

# Nuclear Magnetic Resonance

– From Basic Physics to Biomedical Applications



Tai-huang Huang  
Inst. Biomedical Sciences, Academia Sinica  
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# Outline

1. **The Dawn of NMR** – It is all Physics.
2. **Exploiting the power of NMR** – A party for all.  
Chemistry, biology, material science, and medicine.
3. **Manipulation of nuclear spins** – Spin gymnastics.
4. **Biomedical applications** – Work from our lab.
  - Packaging of SARS CoV nucleocapsid.
  - Mechanism of SUMO mediated signal transduction.
  - Macromolecular dynamics in solid and solution.
5. **Look back on a wonderful journey.**

# 1. The Dawn of NMR – A fertile ground for physicists

- 1924 Pauli proposed the presence of nuclear magnetic moment to explain the presence of hyperfine shift in atomic spectra.
- 1930 Nuclear magnetic moment was detected using the refined Stern–Gerlach experiment by Estermann.
- 1939 Rabi et al first detected nuclear magnetic resonance by applying rf energy to a beam of hydrogen molecules.
- 1946 Purcell et al at Harvard reported nuclear magnetic absorption in parafilm wax.  
Bloch et al at Stanford reported nuclear magnetic resonance phenomenon in liquid water.
- 1940s–60s NMR theories were developed by physicists.

## 2. Exploiting the power of NMR – A party for all

1949 Chemical shift phenomenon was observed.

### 1960s

- Ernst and Anderson introduced Fourier Transform technique into NMR that increased NMR sensitivity by orders of magnitude.
- Solid state NMR was revived due to efforts of Waugh at MIT.  
Application to material and polymer science insoluble proteins etc.
- Biological application became possible due to the introduction of superconducting magnet and high power computers.
- NMR imaging was demonstrated (Lauterbur at Stony Brook).

### 1970s

- Development of multi-dimensional NMR (Jeneer, Ernest, Bax ..)
- Development of methodologies for determining macromolecular structure (Wüthrich).

## 1980s and beyond – Exploding applications.

- Methods for characterizing macromolecular structure/dynamics in solution matured.
- Macromolecular structures in solid and gel states become feasible.
- Material science: Zeolites, polymers, **fuel cells** etc. (Clare Grey in Cambridge on Li–Air battery 5x more compact)
- MRI become a powerful clinical imaging modality.
- Functional MRI come to stage.
- Development of several fast NMR methodologies.
- NMR–based Metabolomics.
- .....

## **Non–trivial applications.**

- Each become a sub–discipline by itself.

