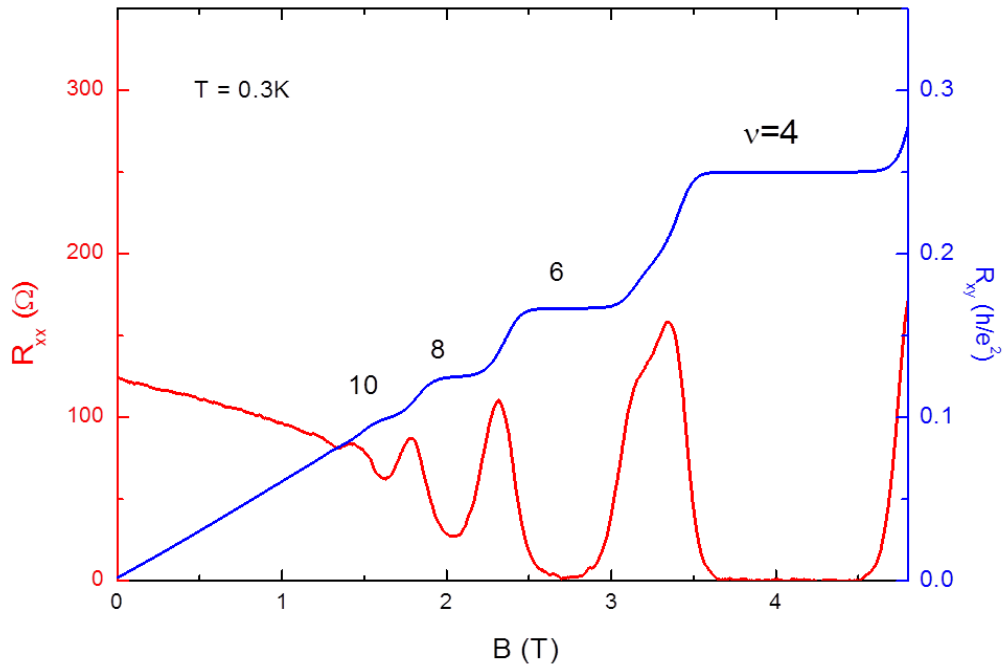
$$B = 0$$



$$B \neq 0$$

$$E = (N + 1/2)\hbar\omega_c$$

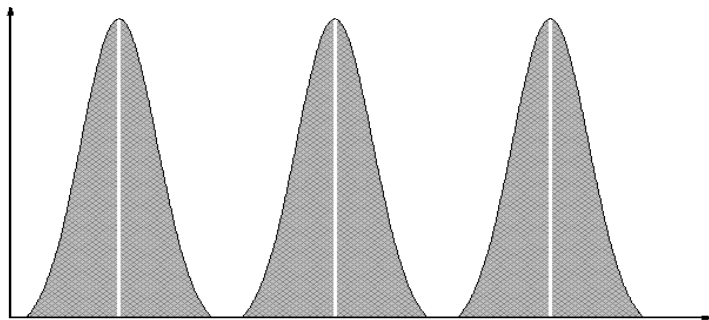
Integer quantum Hall effect



R_{xy} quantized

$$R_{xy} = \frac{h}{\nu e^2}$$

R_{xx} zero



ν – Landau level filling
 $\nu = nh/eB$ (n density)

So ugly and yet so precise



Resistance quantized to a few parts in 10^9

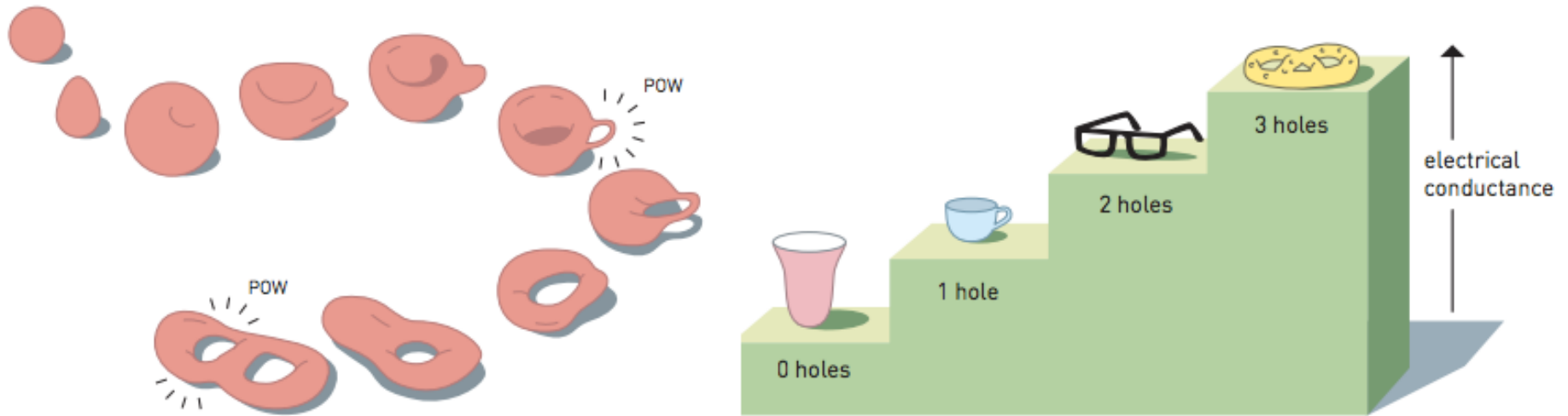


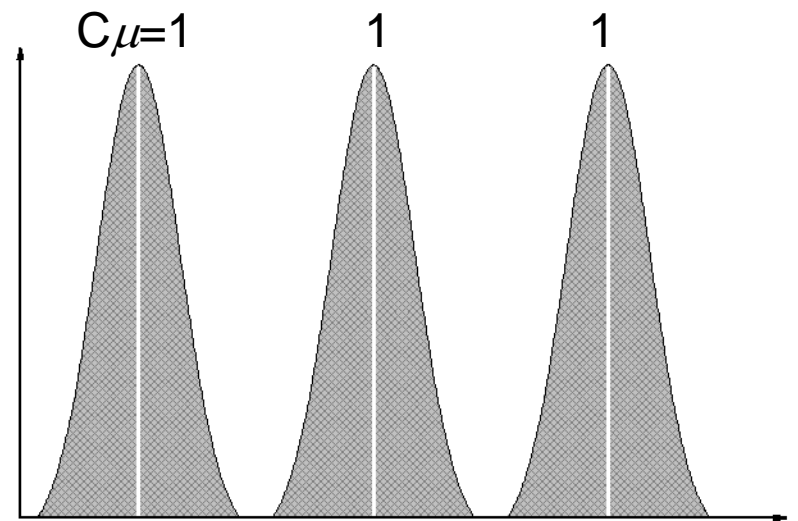
Fig 3. Topology. This branch of mathematics is interested in properties that change step-wise, like the number of holes in the above objects. Topology was the key to the Nobel Laureates' discoveries, and it explains why electrical conductivity inside thin layers changes in integer steps.

Chern number as a topological order parameter: TKNN formula

$$\begin{aligned} \sigma_{xy} &\propto \int_{\mathbf{k} \in \text{BZ}} d^2\mathbf{k} \sum_{\epsilon_\mu(\mathbf{k}) < \epsilon_F < \epsilon_\nu(\mathbf{k})} \frac{\langle u_\mu(\mathbf{k}) | \nabla_{\mathbf{k}} H}{\epsilon_\mu(\mathbf{k}) - \epsilon_\nu(\mathbf{k})} \\ &= \int_{\mathbf{k} \in \text{BZ}} d^2\mathbf{k} \sum_{\epsilon_\mu(\mathbf{k}) < \epsilon_F} \langle \nabla_{\mathbf{k}} u_\mu(\mathbf{k}) | \times | \nabla_{\mathbf{k}} u_\mu(\mathbf{k}) \rangle \end{aligned}$$

where $u_{\mu\mathbf{k}}(\mathbf{r})$ is the periodic part of a Bloch wave function

$$\left[\frac{1}{2m} (-i\hbar\nabla + \mathbf{p}) \right]$$

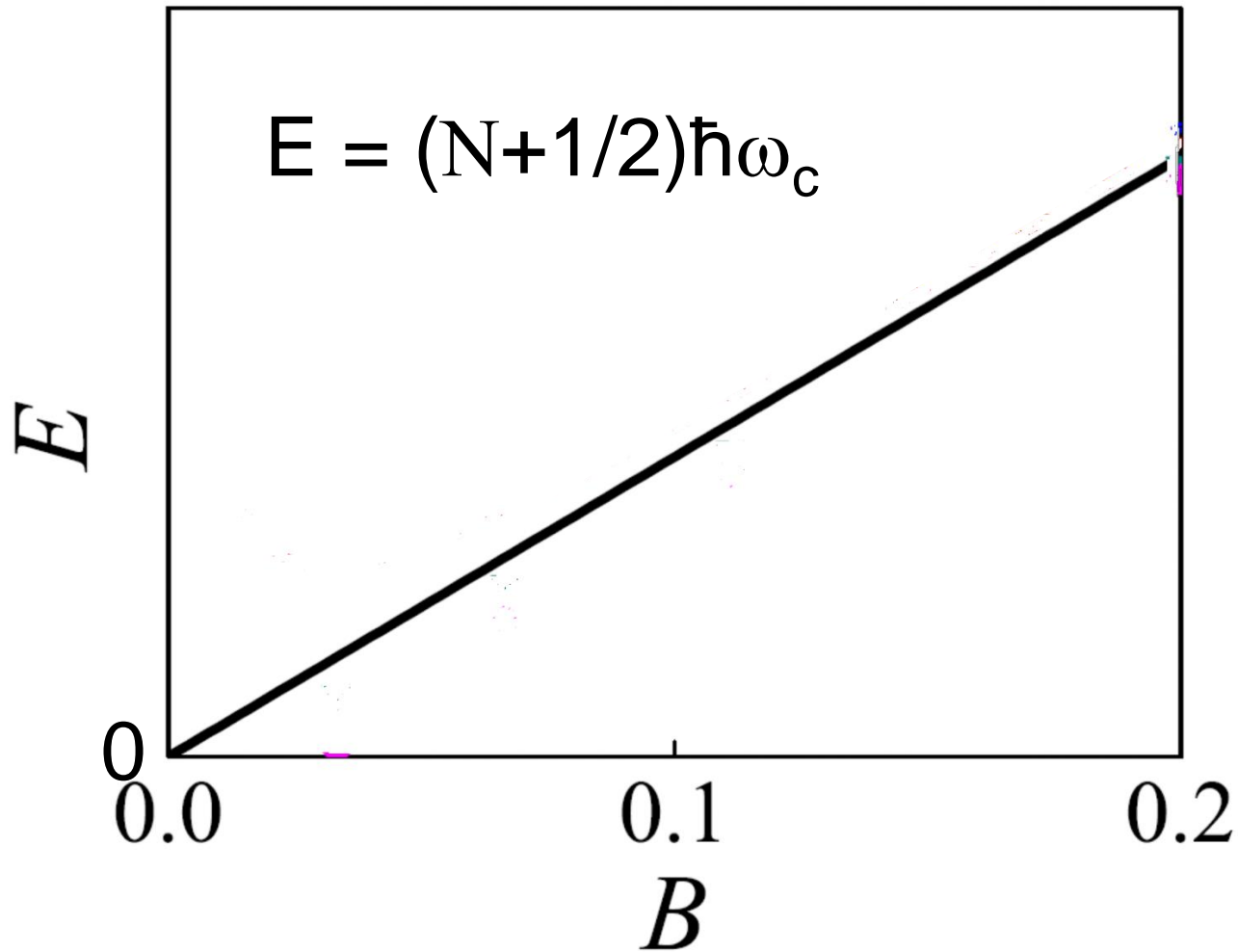


- This is the famous Thouless-Kohmoto-Nightingale-Chen topological invariant “order parameter” c_μ which is related to the Hall conductivity via $\sigma_{xy} = ne^2/h$.

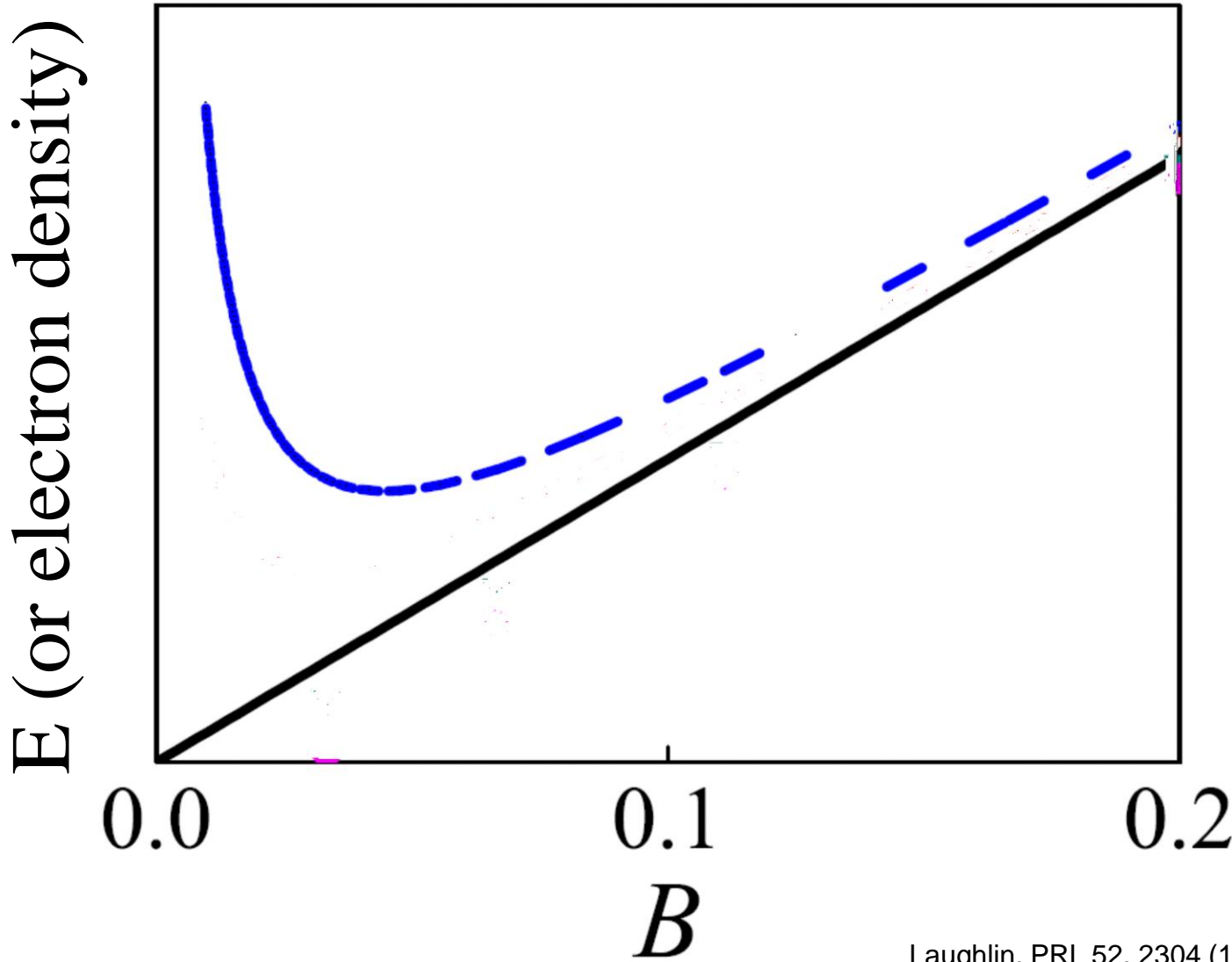
$$n = \sum_{\epsilon_\mu(\mathbf{k}) < \epsilon_F} c_\mu$$

$$c_\mu = \frac{i}{2\pi} \int_{\mathbf{k} \in \text{BZ}} d^2\mathbf{k} \langle \nabla_{\mathbf{k}} u_\mu(\mathbf{k}) | \times | \nabla_{\mathbf{k}} u_\mu(\mathbf{k}) \rangle \cdot \hat{z}$$

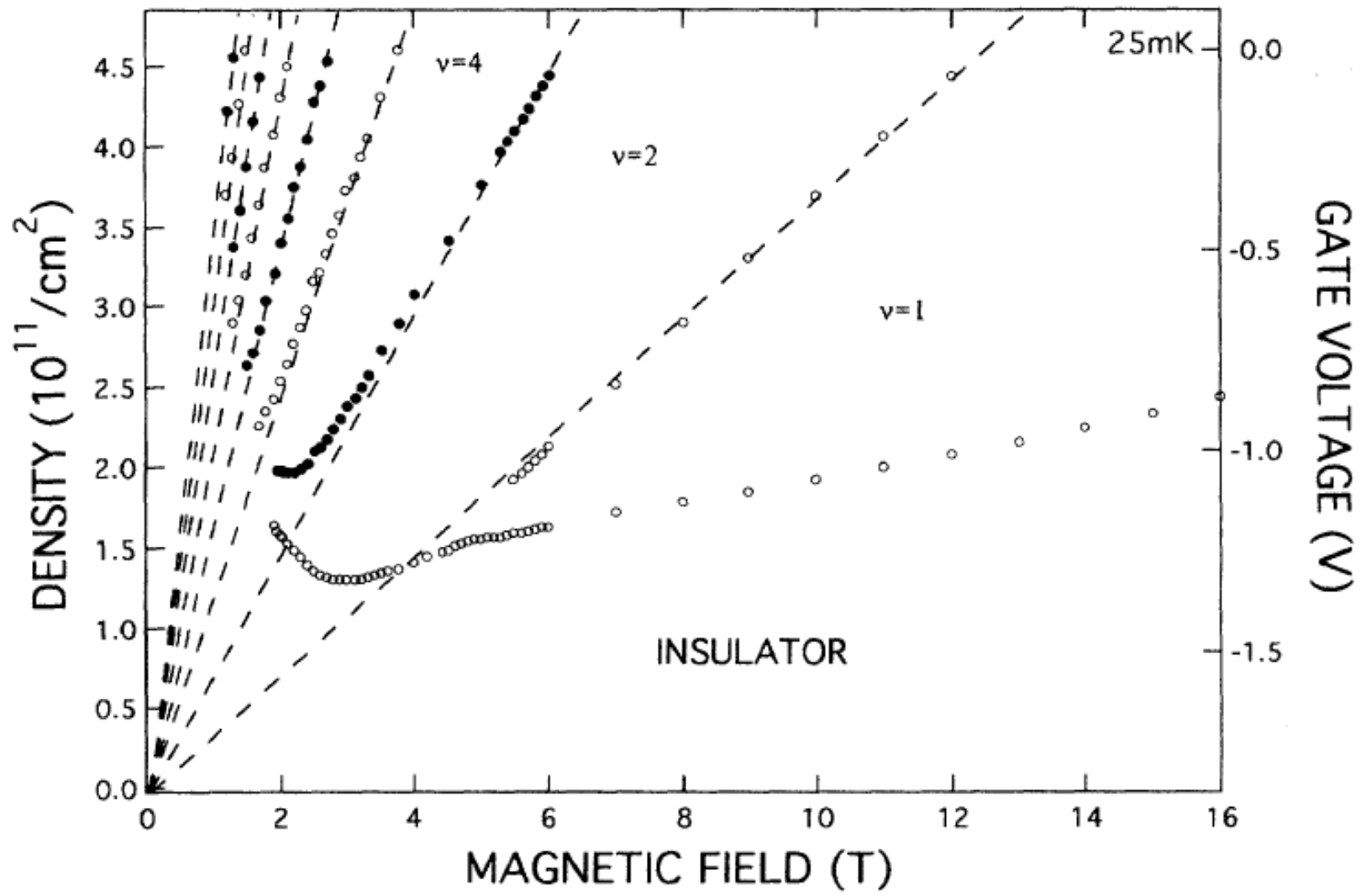
Chern number never disappears by itself



Floating of Landau levels in vanishing B field



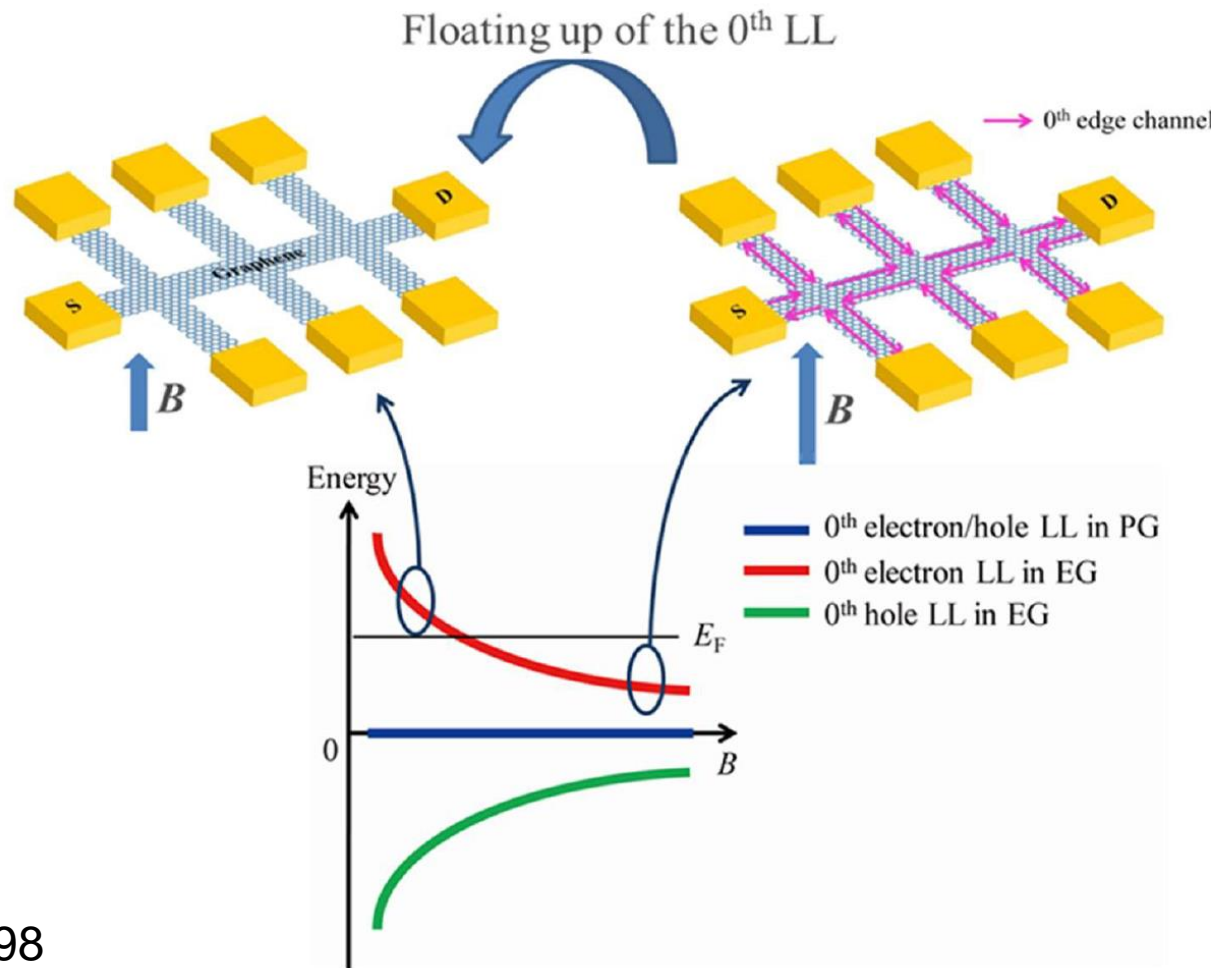
Laughlin, PRL 52, 2304 (1984).
Khmelnitskii, Phys. Lett. A 106, 182 (1984).