# Nobel Laureates in NMR



Isador I Rabi,  
Physics 1944



Edward M. Purcell  
Physics, 1952



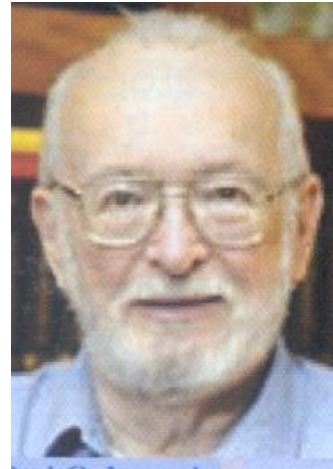
Felix Bloch  
Physics, 1952



Richard R. Ernst  
Chemistry, 1991



Kurt Wüthrich  
Chemistry, 2002

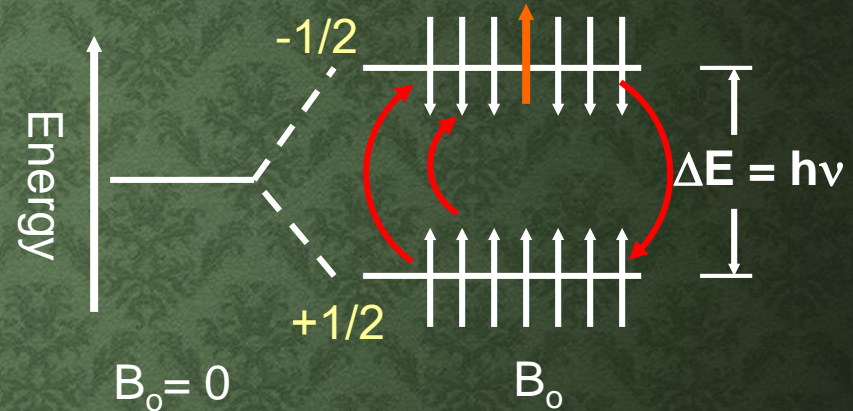
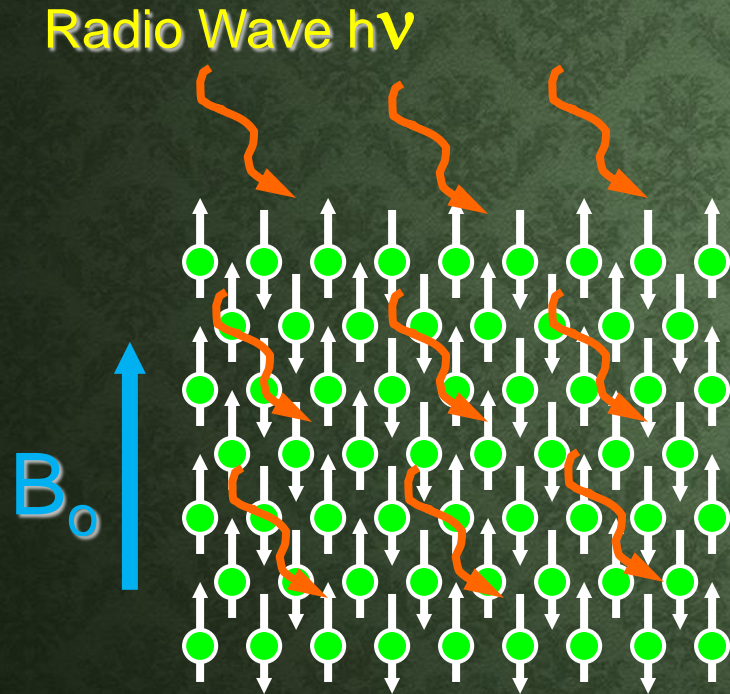


Paul C. Lauterbur  
Physiol. Medicine, 2003



Peter Mansfield  
Physiol. Medicine, 2003

# NMR Spectroscopy



Larmor Equation ( $I = 1/2$ ):