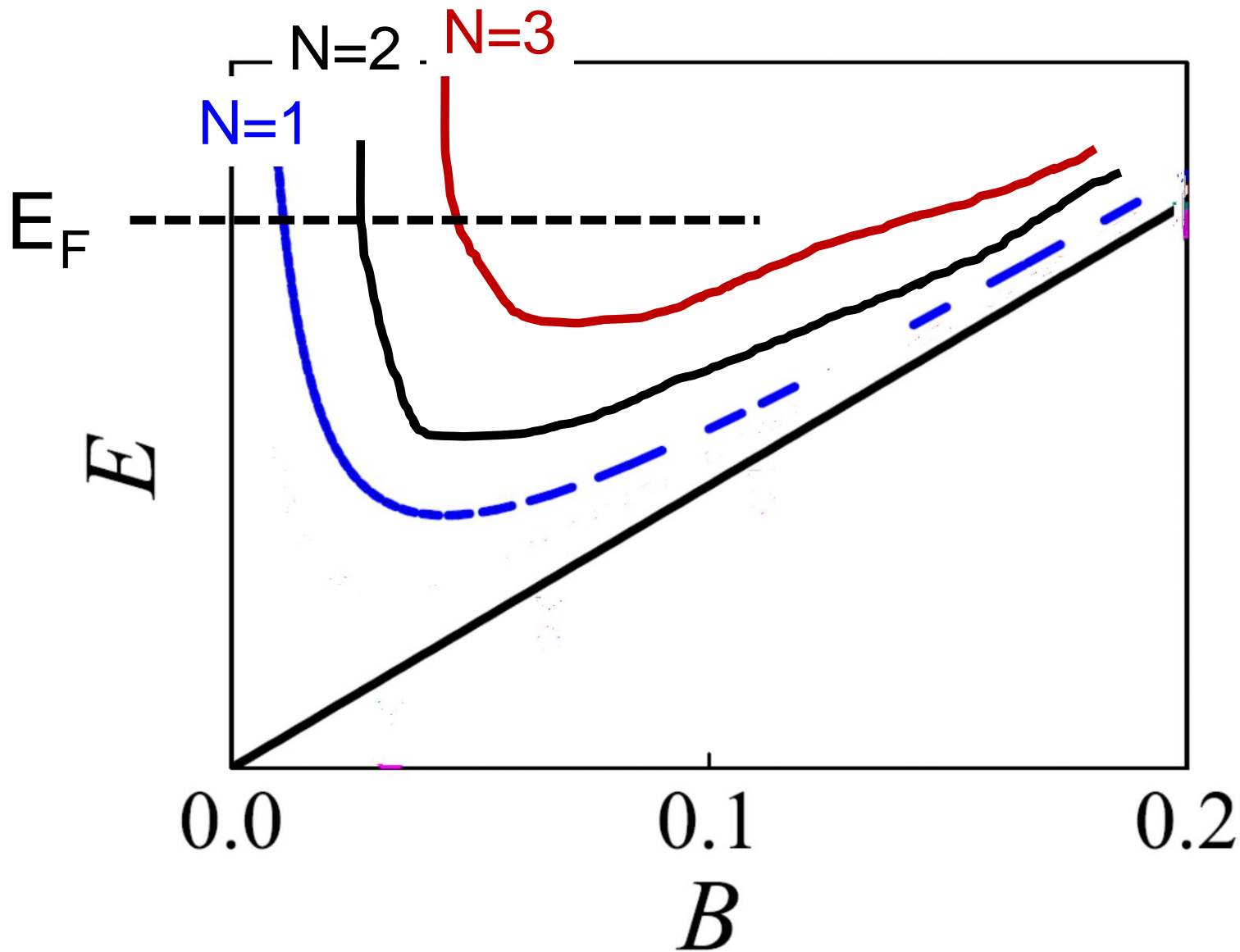
Glazman, Johnson, and Jiang PRL 74, 594 (1995)

Floating up of the zero-energy Landau level in monolayer epitaxial graphene

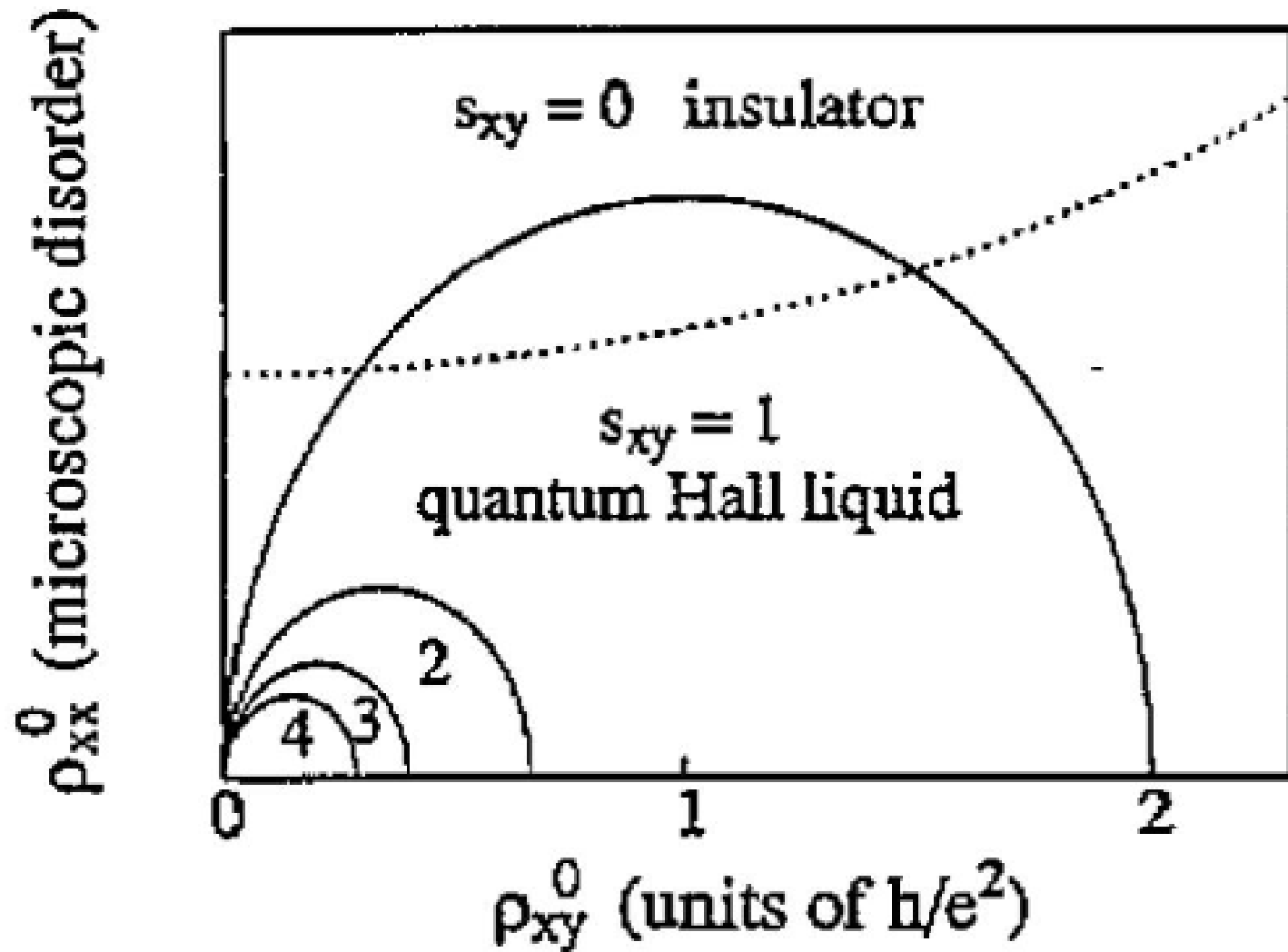
Lung-I Huang^{1,2}, Yanfei Yang^{1,3}, Randolph E. Elmquist¹,
Shun-Tsung Lo^{4,*}, Fan-Hung Liu⁴, and Chi-Te Liang^{2,4,*}



Only insulator to $N = 1$ transition allowed

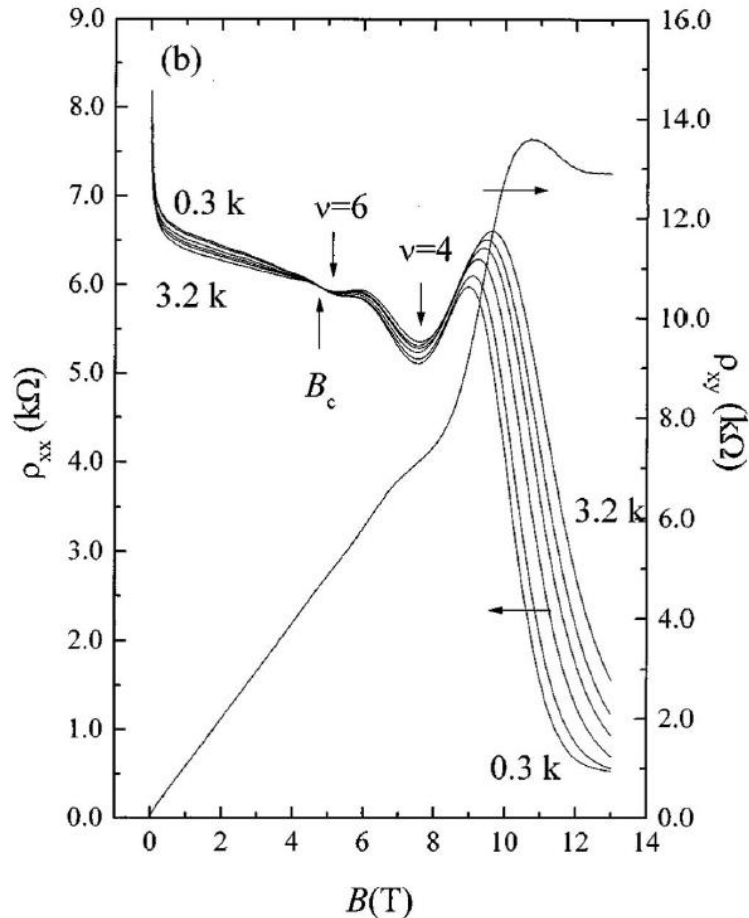


Global phase diagram



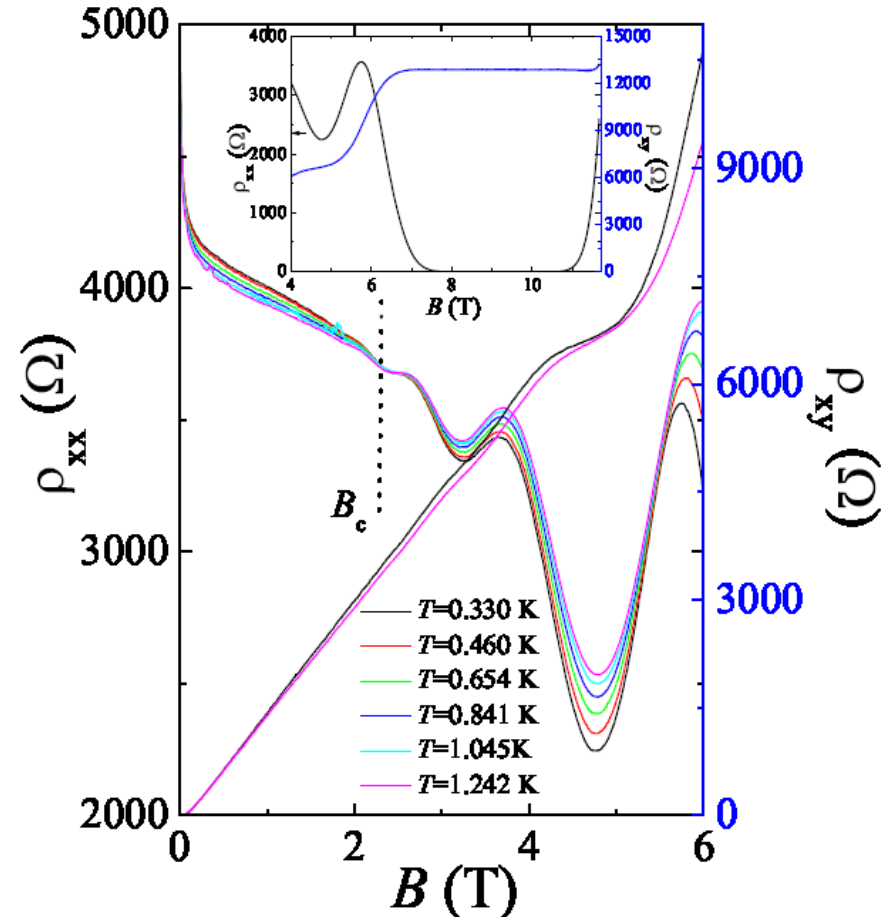
However, transition from insulator to high order quantum Hall states has been observed in experiments ...

Insulator to N=3 transition



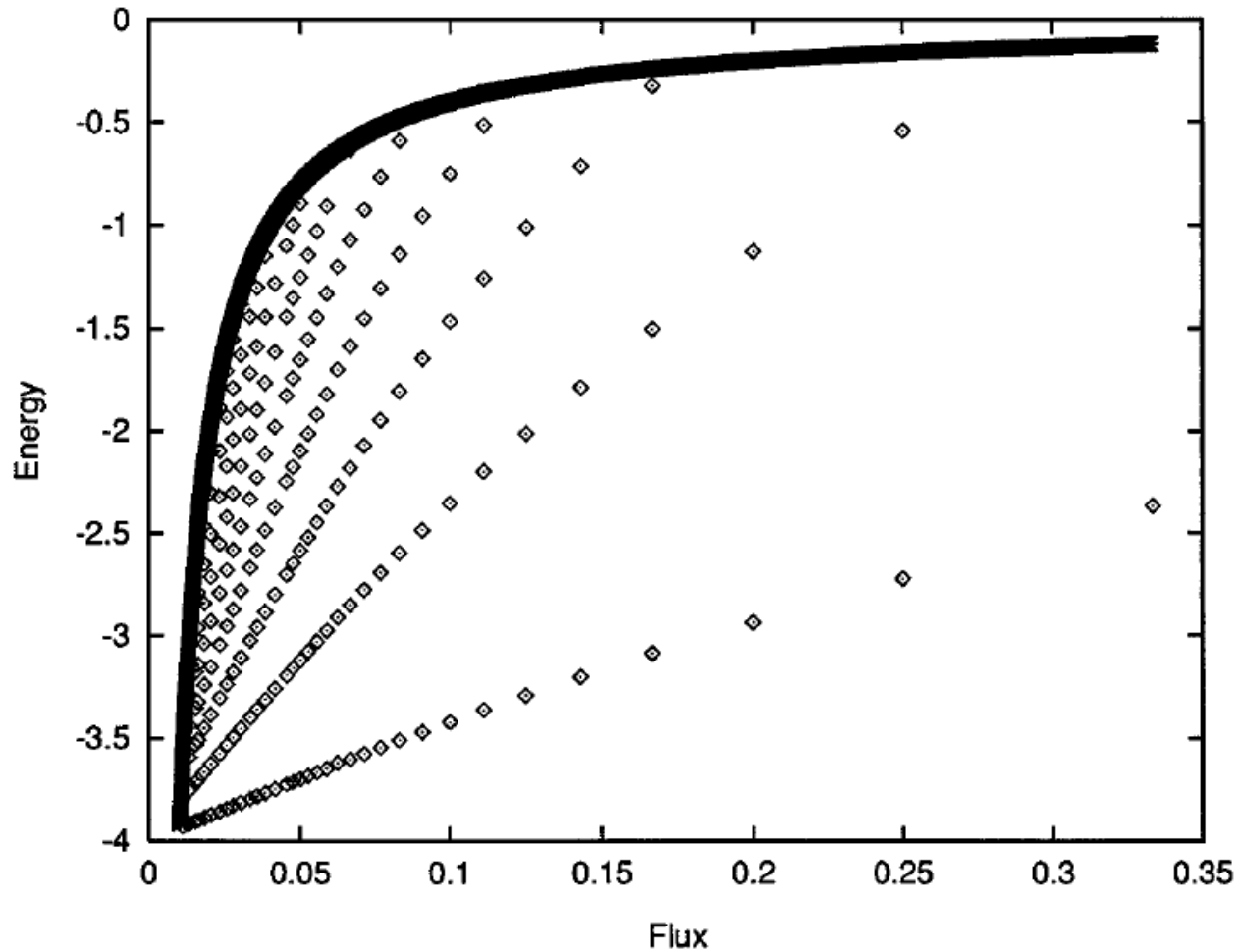
C.H. Lee, Y.H. Chang, Y.W. Suen, and H.H. Lin, PRB (1998)