$$\nu = \gamma B_0 / 2\pi$$

$\nu$  = Larmor frequency

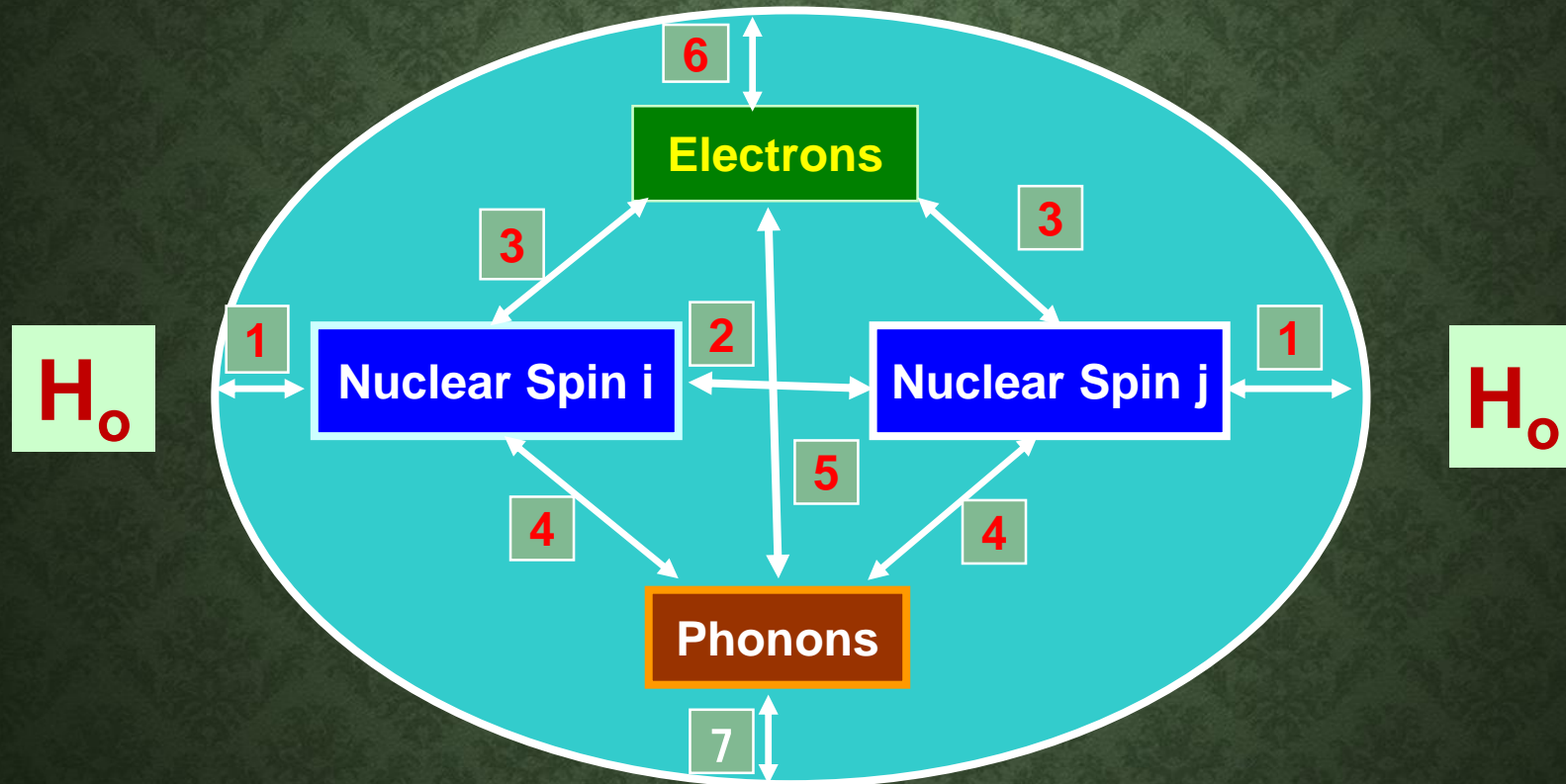
$\gamma$  = nuclear gyric ratio

$B_0$  = magnetic field strength

Biologically interested nuclei:

$^1\text{H}$ ,  $^{13}\text{C}$ ,  $^{15}\text{N}$ ,  $^{19}\text{F}$ ,  $^{31}\text{P}$  ( $S=1/2$ ),  $^2\text{D}$  ( $S=1$ )

# Basic Nuclear Spin Interactions



**Dominant Interactions:**  $H = H_Z + H_{CSA} + H_D + H_Q + H_J + \dots$

$H_Z$  : Zeeman Int.;  
 $H_D$  : Dipolar Int.

$H_{CSA}$  : Chemical Shielding Anisotropic Int.;  
 $H_Q$  : Quadrupolar Int.       $H_J$  : J-Coupling



# Basic Nuclear Spin Interactions

## Zeeman Interaction ( $H_z$ ) (Field depend);

Interaction of nuclear spin with external magnetic field .