Insulator to N=4 transition



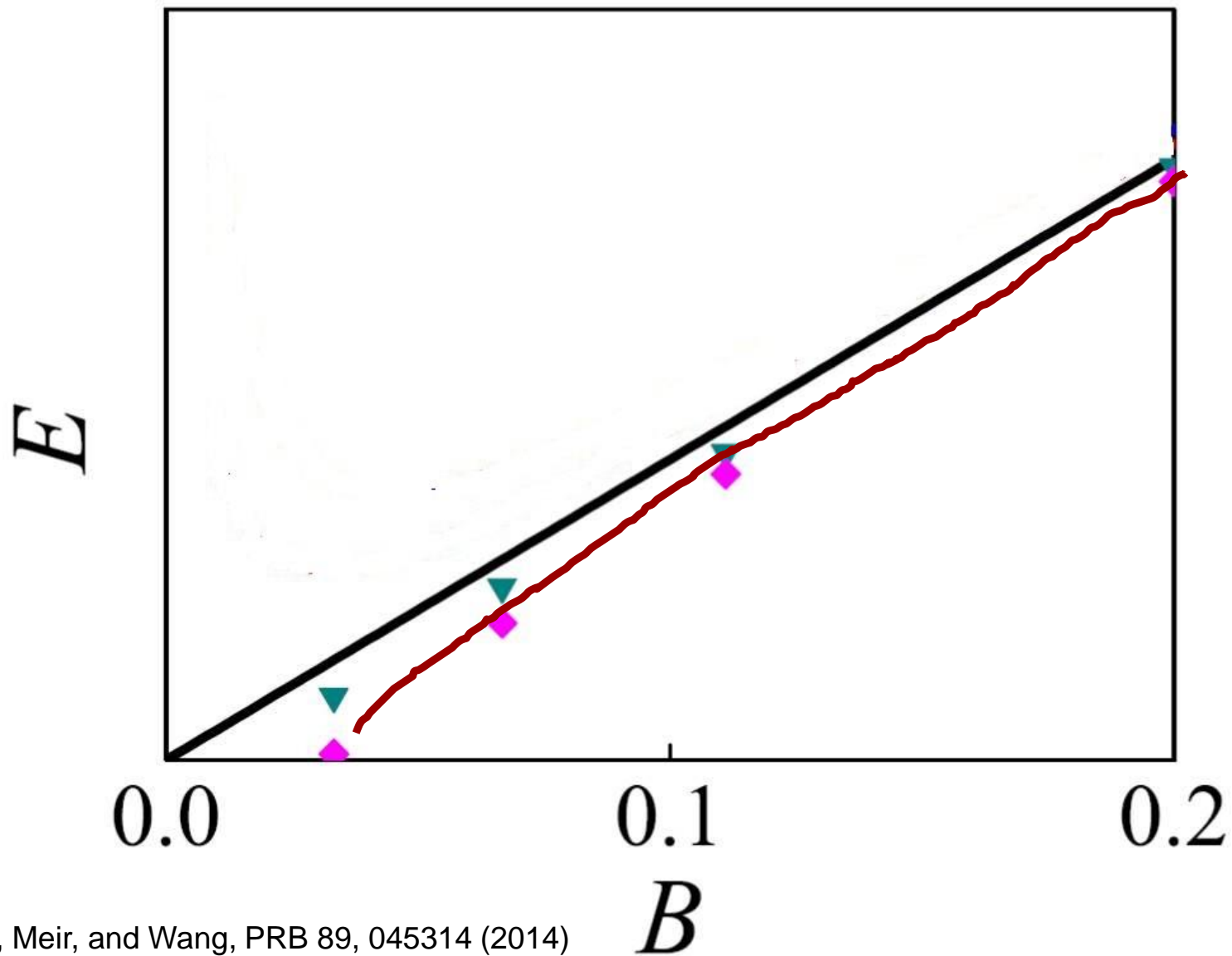
S.T. Lo, et al, C.-T. Liang, Solid State Commun. (2010)

non-floating behavior

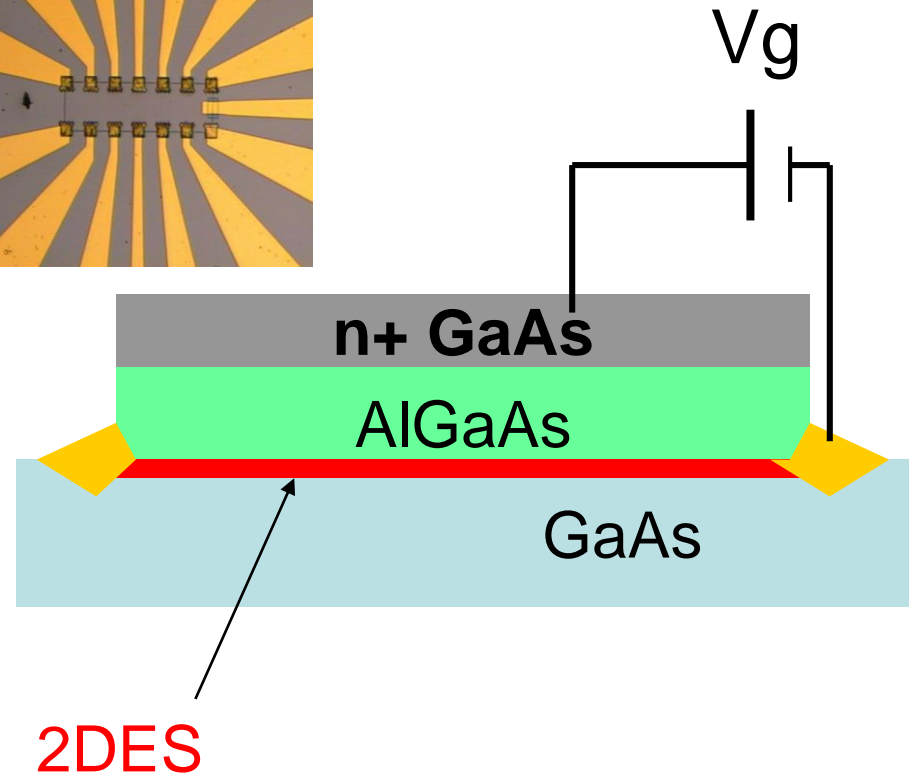
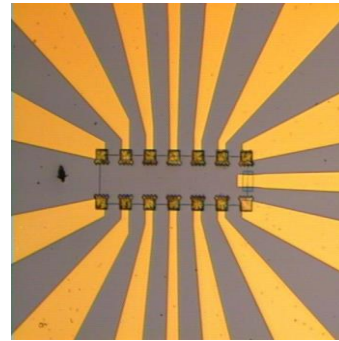
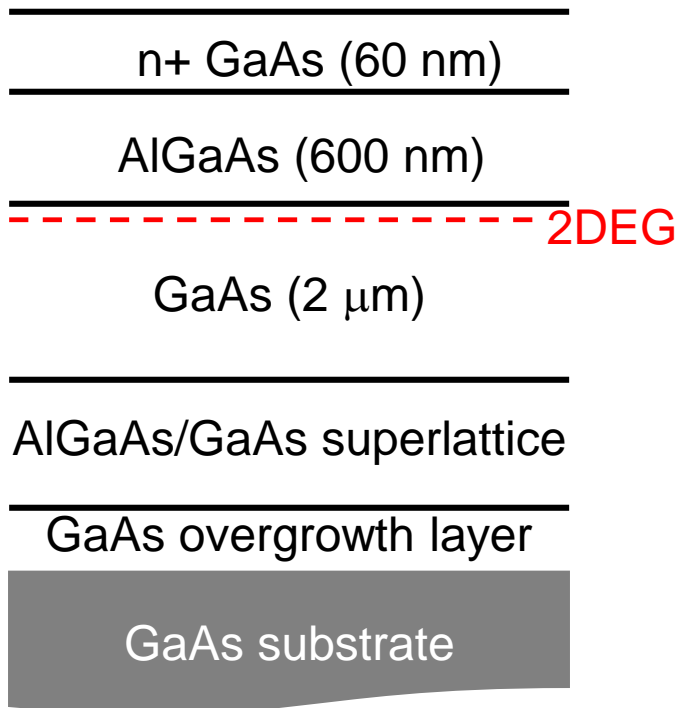


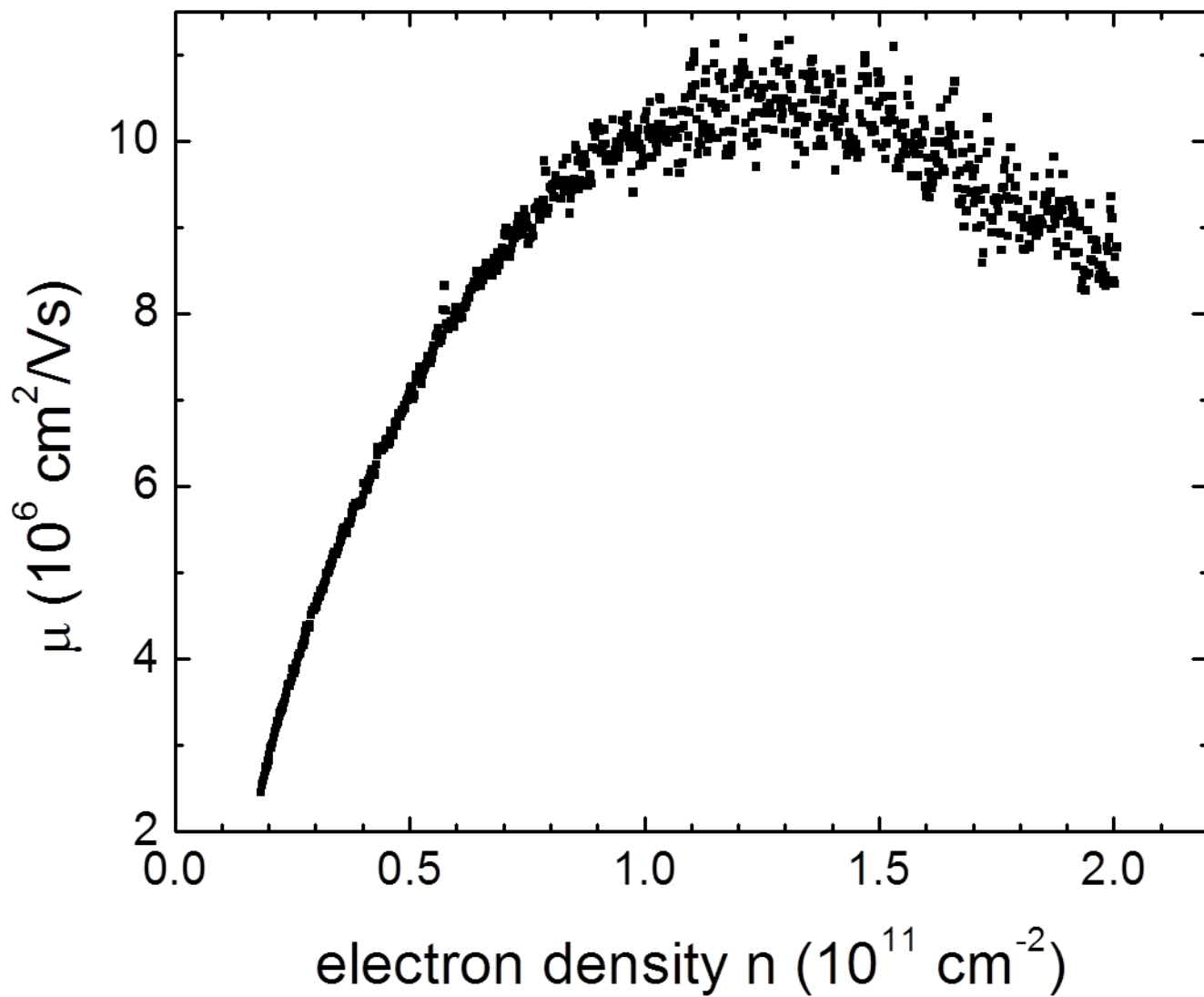
Liu et al, PRL 76, 975 (1996)
Sheng et al, PRL 78, 318 (1997)
Yang et al, PRL 76, 1316 (1996)

Anti-levitation of Landau levels

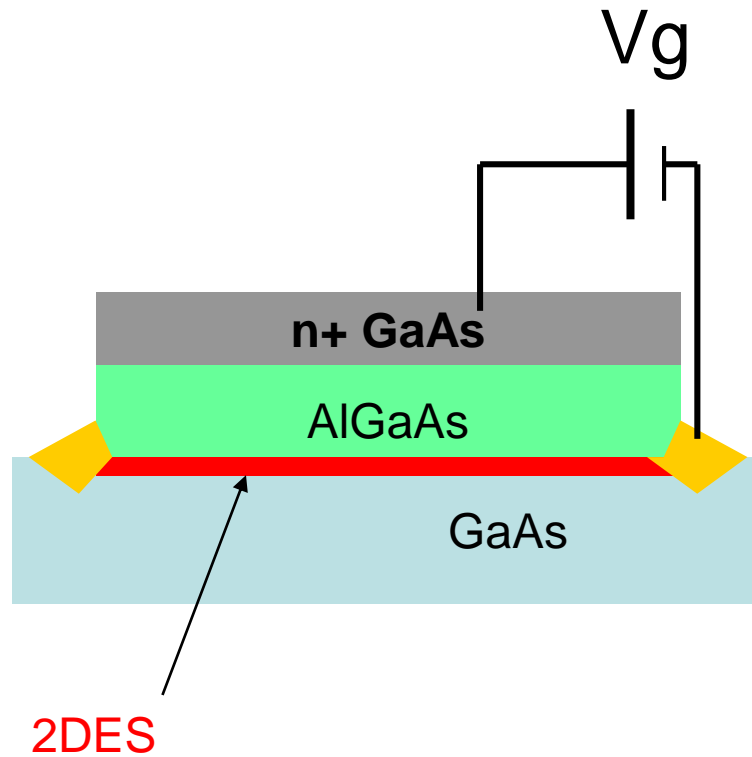


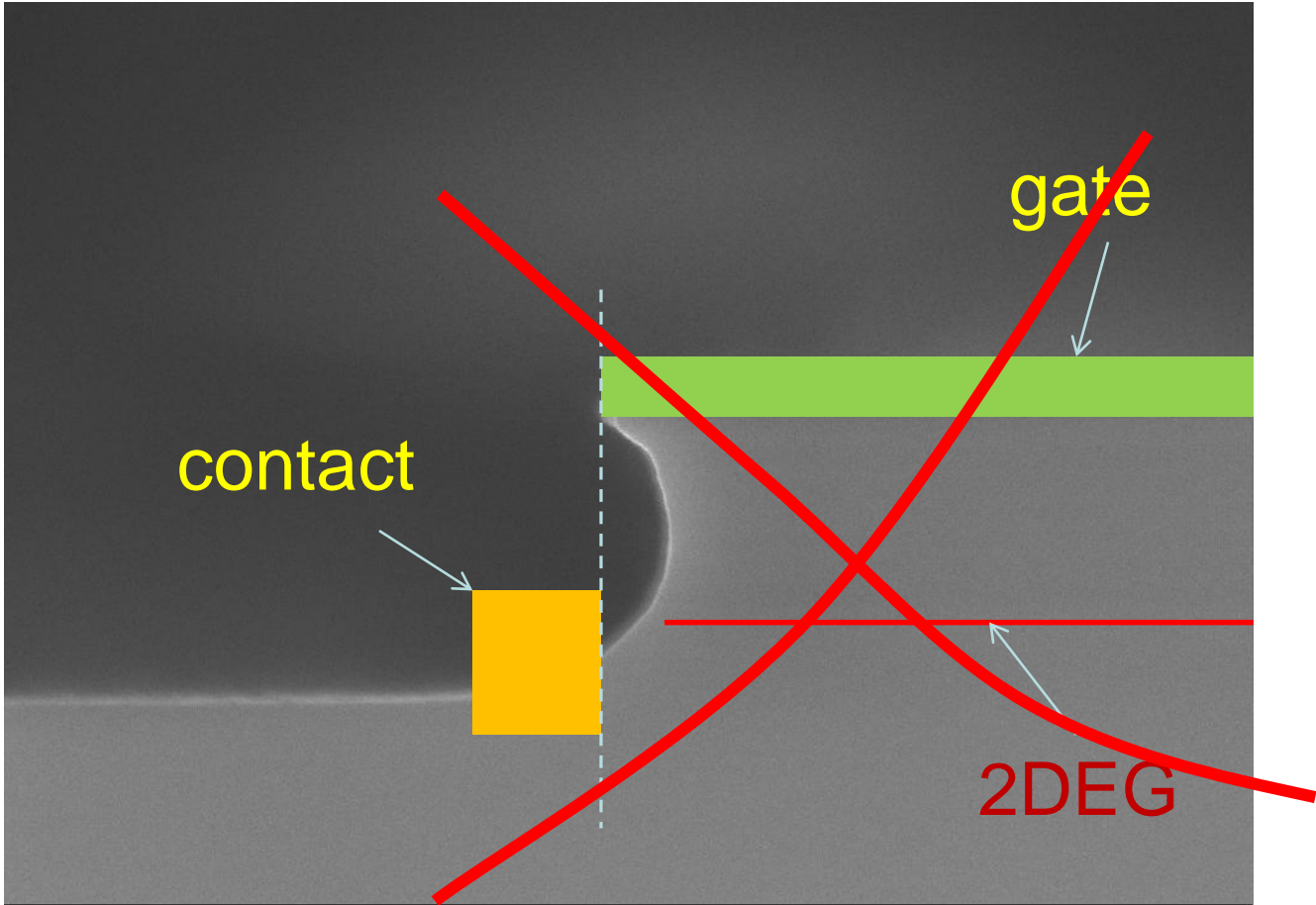
HIGFET (Heterojunction Insulated-Gate Field-Effect Transistor)

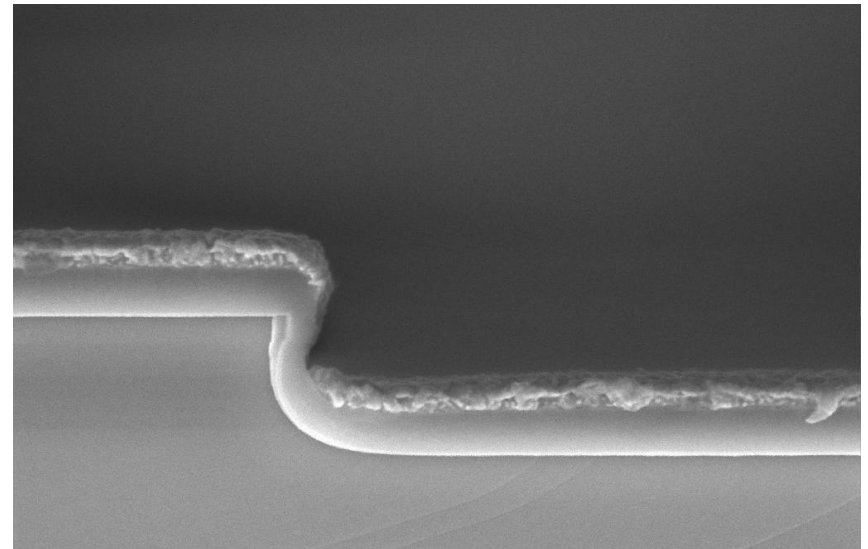
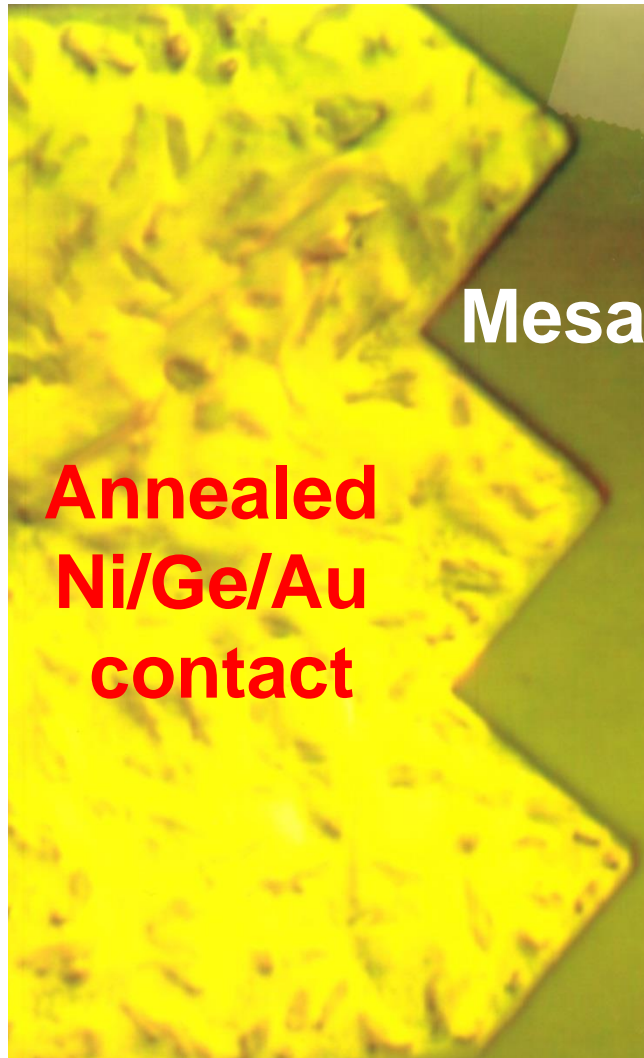




Straight sidewall is important

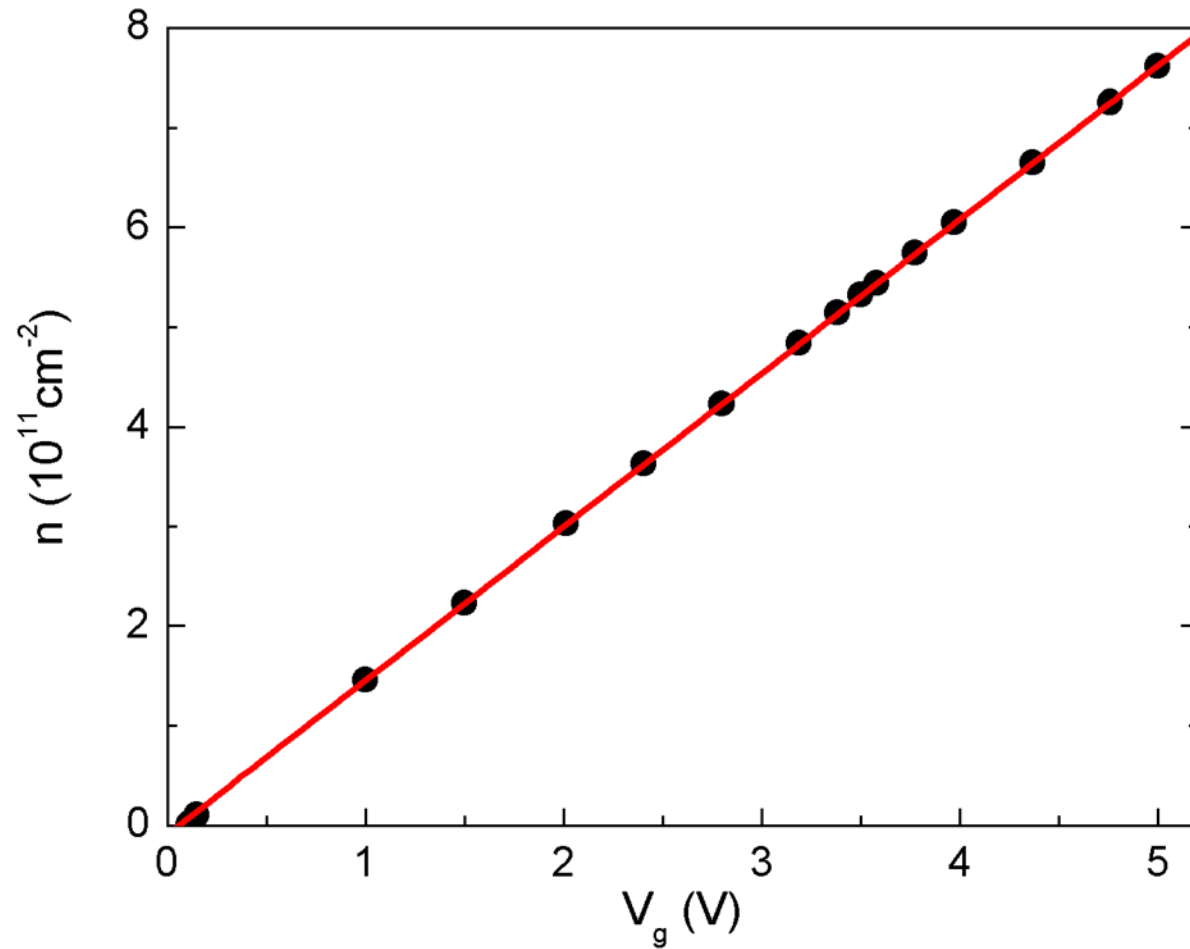




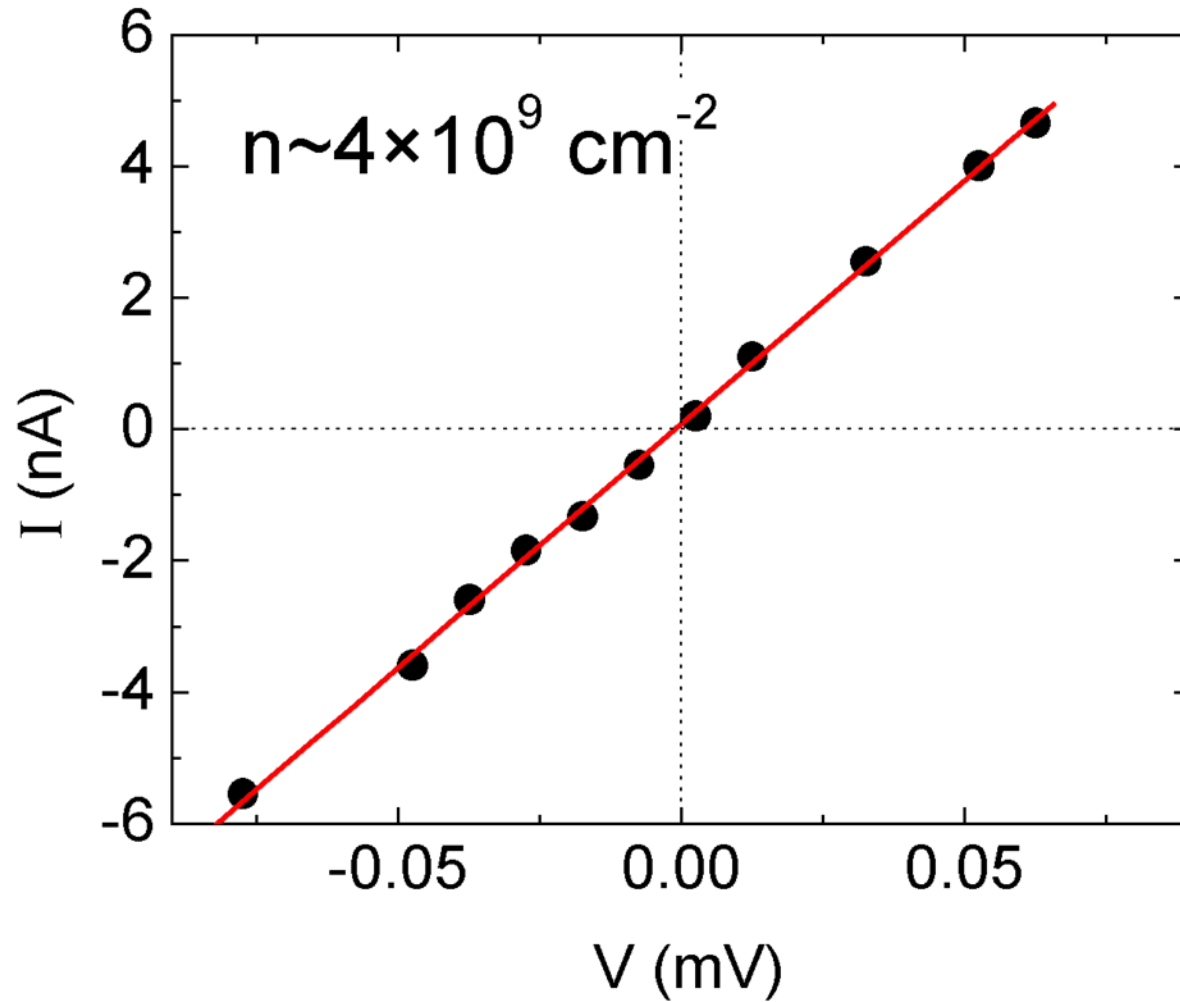


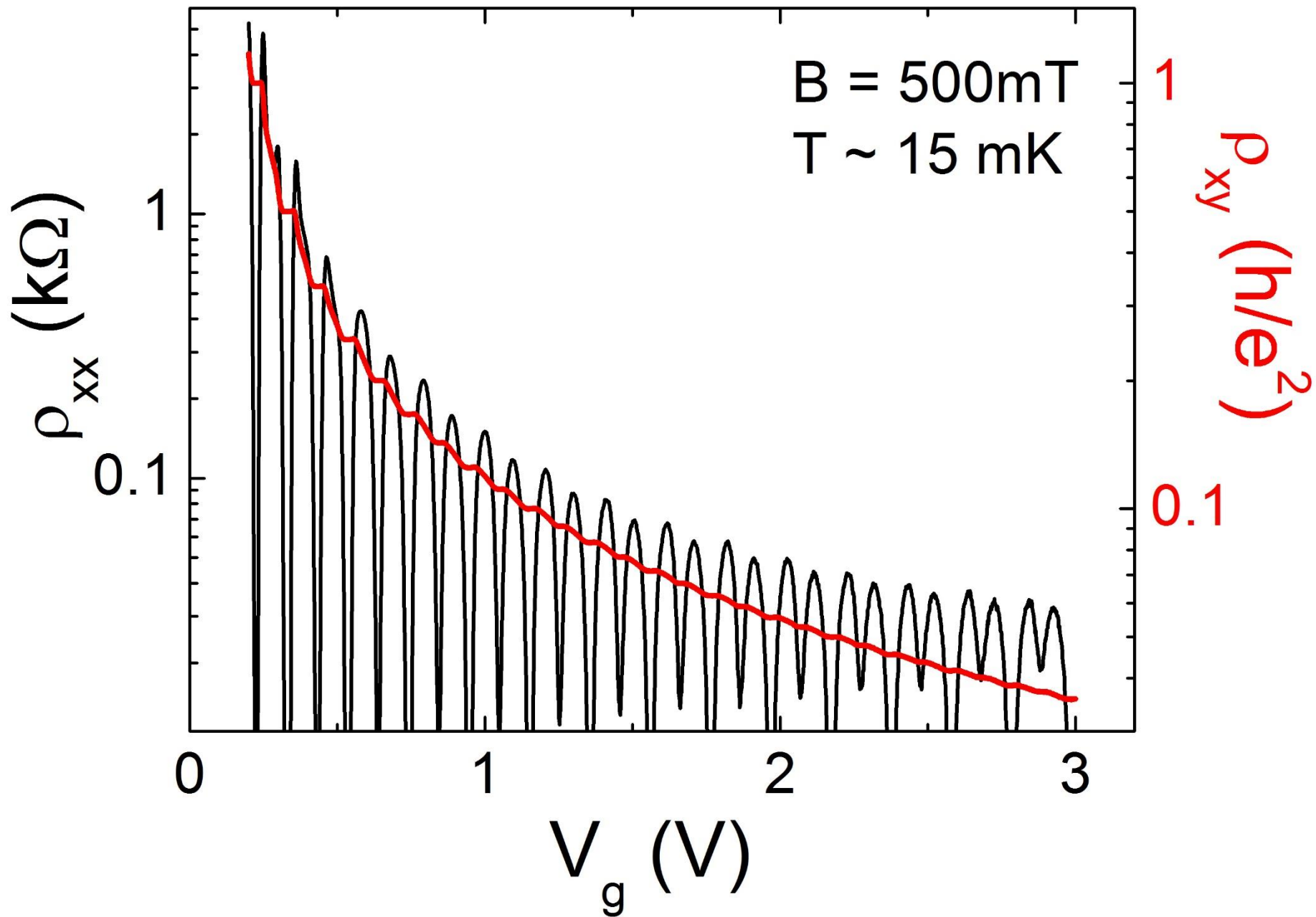
device works!

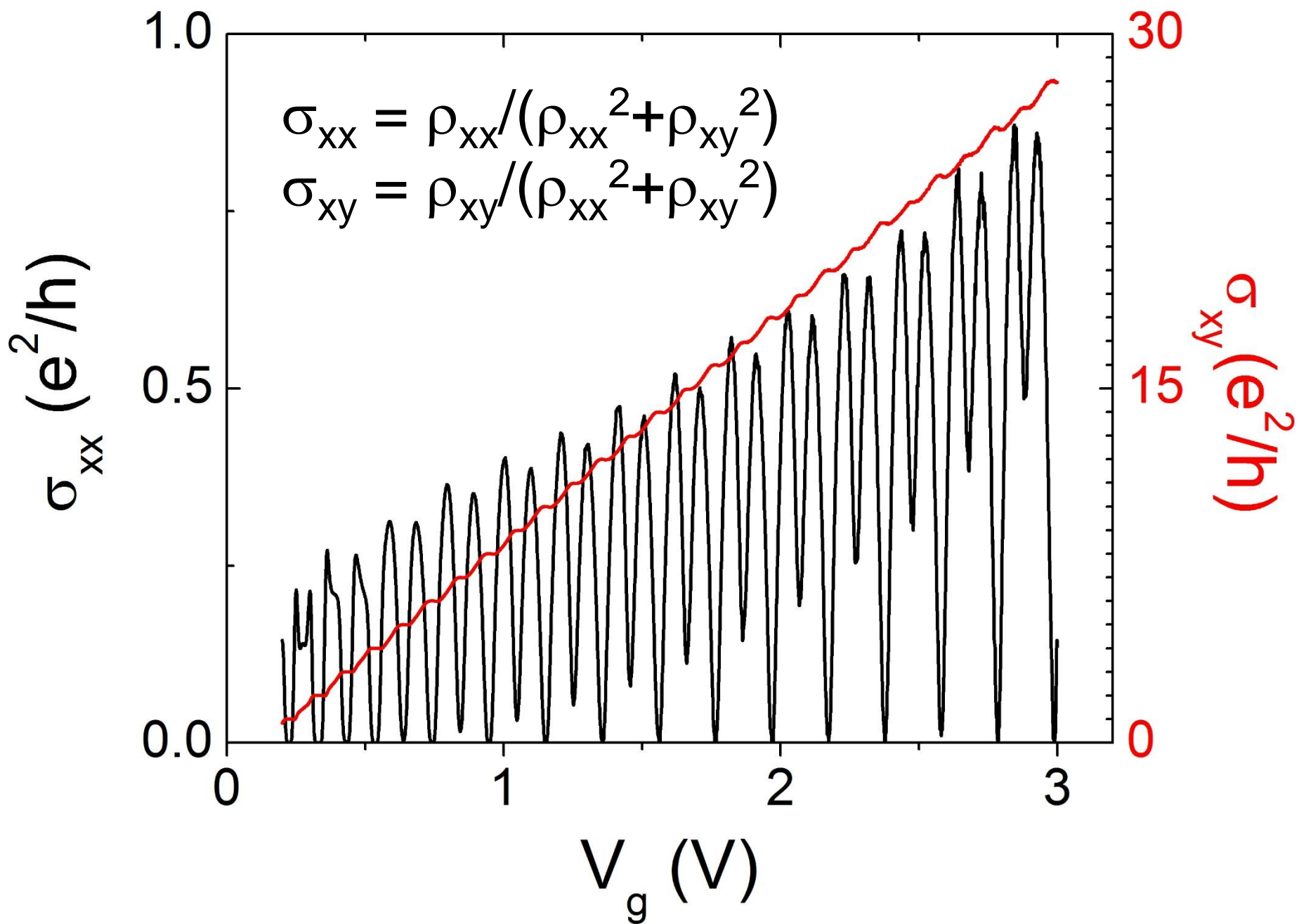
Very large density range
 $\sim 1 \times 10^9$ to $\sim 7.5 \times 10^{11} \text{ cm}^{-2}$



Linear I-V at very low densities

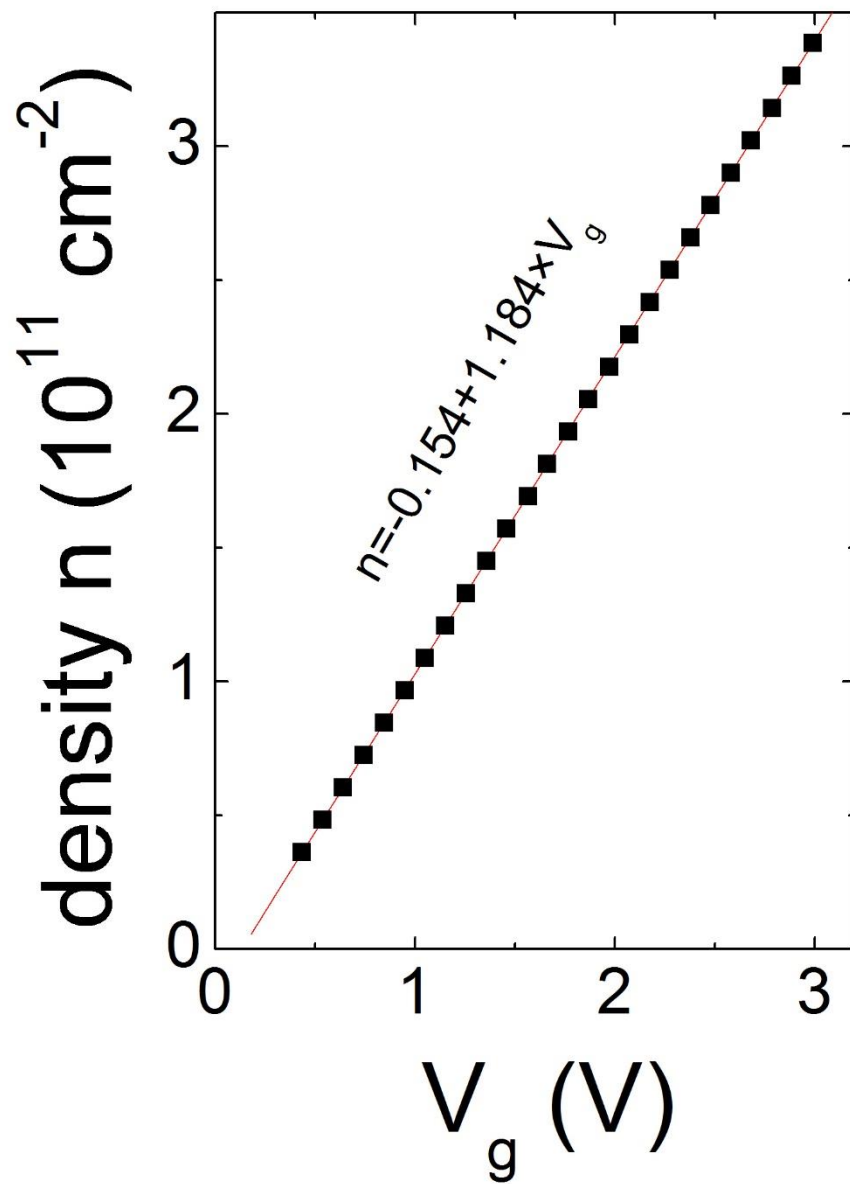
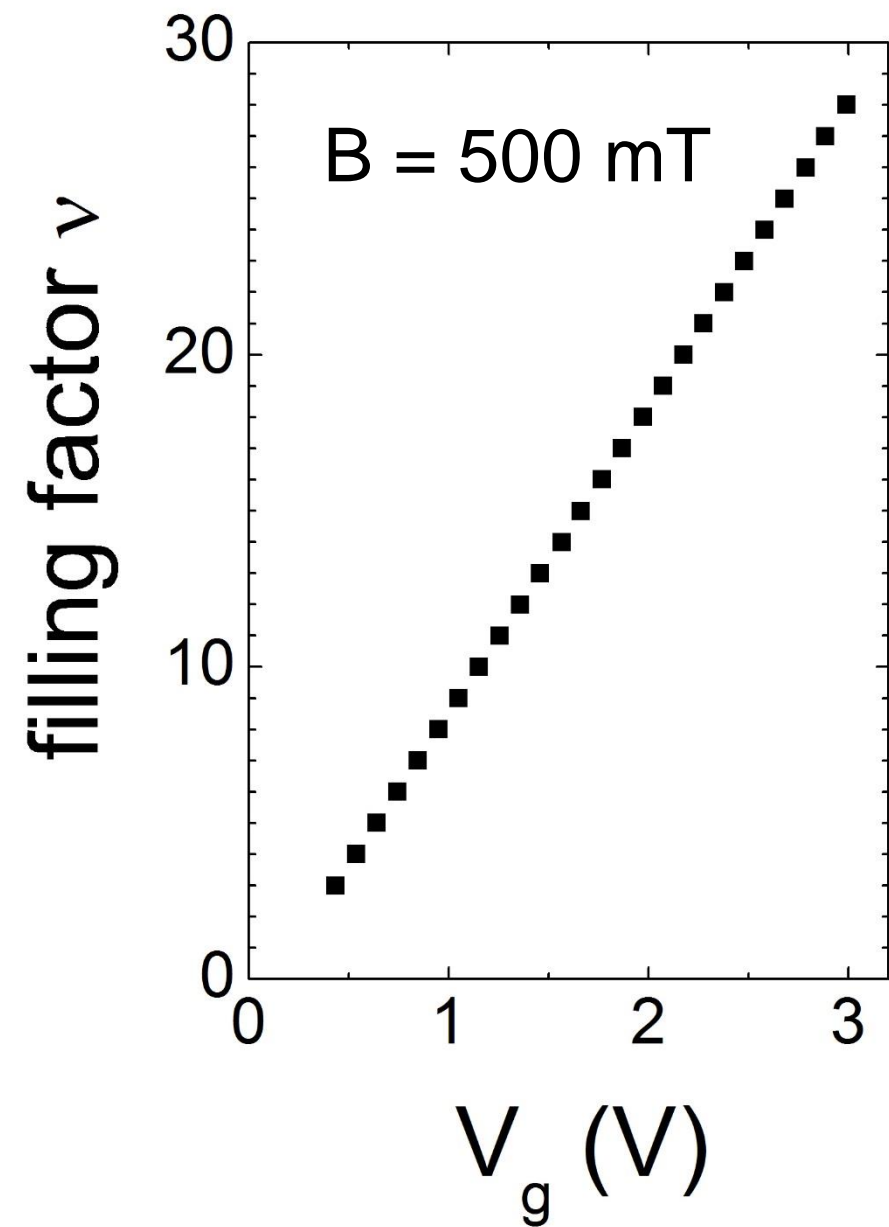