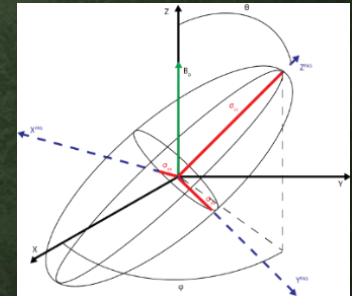
$$H_Q = -\gamma I_z \cdot B_0$$

## Chemical Shielding Anisotropic Interaction ( $H_{CSA}$ ) (Field dep.);

The nuclear shielding effect of an applied magnetic field, caused by an induced magnetic field resulting from circulation of surrounding electrons

$$H_{CSA} = -\gamma I \cdot \sigma \cdot B_0$$

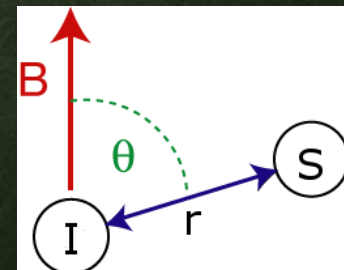
$$\sigma = \begin{pmatrix} \sigma_{xx} & \sigma_{xy} & \sigma_{xz} \\ \sigma_{yx} & \sigma_{yy} & \sigma_{yz} \\ \sigma_{zx} & \sigma_{zy} & \sigma_{zz} \end{pmatrix}$$



## Dipolar Interaction ( $H_D$ ) (Thru space) (Field indep):

Interaction between adjacent nuclear spins through magnetic dipolar field.

$$H_D = \frac{\hbar\gamma_I\gamma_S}{4\pi^2 r_{IS}^3} [1 - 3 \cos^2 \theta] (3I_z S_z - \vec{I} \cdot \vec{S})$$



## Quadrupolar Interaction ( $H_Q$ ) : (Field indep)

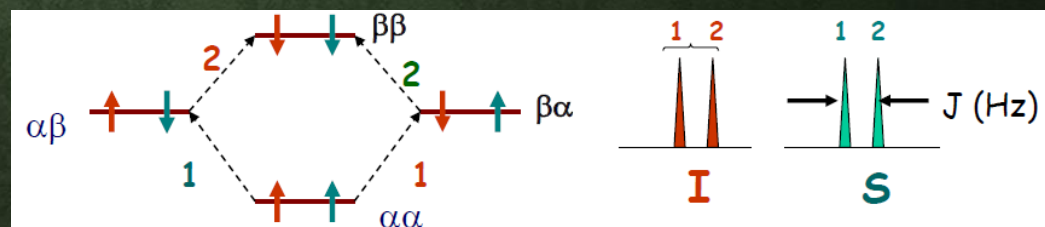
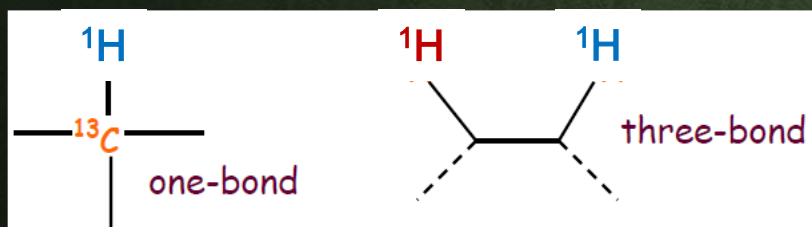
Nuclei with spin  $> 1/2$  have a asymmetric distribution of nucleons (non spherical distribution of positive electric charge)

$$H_Q = I \cdot V \cdot I$$

$$V = \begin{bmatrix} V_{xx} & V_{xy} & V_{xz} \\ V_{yx} & V_{yy} & V_{yz} \\ V_{zx} & V_{zy} & V_{zz} \end{bmatrix}$$

## J-Couplings (Thru bond connection) : ( Field indep)

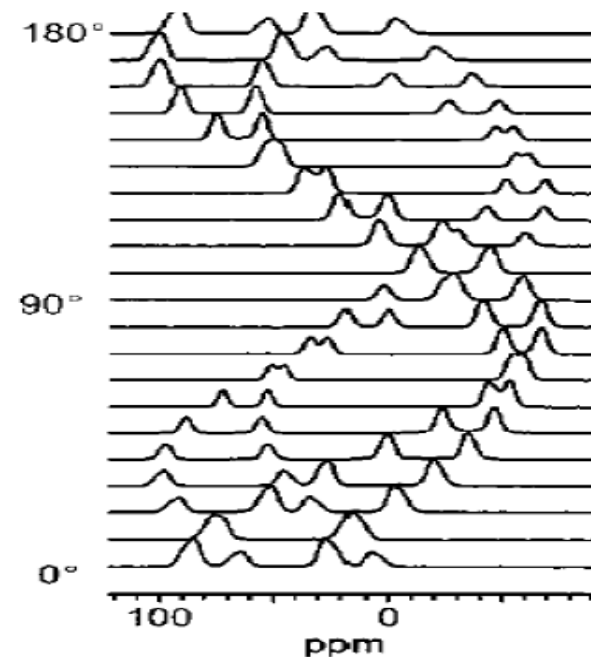
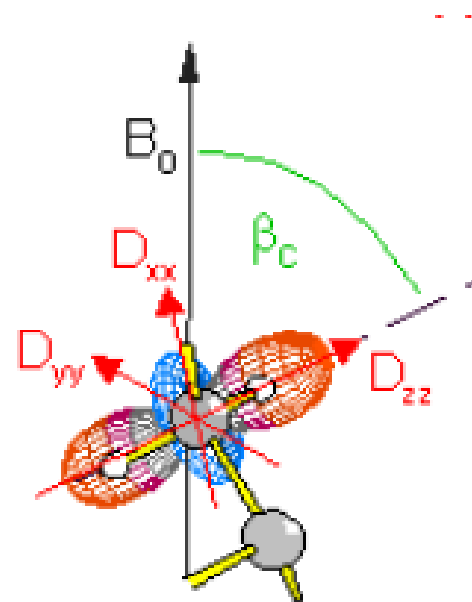
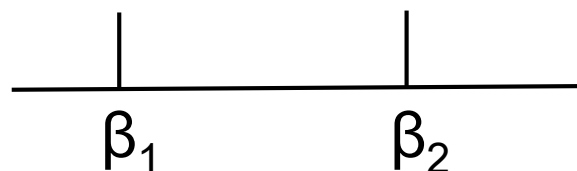
Resonance splitting mediated through chemical bonds connecting two spins. It is an indirect interaction between two nuclear spins which arises from hyperfine interactions between the nuclei and local electrons.



Interaction	Magnitude (Hz) ( <sup>1</sup> H at 2.1T)
Zeeman	10 <sup>8</sup>
Quadrupole	10 <sup>6</sup>
Chemical shift	10 <sup>3</sup>
Dipole	10 <sup>3</sup>
J-Coupling	10

The resonance frequency of a nuclear spin in single crystal depends on the orientation of the tensorial interaction w.r.t. the magnet field.