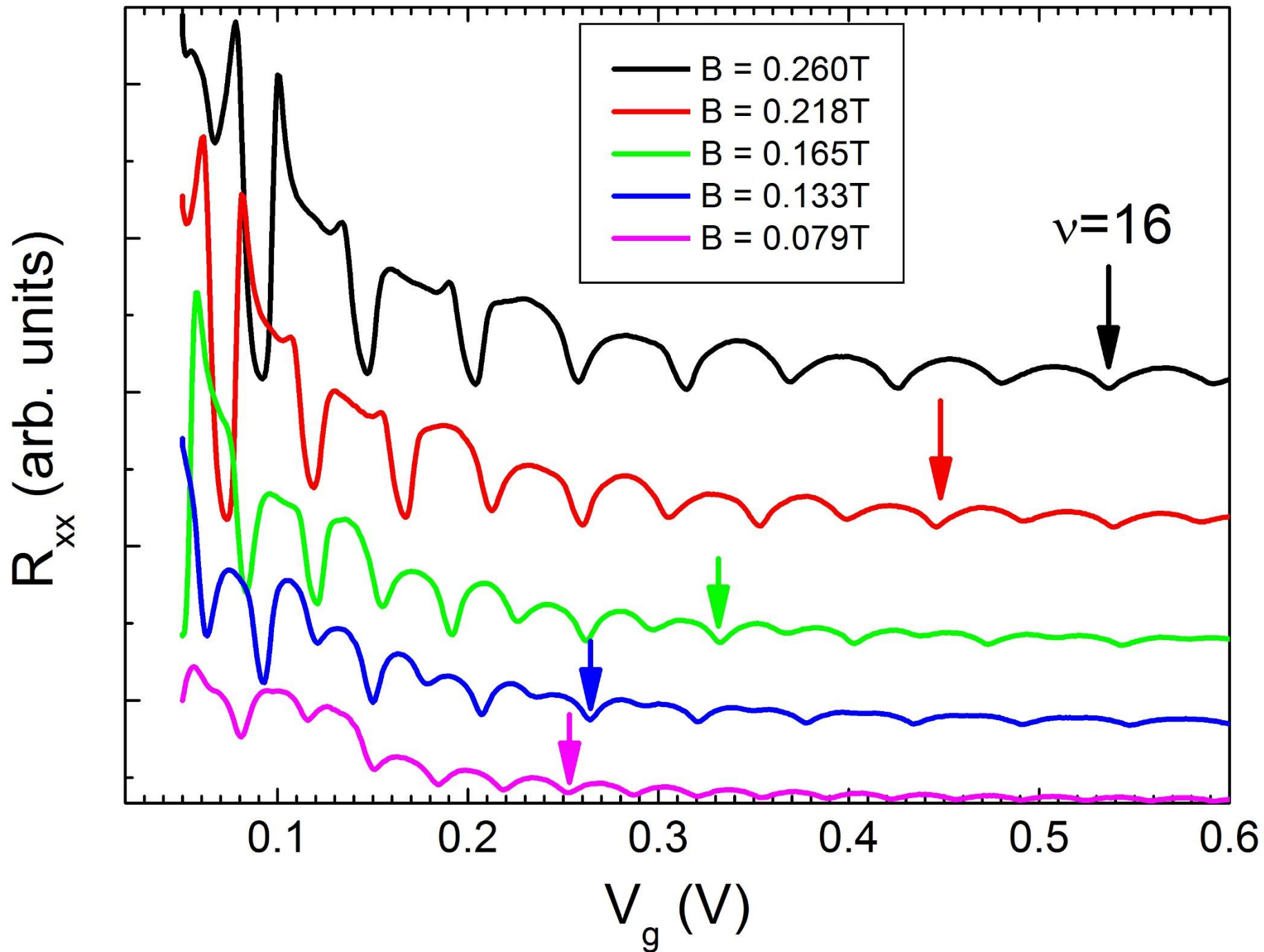


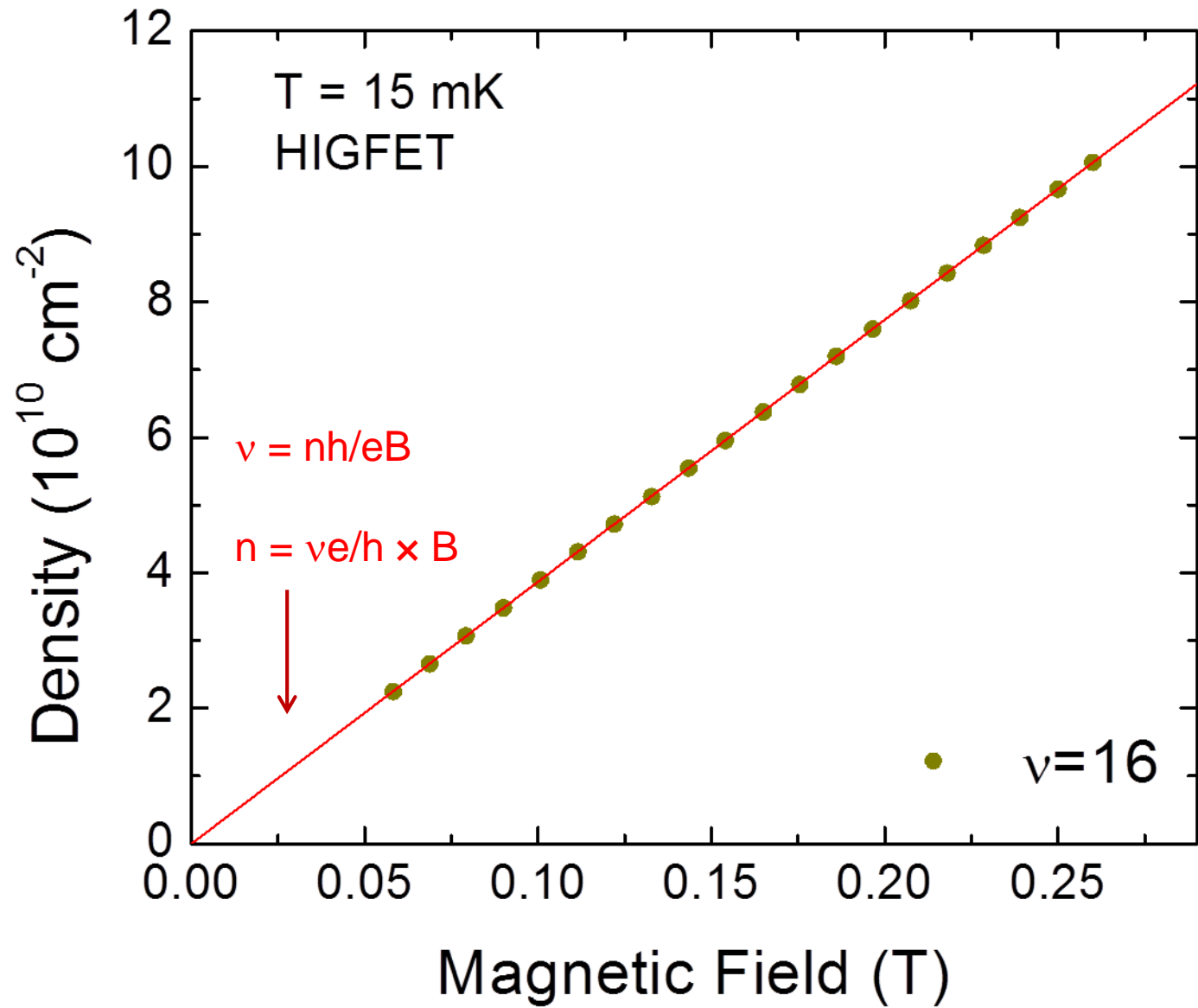


$$\nu = nh/eB$$

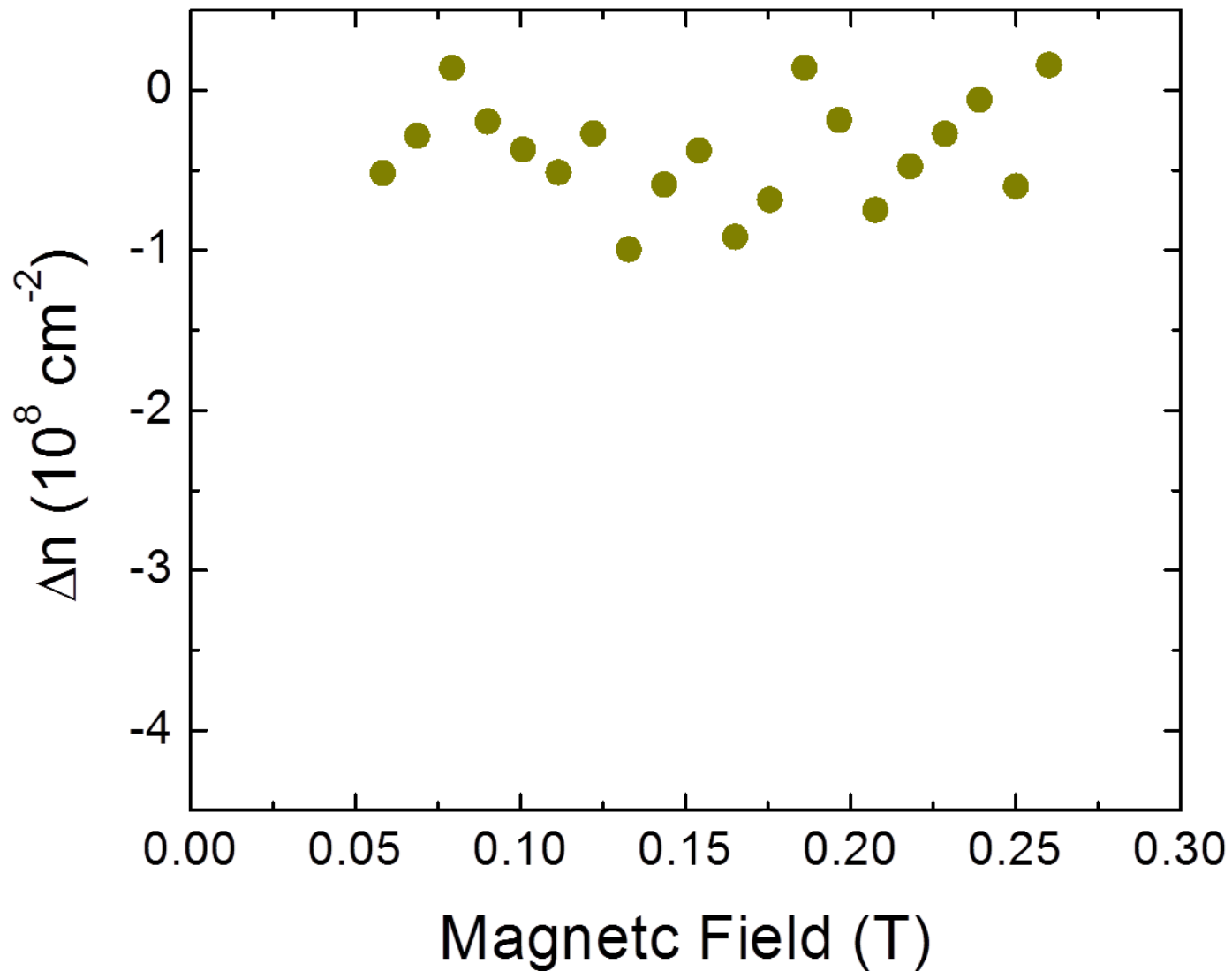
$$n = \nu e/h \times B$$

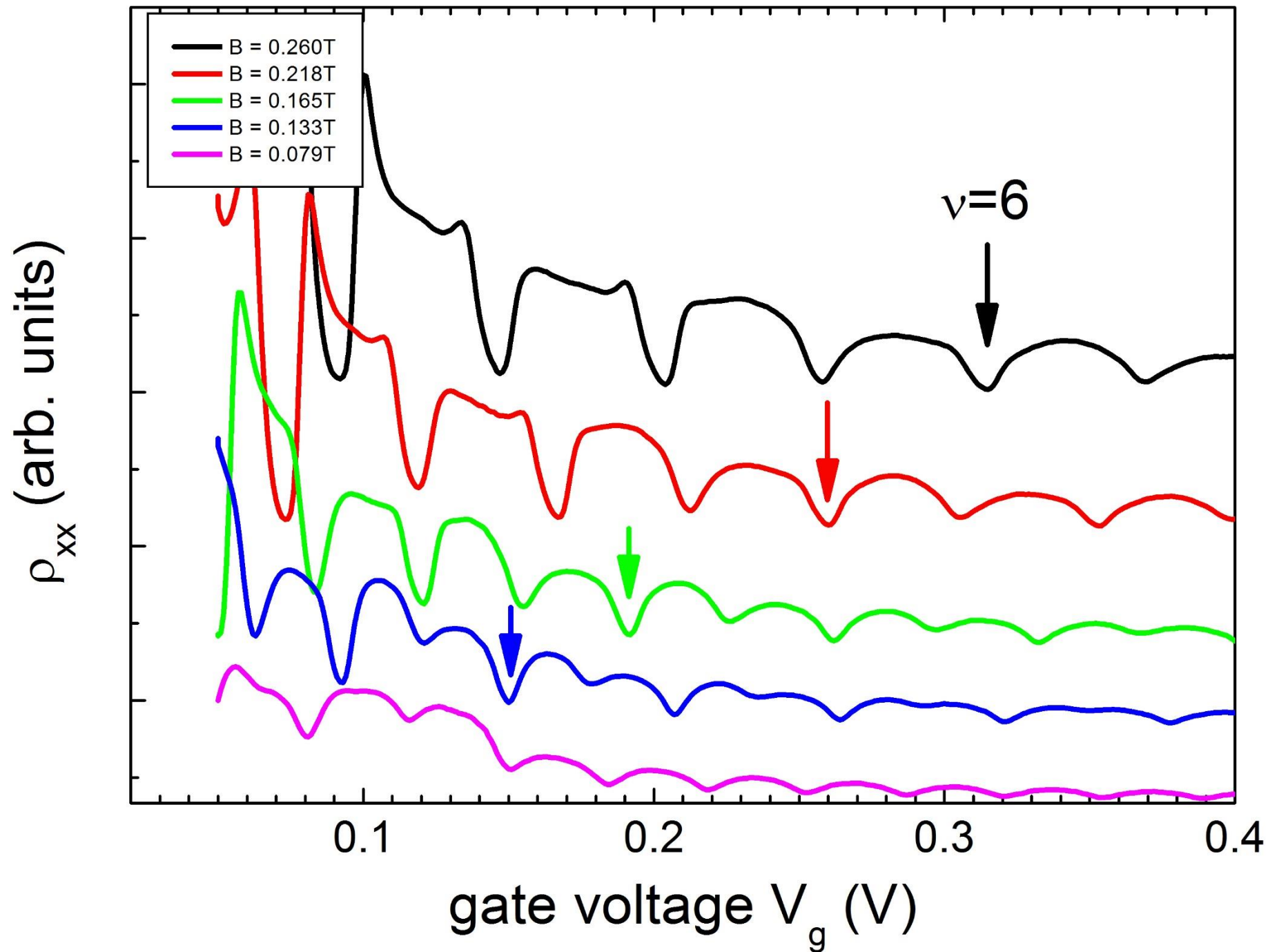


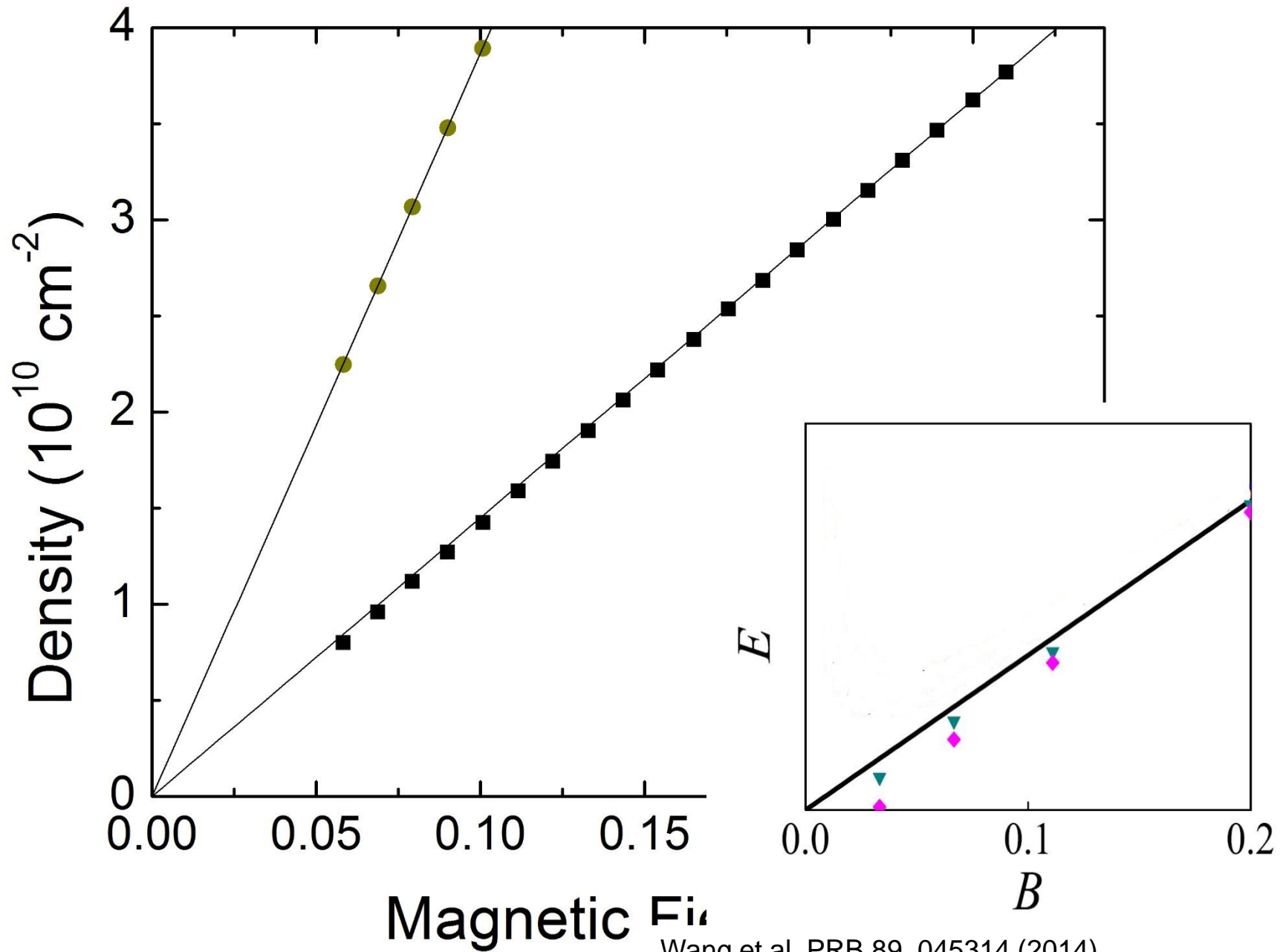


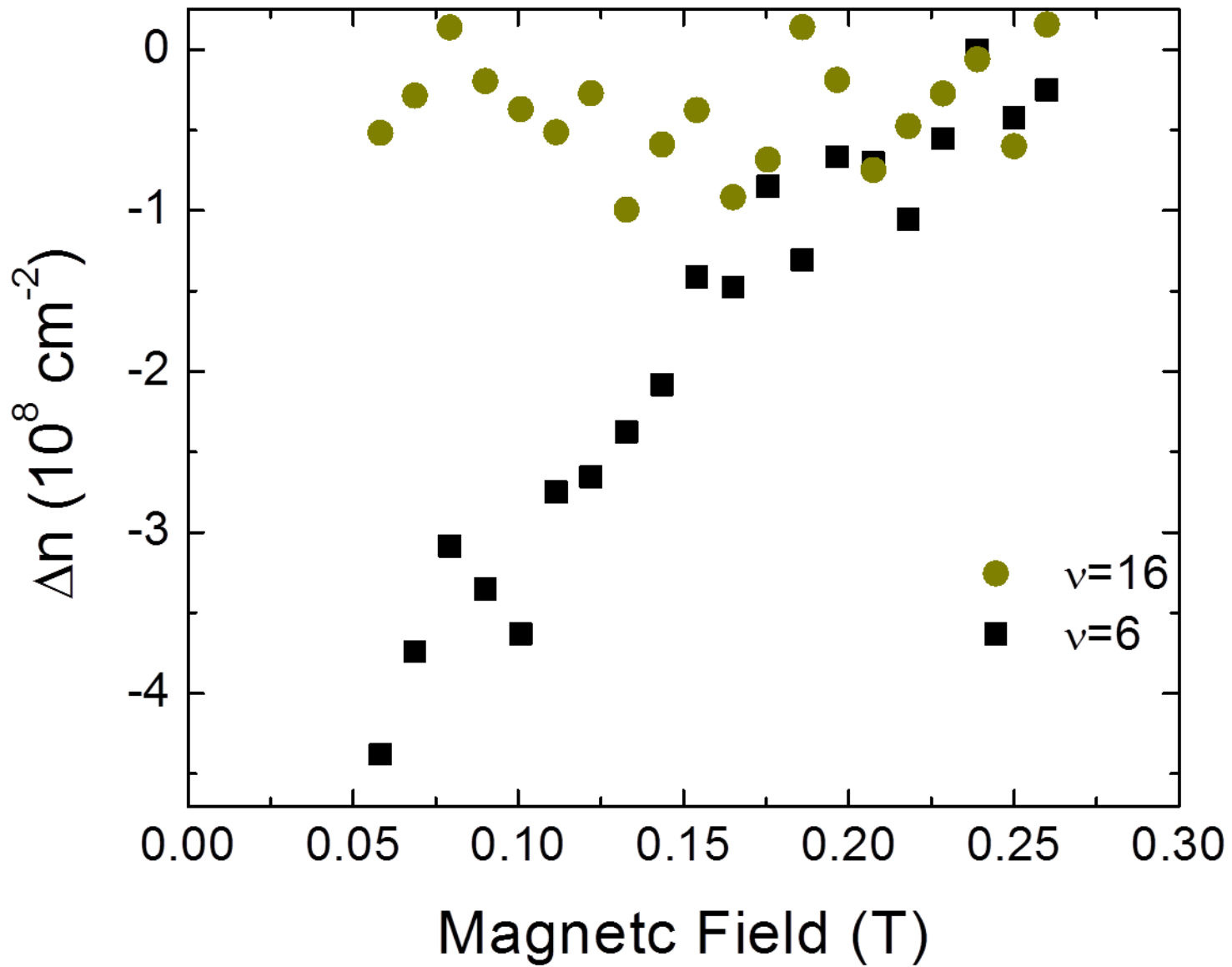


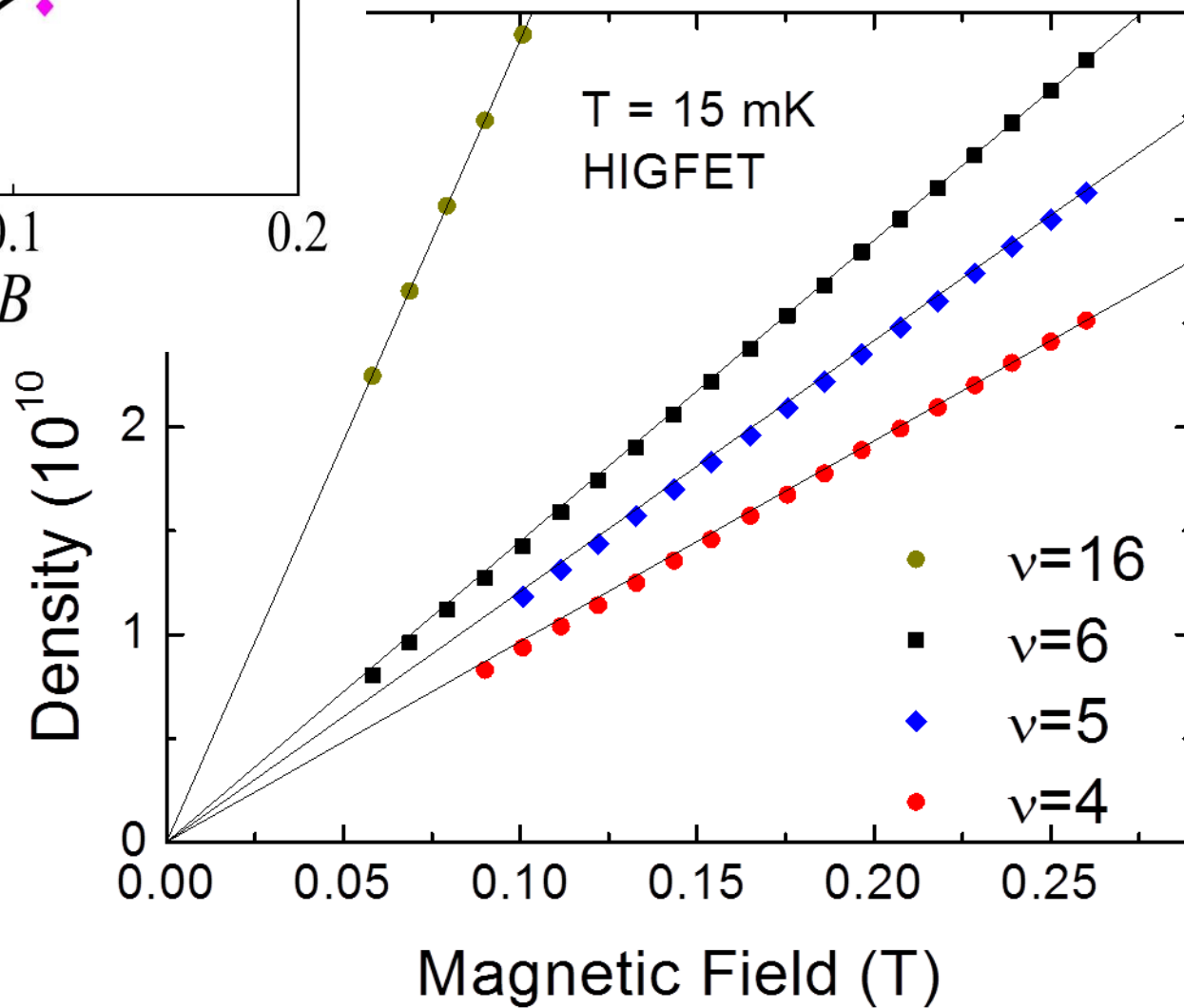
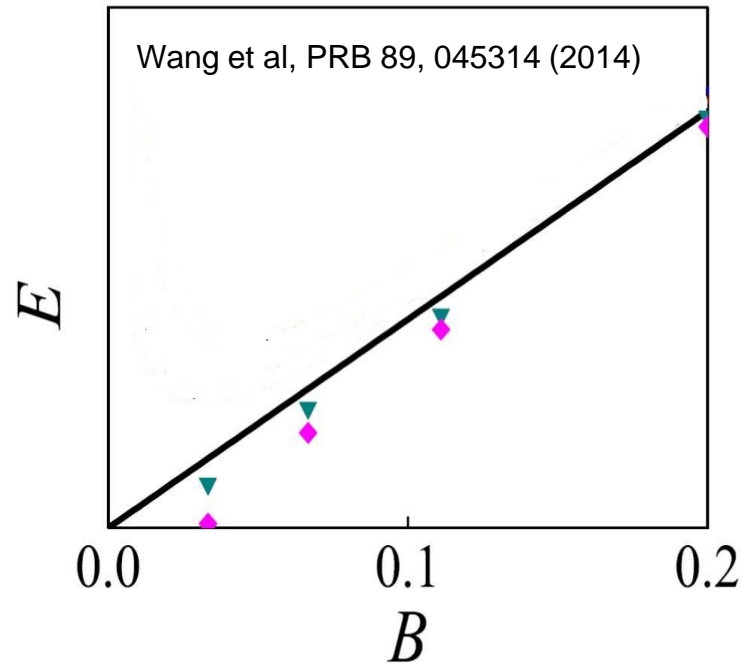
$$\langle \delta n \rangle \approx -4 \times 10^7 \text{ cm}^{-2}$$



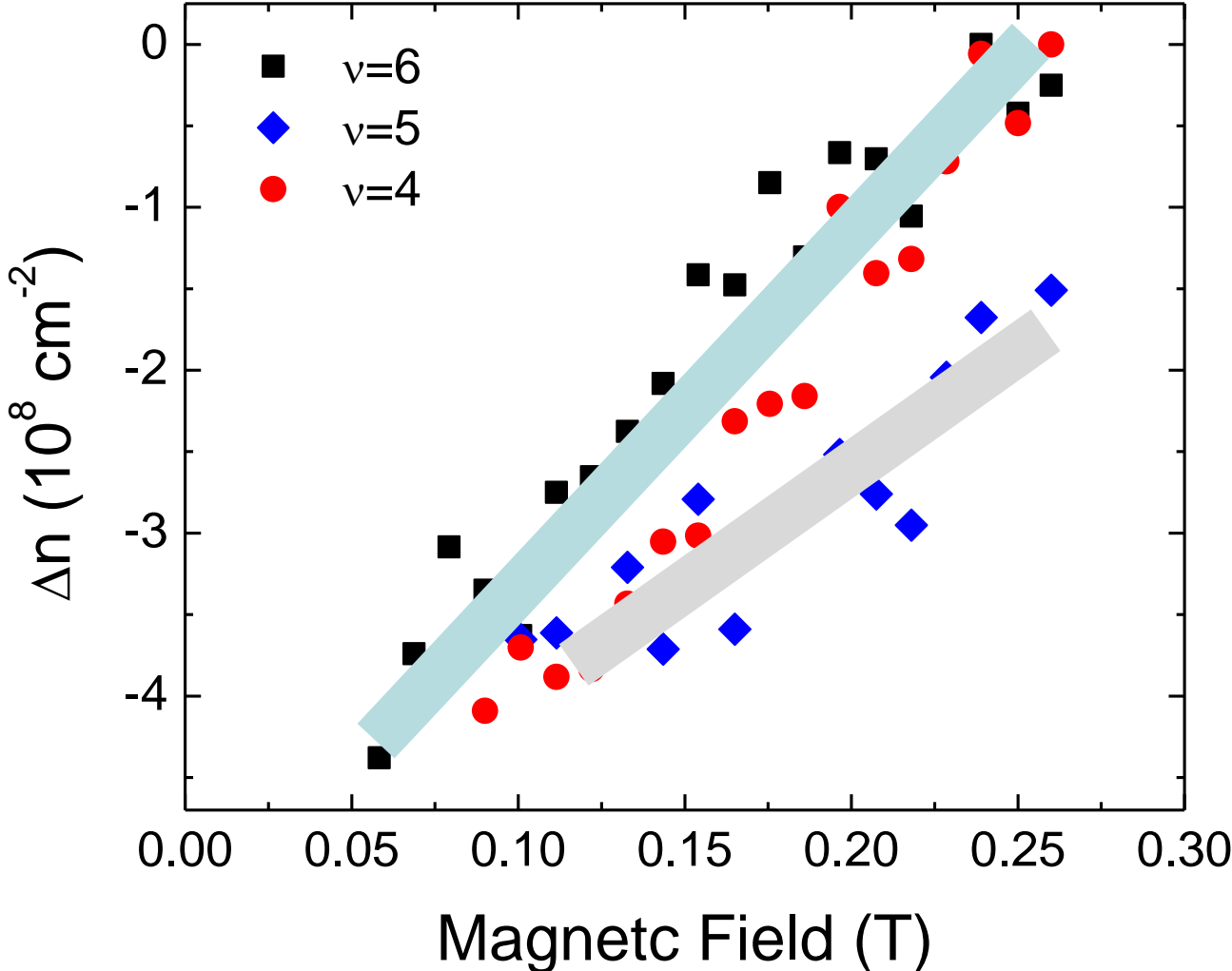




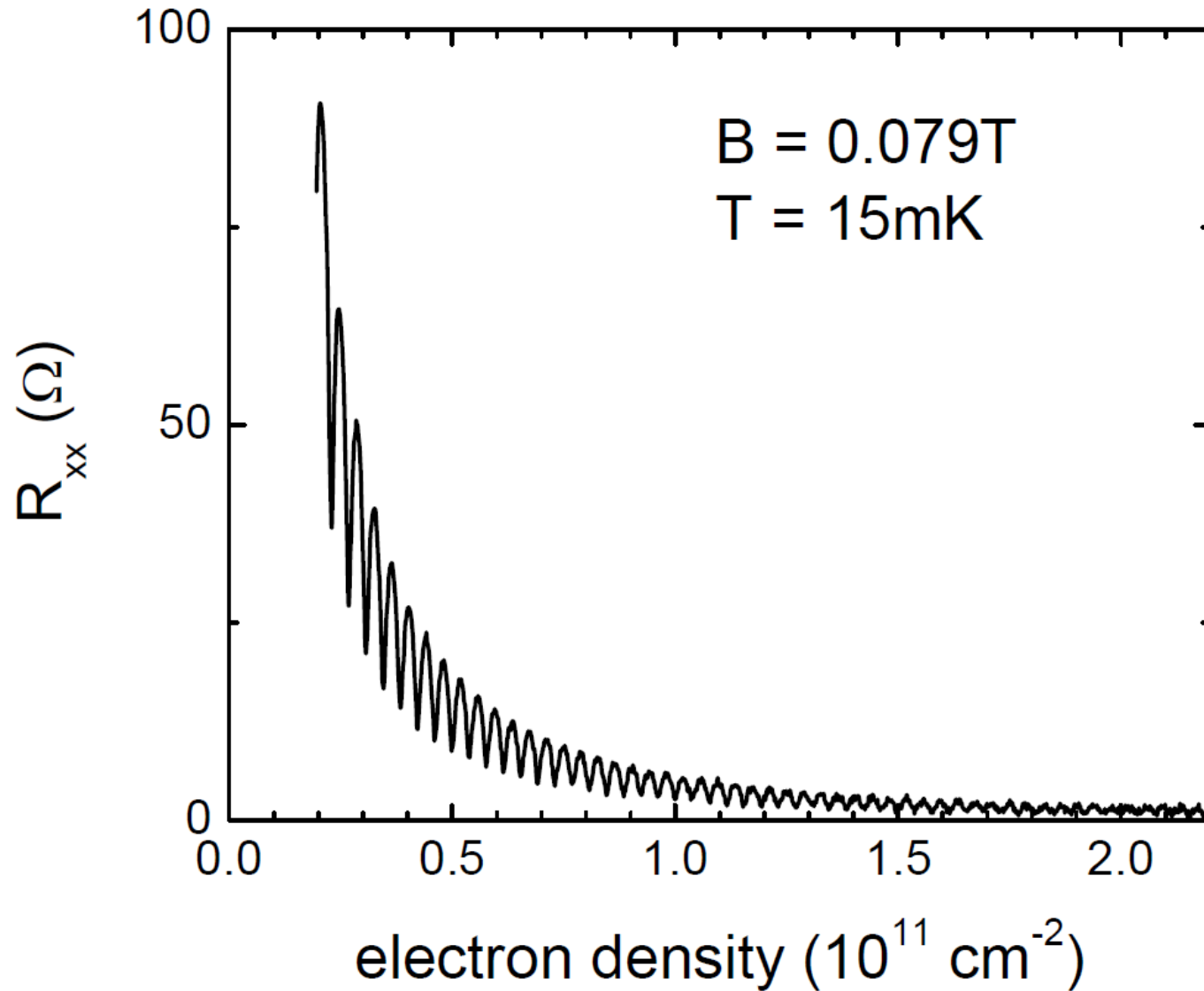


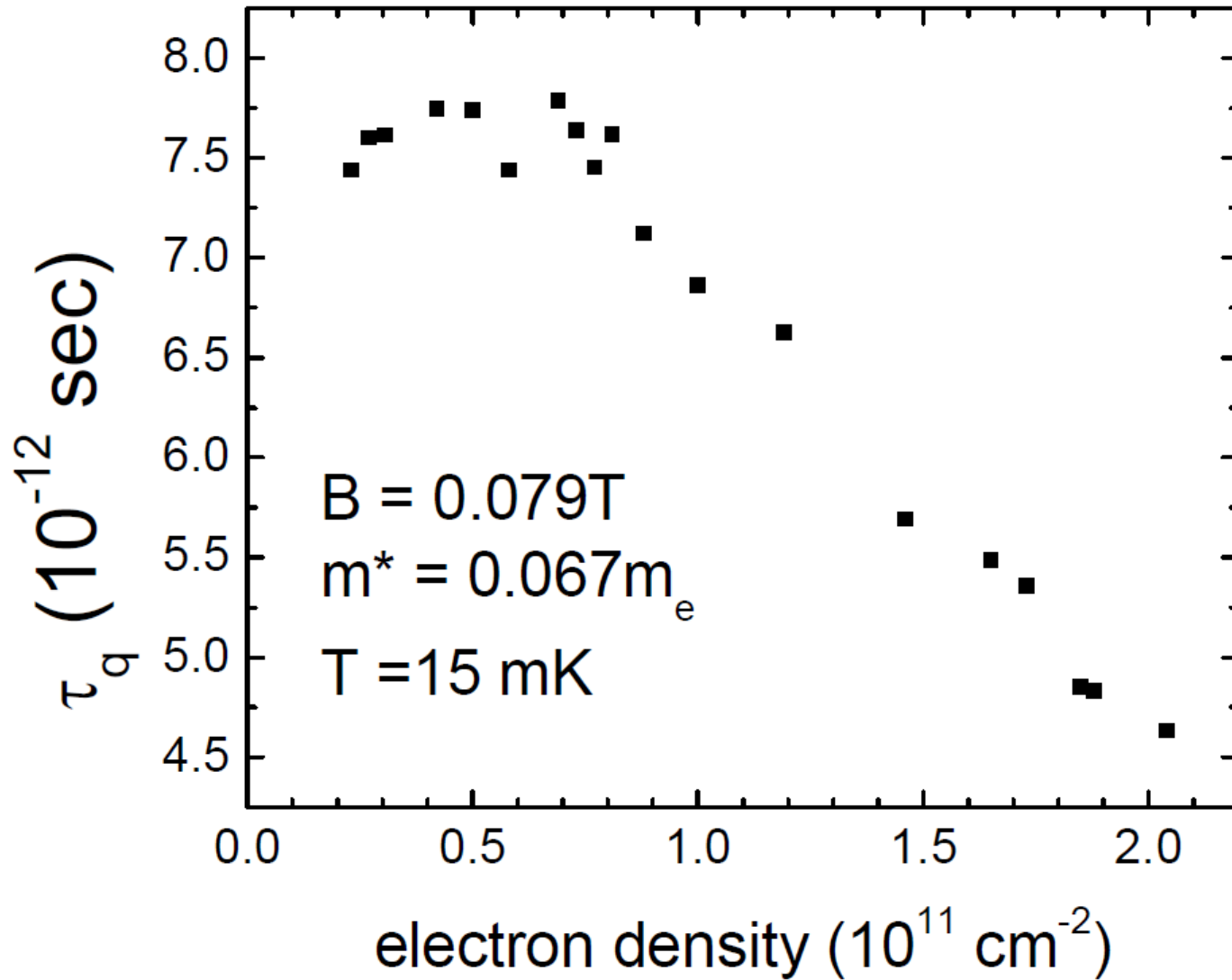


Observation of anti-floating in vanishing B field



SdH oscillations at $B = 0.079\text{T}$





$$\Delta\rho/\rho = 4x(2\pi^2k_B T/\hbar\omega_c/\sinh(2\pi^2k_B T/\hbar\omega_c))x\exp(-\pi/\omega_c\tau_q)$$

$\Delta\rho$ from SdH oscillations, $\rho = 1/(ne\mu)$

part I conclusion

In a high-quality HIGFET, anti-levitation of Landau levels is observed in vanishing magnetic fields.

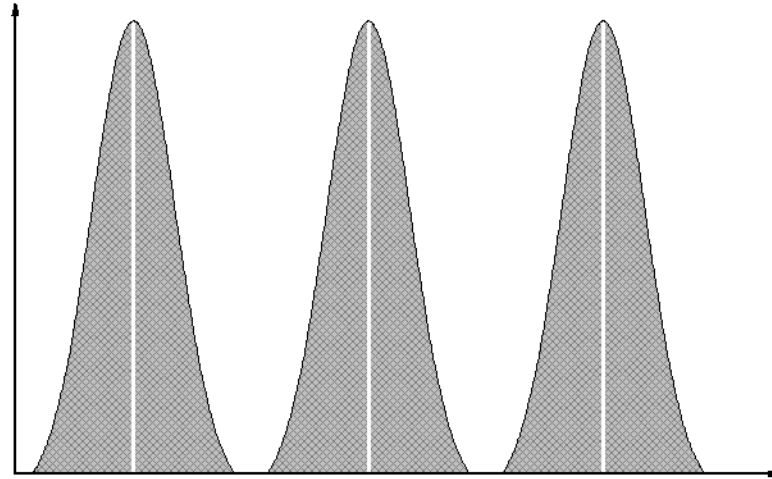
This observation is in a good agreement with the theoretical prediction (C. Wang et al, PRB 2014).

part II outline

(Collapse of spin splitting in the quantum Hall regime)

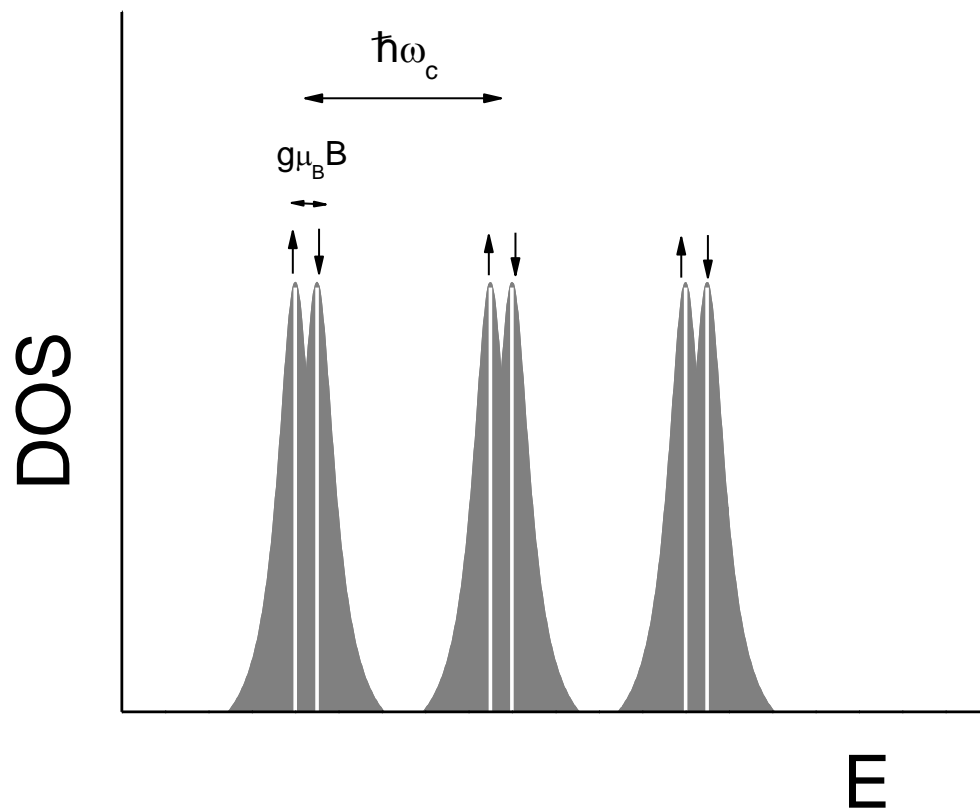
- Background
- Sample
 - HIGFET (Heterojunction Insulated-Gate Field-Effect Transistor)
- Result
 - Landau level number N displays a power-law dependence on 2DEG density n , where the spin splitting collapses.
 - $N = 11.47 \times n^{0.64 \pm 0.01}$ (n is in units of 10^{11} cm^{-2}).
 - This power-law dependence is in good agreement with the theoretical prediction in the low-density regime.