Single crystal



# NMR spectrum of samples in solid states

## Powder patterns

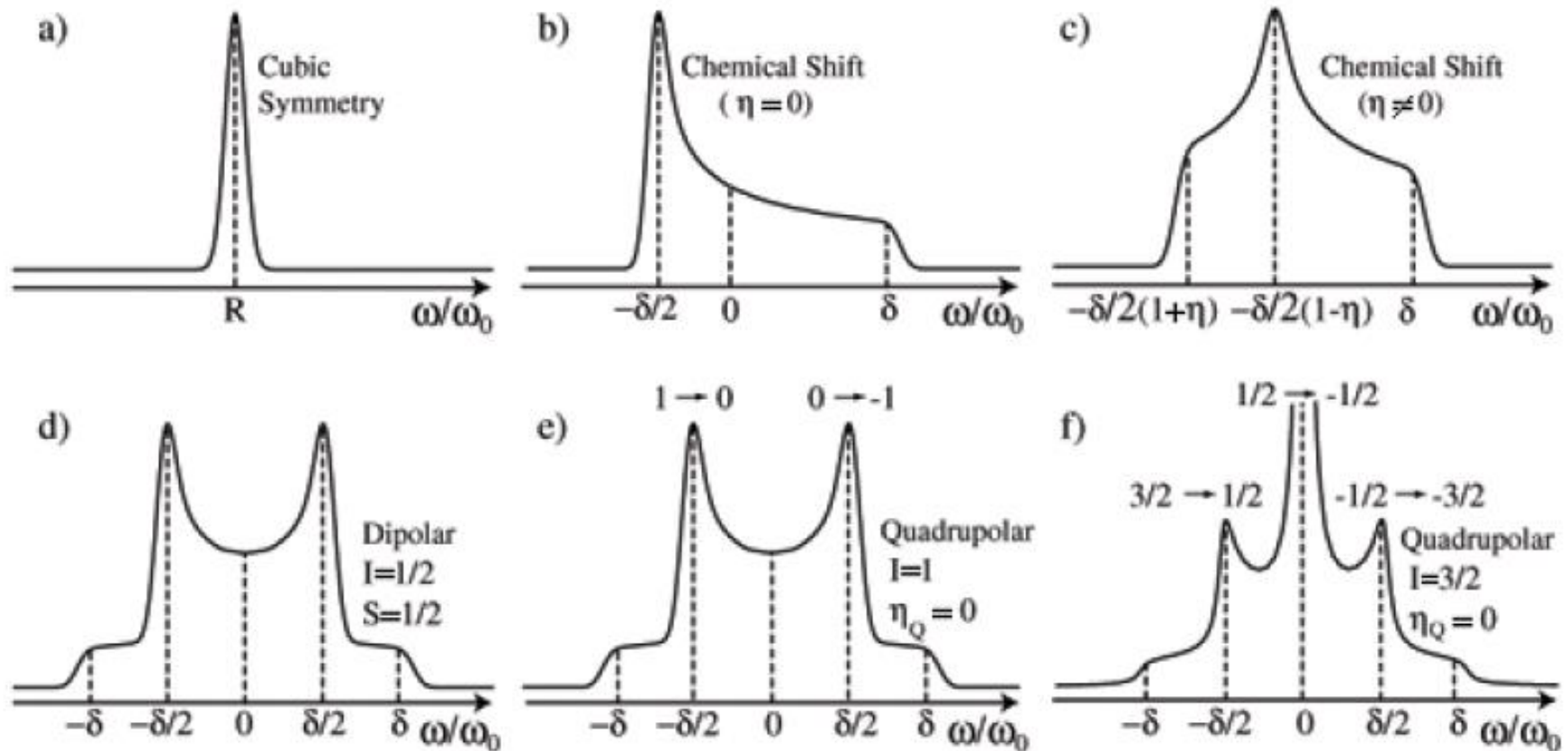
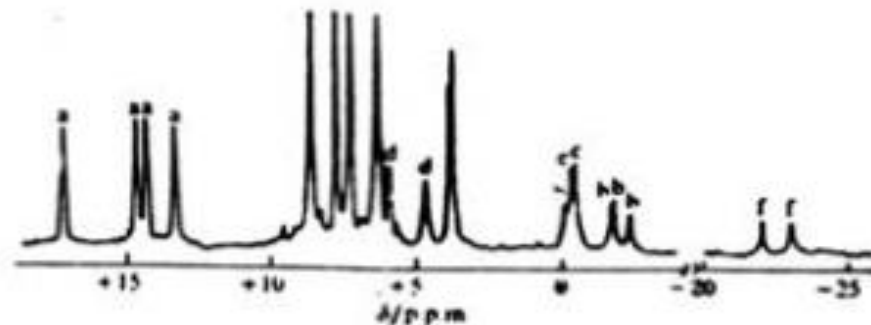


FIG. 1: Calculated NMR spectra of polycrystalline or amorphous samples (powder patterns) corresponding to different NMR interactions: a-c) Chemical Shift under different symmetry conditions; d) Dipolar interaction between two spins  $1/2$  distant each other by a fixed distance; and e-f) Quadrupolar interaction for spins  $1$  and  $3/2$ .