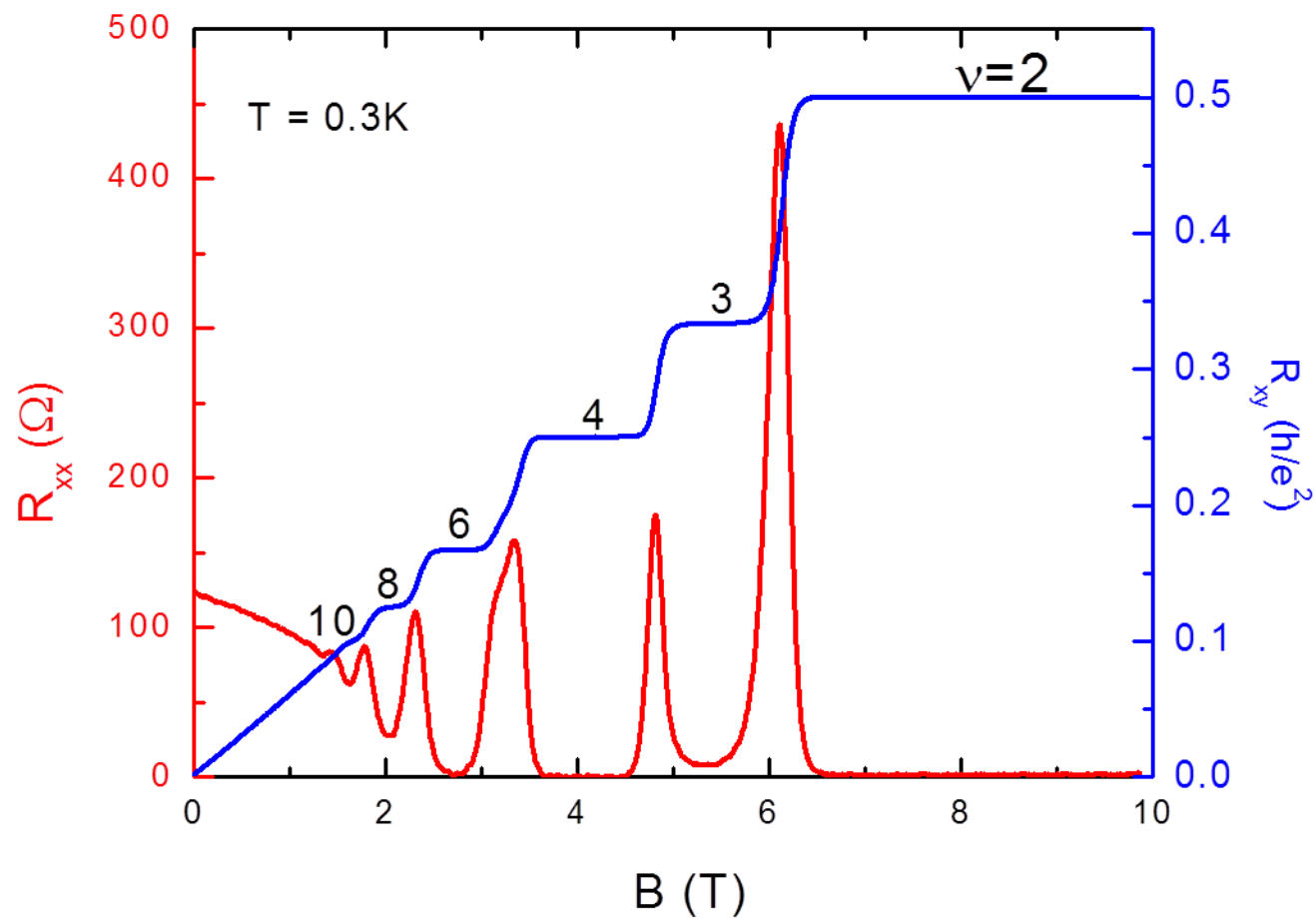
$$\frac{dN}{d\varepsilon}$$

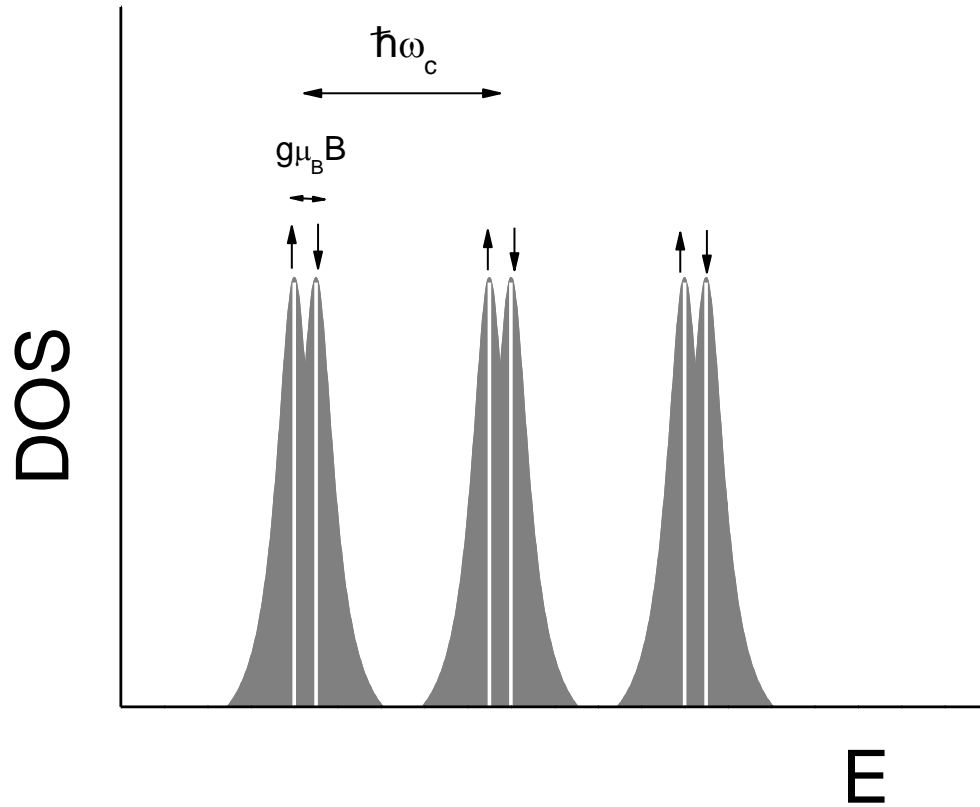


$B \neq 0$

Spin degeneracy lifted



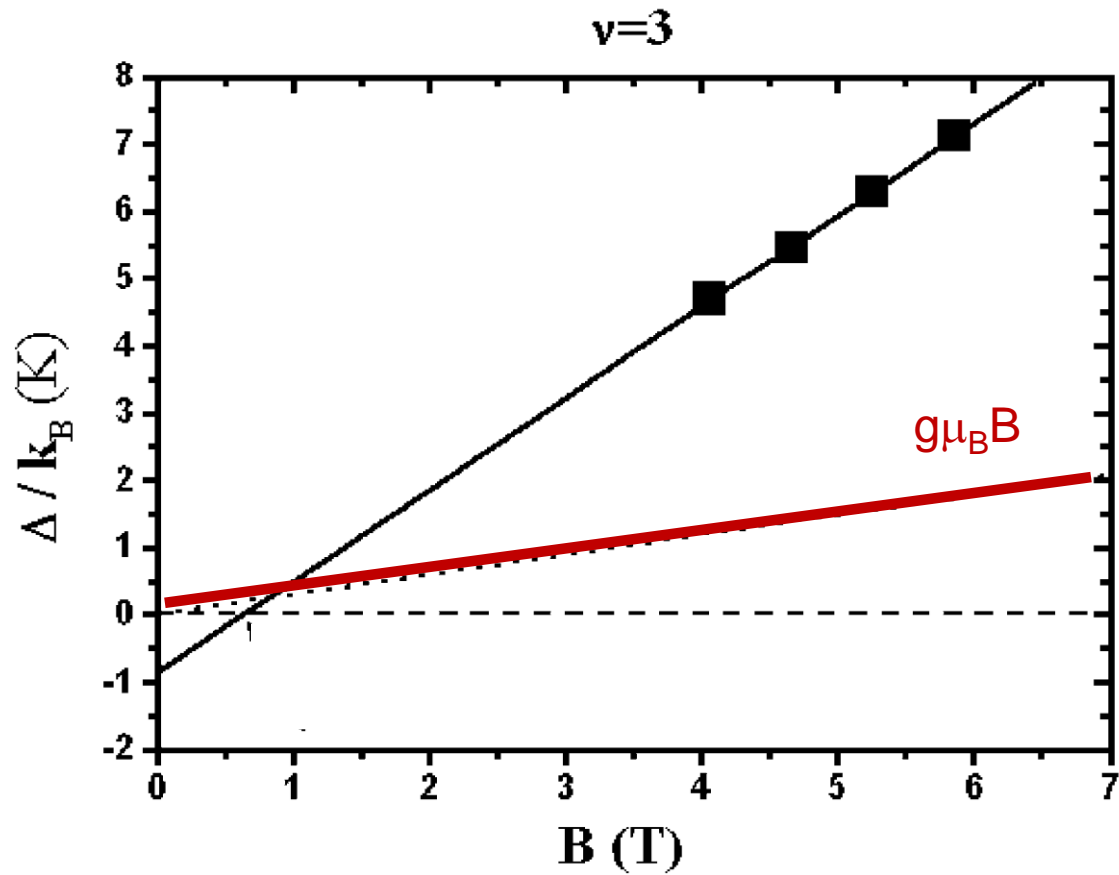




odd Landau level filling states – $\Delta \sim g\mu_B B$

$g = 0.44$, $\mu_B = 0.67\text{K/Tesla}$, $B = 5\text{Tesla}$, $\Delta \sim 1.5\text{K}$

However, odd Landau level filling states – $\Delta \gg g\mu_B B$



g factor enhancement

PHYSICAL REVIEW

VOLUME 178, NUMBER 3

15 FEBRUARY 1969

g Factor of the Two-Dimensional Interacting Electron Gas

J. F. JANAK

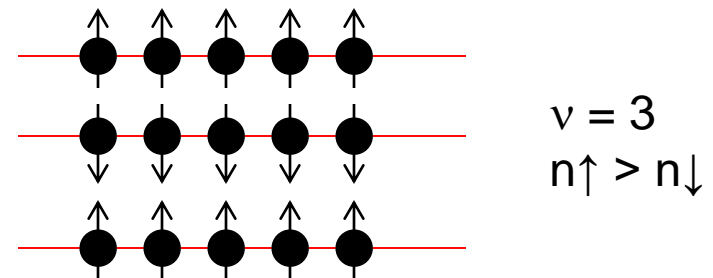
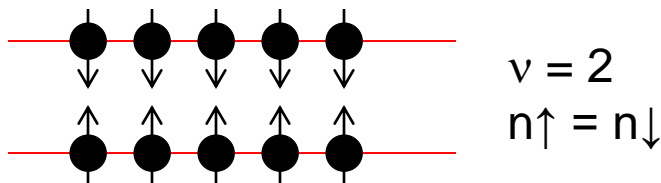
IBM Watson Research Center, Yorktown Heights, New York 10598

(Received 27 September 1968)

$$g^* \mu_B \cdot B = g \mu_B \cdot B + E_{\text{ex}} \sum_{N'} (n_{N'\uparrow} - n_{N'\downarrow}).$$

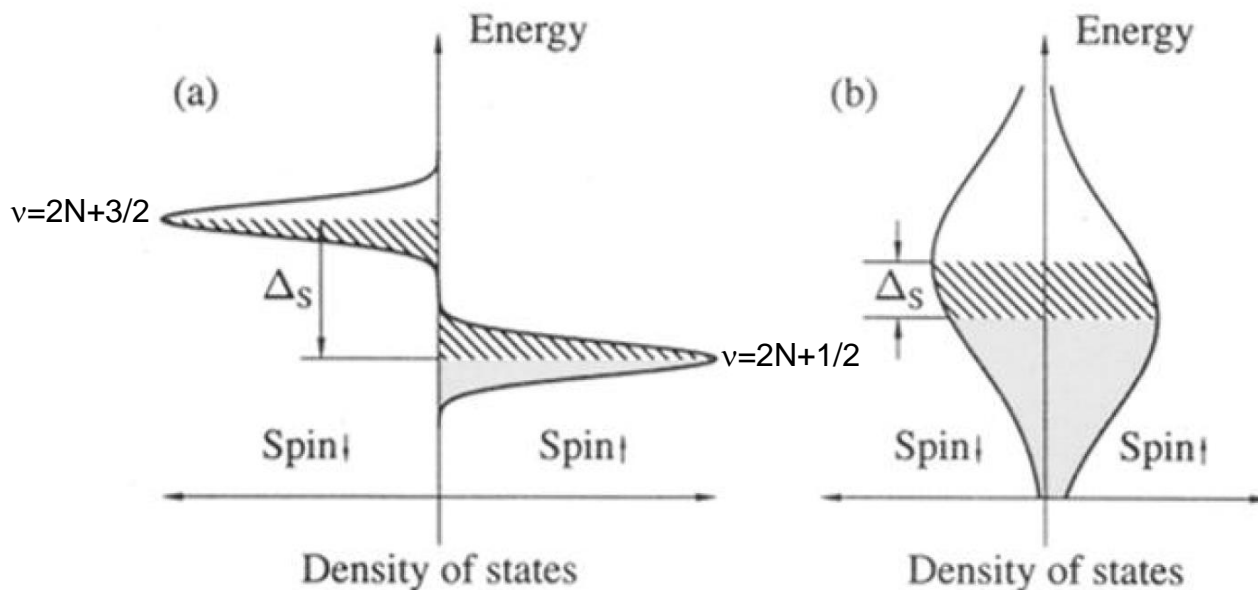
E_{ex} is the exchange parameter

n_{\uparrow} , n_{\downarrow} are the occupation factors of the spin levels.



disorder-induced destruction of exchange enhancement

Fogler and Shklovskii [PRB **52**, 17366 (1995)]



width of Landau level $\ll \Delta_s$

width of Landau level $\sim \Delta_s$

$$\Delta v = 1$$

$$\Delta v \rightarrow 0$$

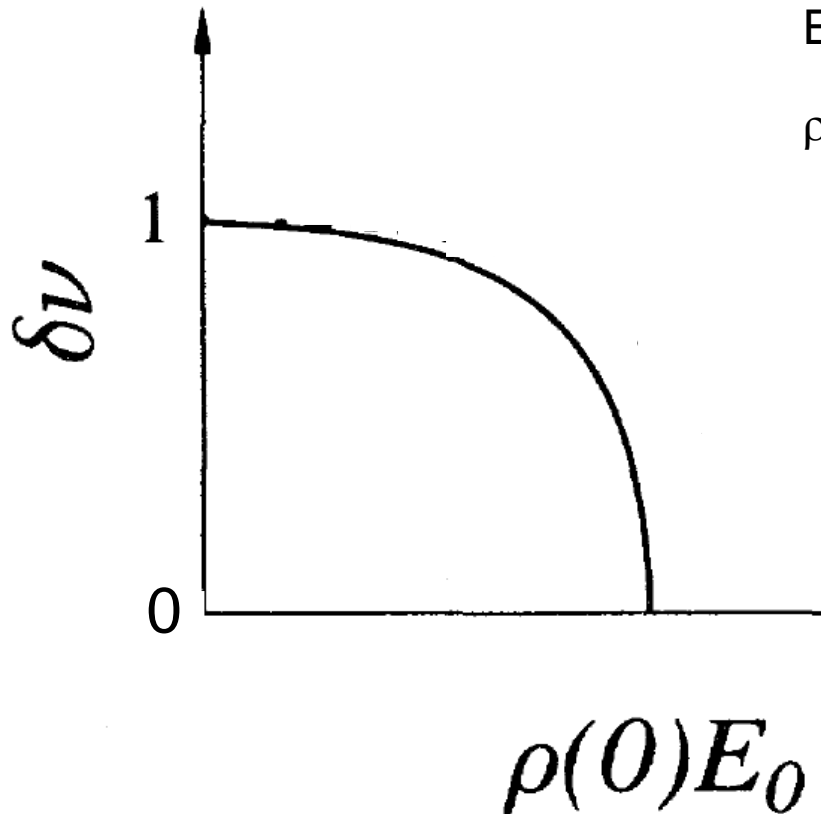
Δv = the Landau level filling between spin-up and spin-down bands

a second-order phase transition

$$\rho(0) = \hbar^{-1} \sqrt{(2/\pi)(\tau/\omega_c)}$$

$$E_0 \propto \hbar\omega_c$$

$$\rho(0)E_0 \propto (\mu B)^{1/2}$$



theoretical prediction

Fogler and Shklovskii [PRB 52, 17366 (1995)]

In high mobility GaAs/AlGaAs heterostructures:

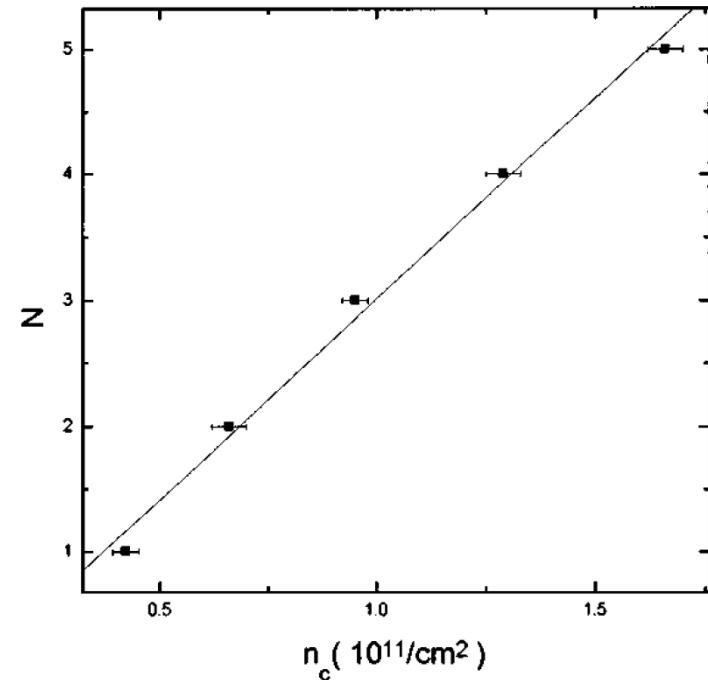
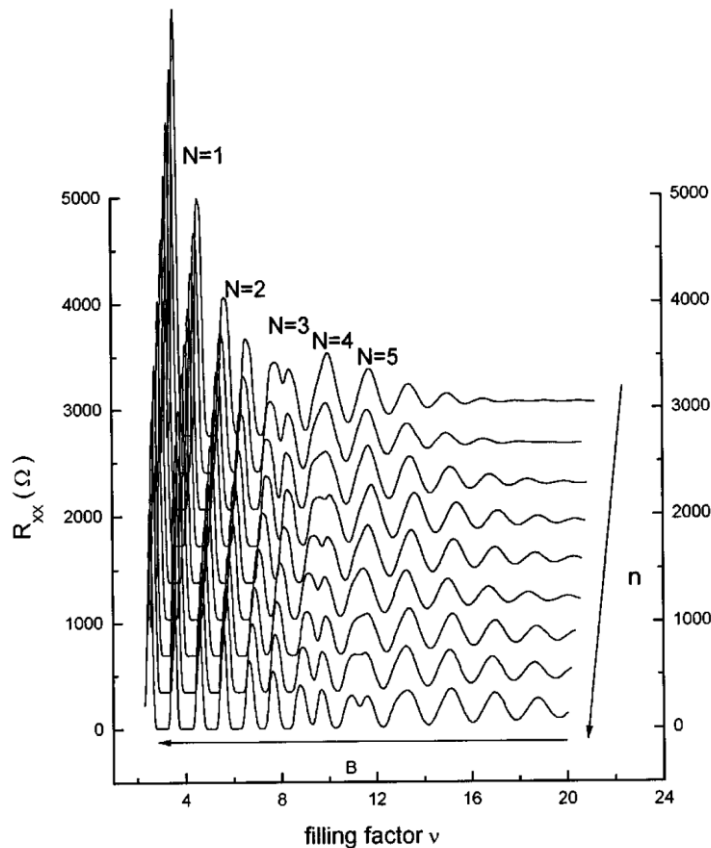
$$N_c = \begin{cases} \sqrt{8\pi} \alpha^2 n^{3/2} n_i^{-1} = 0.02d \frac{n^{1/2} \ln^2(8\pi n a_B^2)}{n_i a_B^2}, & n \gtrsim n_* & (4a) \\ 0.9d \frac{n^{5/6}}{n_i^{1/3}}, & n_i \lesssim n \lesssim n_* & (4b) \\ 0.9d \frac{n^{2/3}}{n_i^{1/6}}, & n \lesssim n_i, & (4c) \end{cases}$$



low density regime: $N_c \propto n^{2/3}$

previous experimental work

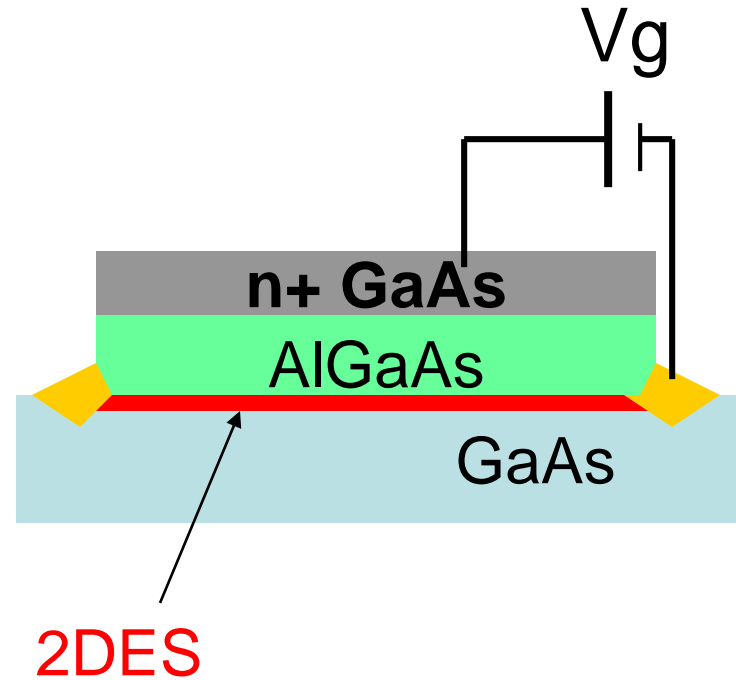
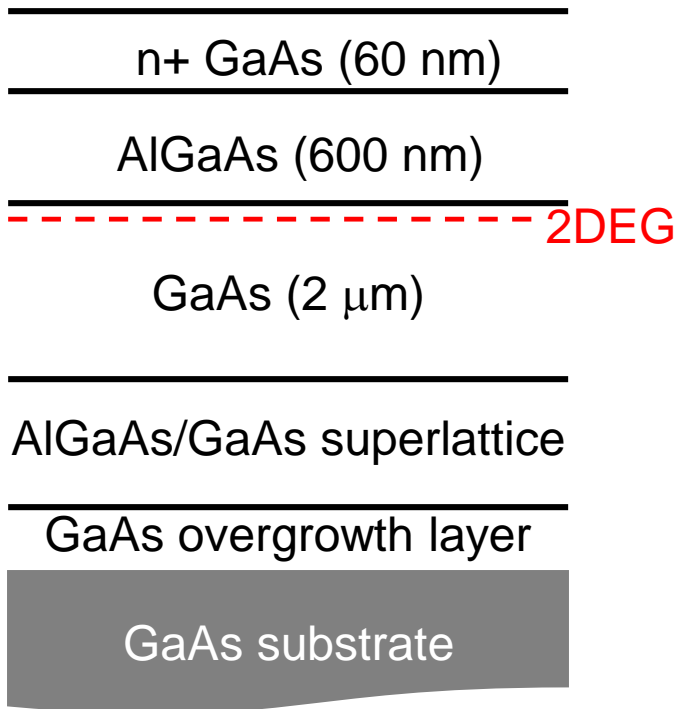
Wong, Jiang, Palm, and Schaff, PRB **55**, R7343 (1997).

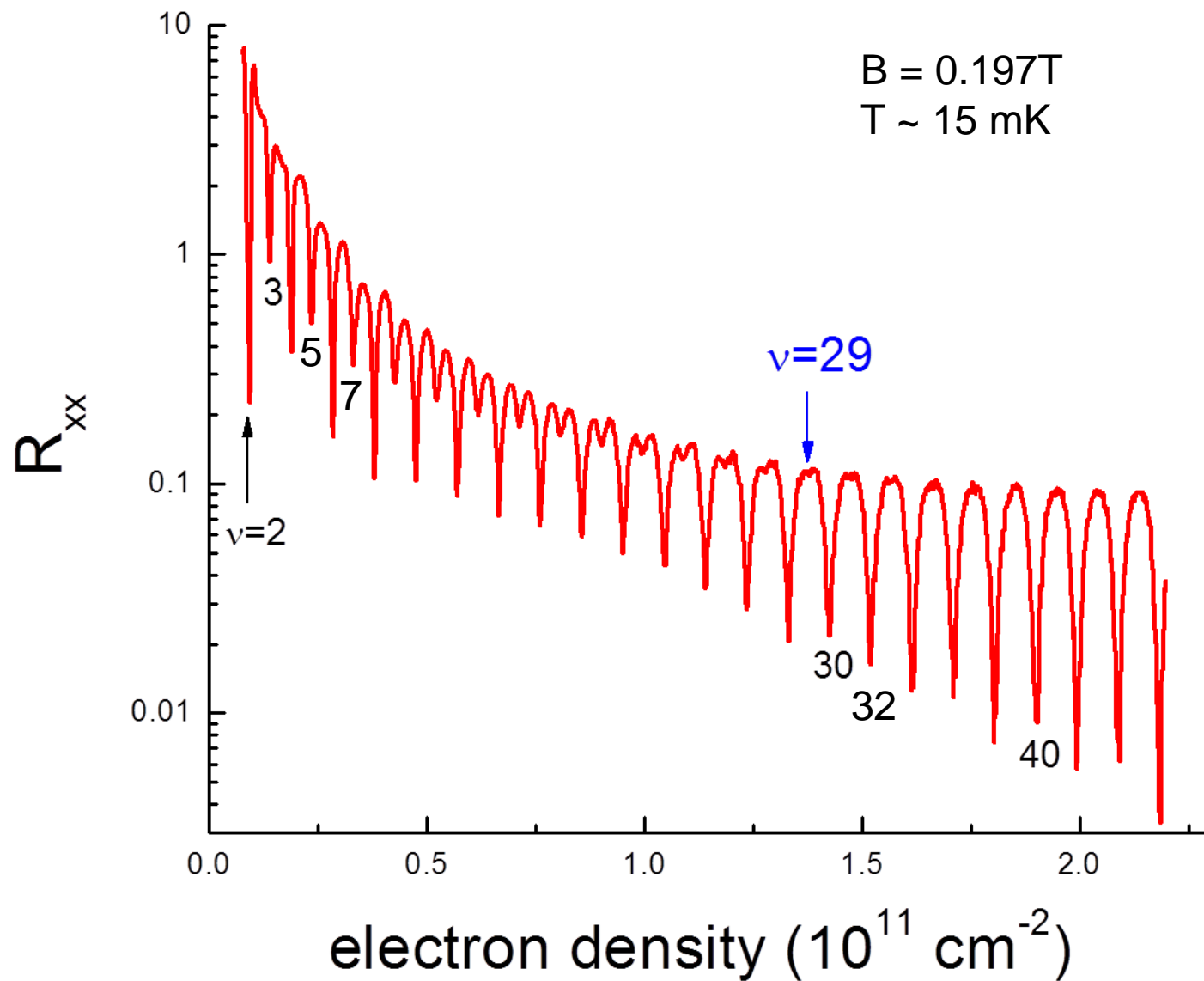


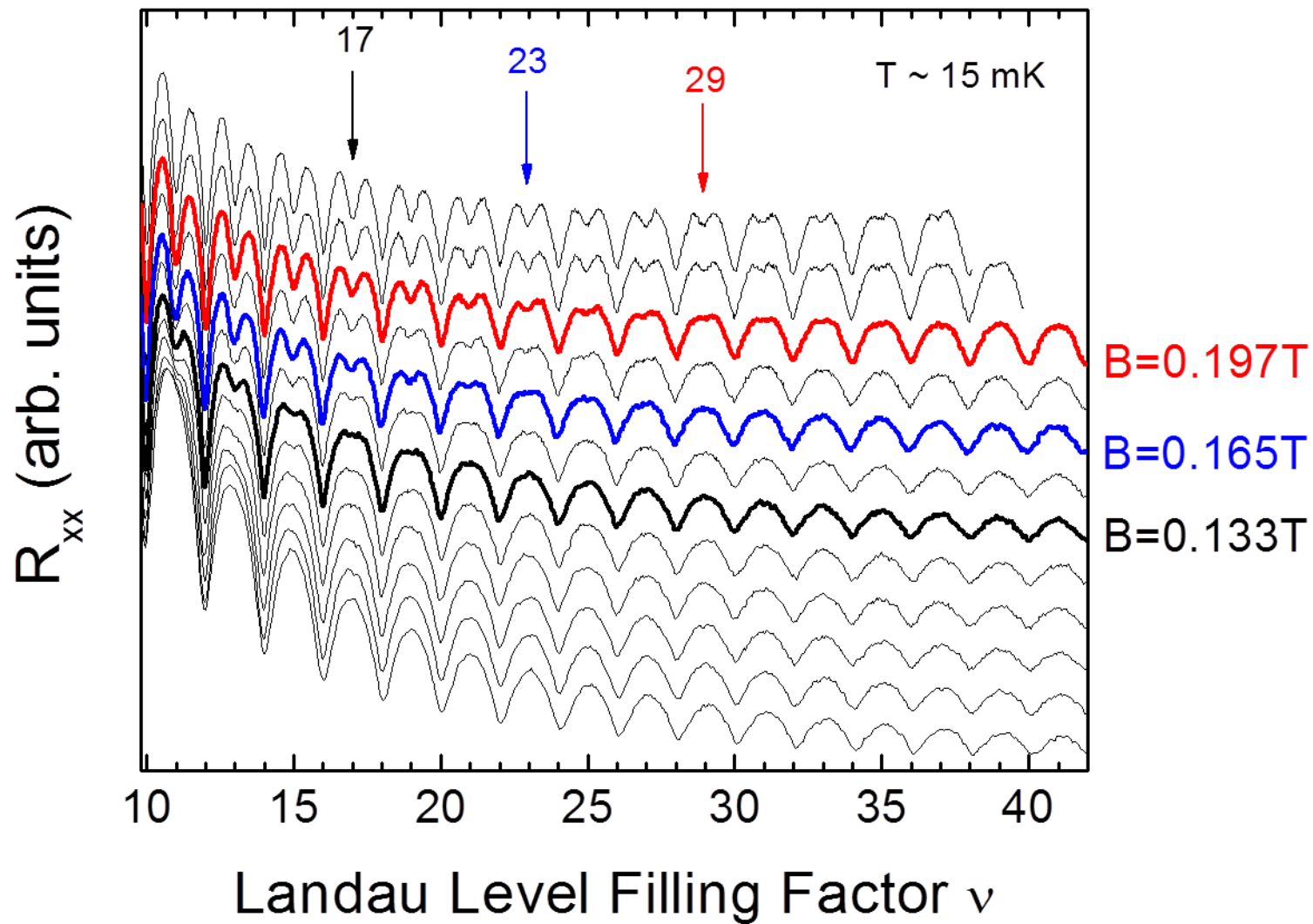
sample peak mobility $< 10^6 \text{ cm}^2/\text{Vs}$

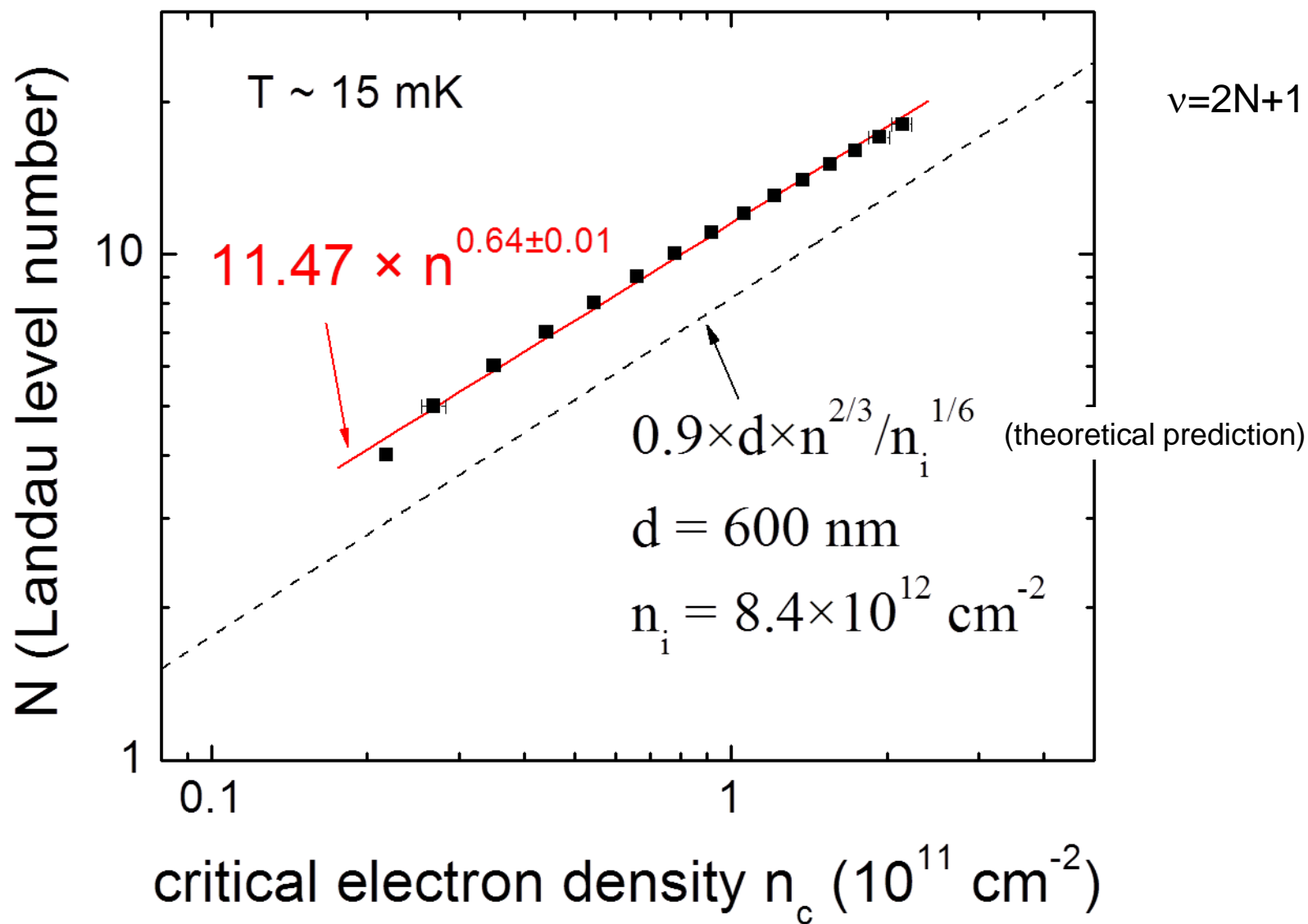
HIGFET

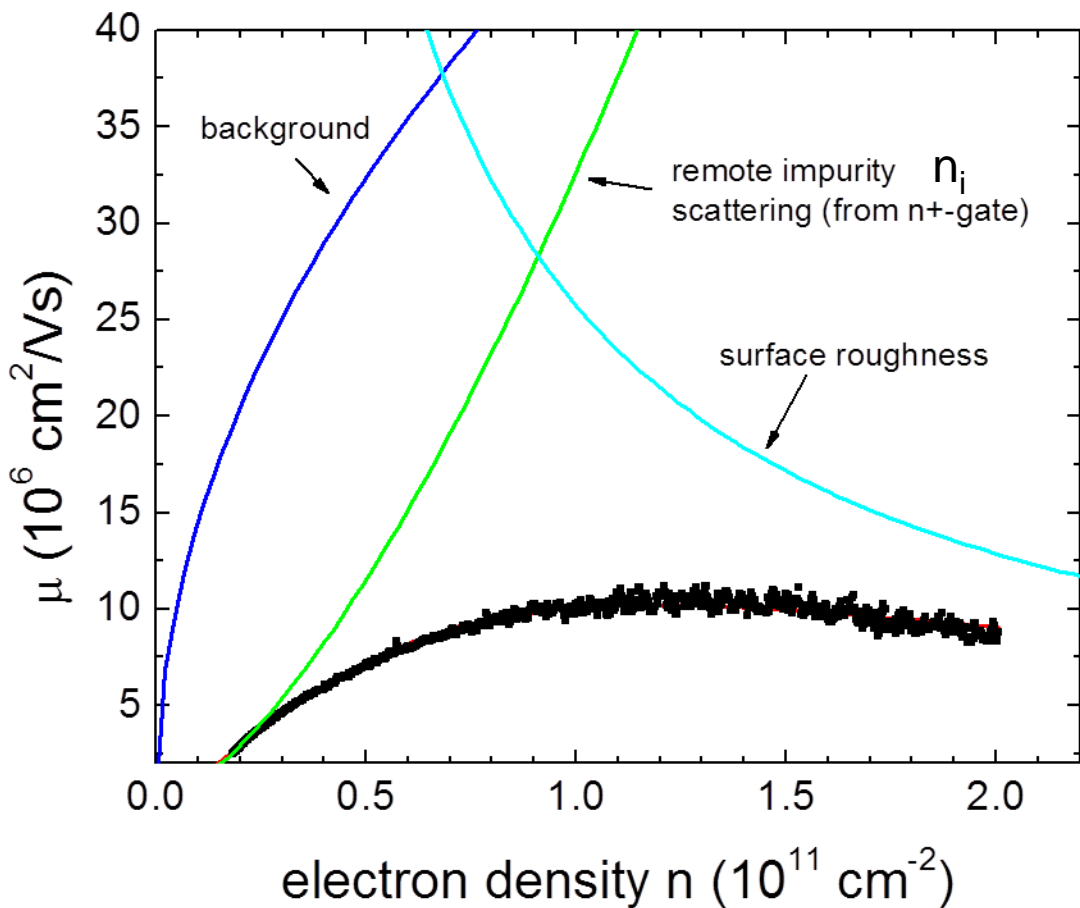
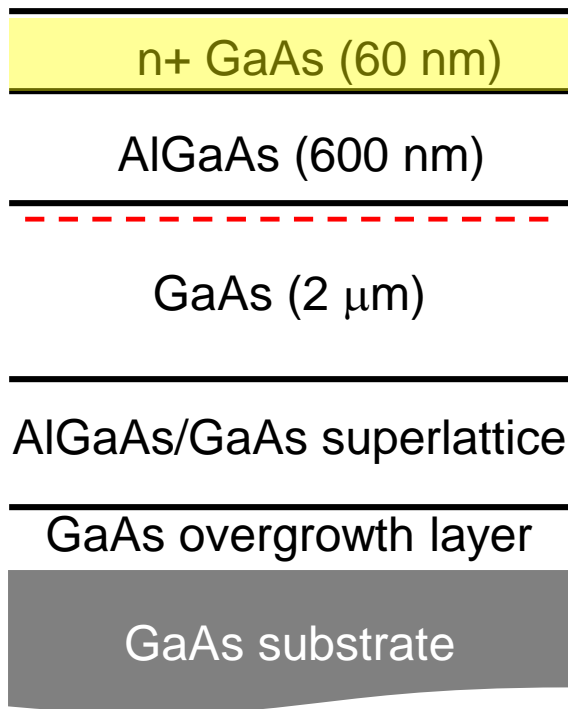
high mobility down to low densities

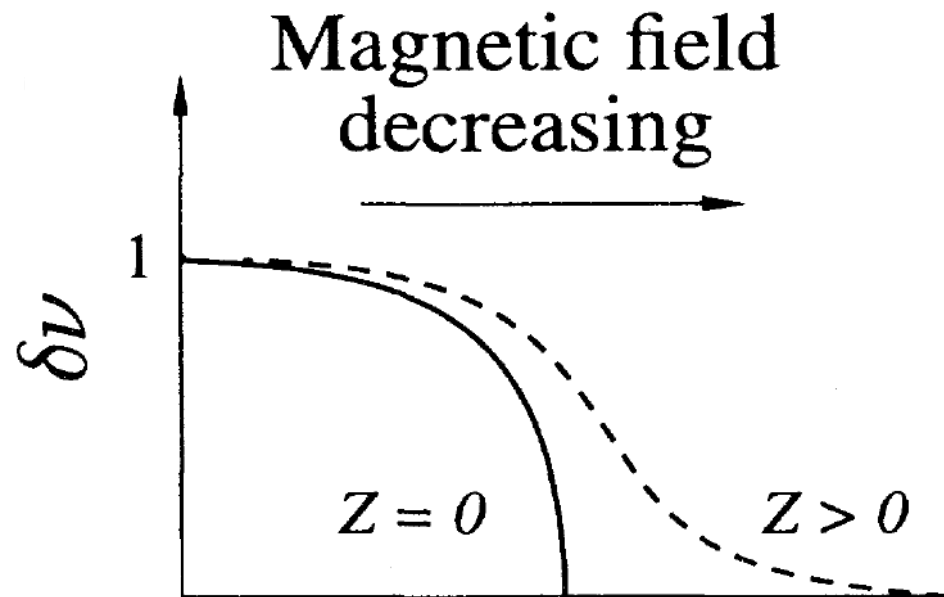
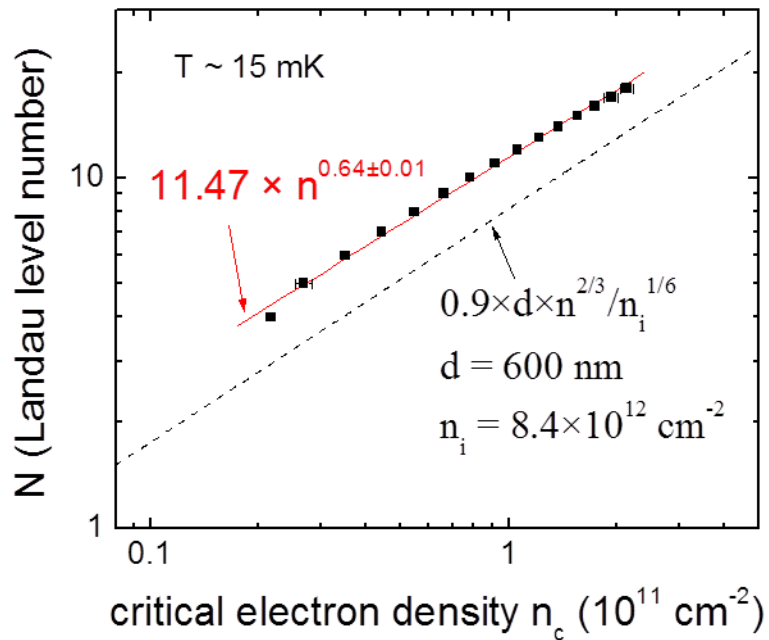












Fogler and Shklovskii [PRB 52, 17366 (1995)]

part II conclusion

In a high-quality HIGFET, the Landau level number N follows a power-law dependence on the 2DEG electron density n , where the spin splitting collapses.

$$N = 11.47 \times n^{0.64 \pm 0.01}$$

This power-law dependence is in a good agreement with the theoretical prediction in the low-density regime.

Thank you for your attention