# NMR spectra of samples in different states

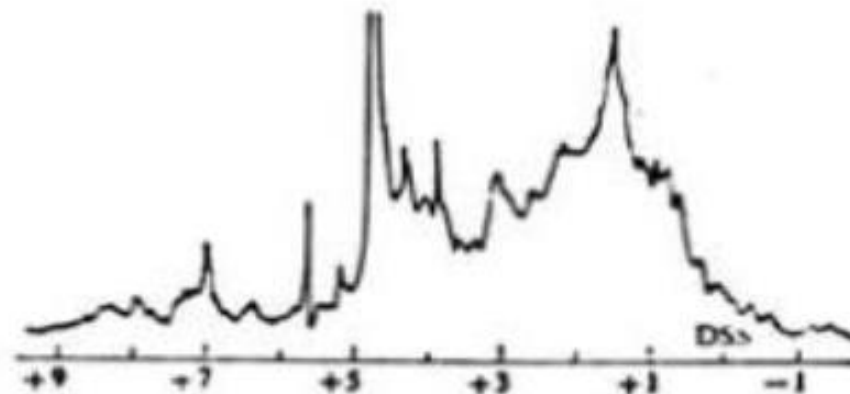
## Small molecules in solution

$\langle H_D \rangle = \langle H_Q \rangle = 0$   
 $\langle H_{CSA} \rangle = \sigma_{iso}$ ;  $\langle H_J \rangle = J_{iso}$   
Well-resolved sharp lines

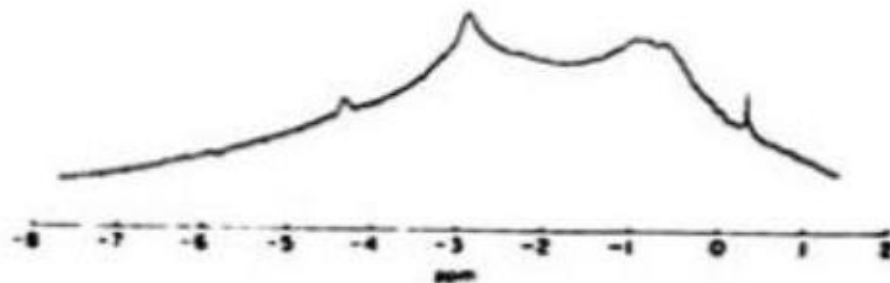


## Macromolecules

(Slow tumbling)  
Broad overlapping



**Gel state**  
(Featureless humps)



1. NMR spectra contains rich information derived from the presence of multiple interactions.
2. Each interaction provide insights into the structure/dynamics of the spin system.
3. It is difficult to quantify the interaction when there are more than one present.

## Question:

How to extract the inter-twined interactions ?

- ➔ Design special pulse sequences to selectively observe/suppress certain interaction(s)
- ➔ Spin gymnastics

## Example: (HSQC)

(2D Heteronuclear Single Quantum Correlation Spectroscopy)

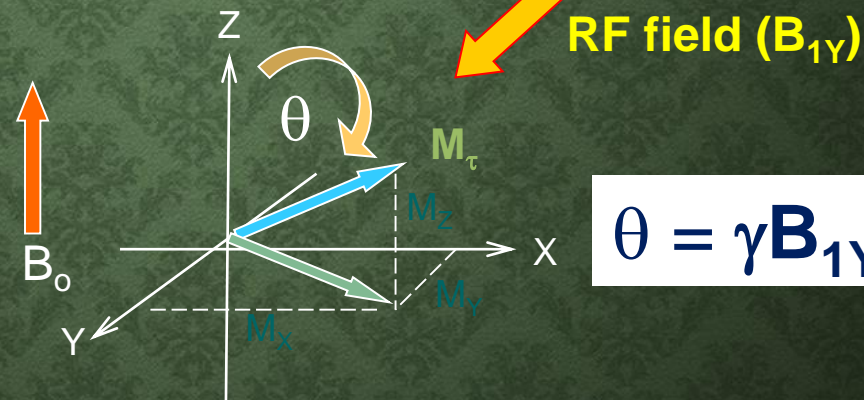
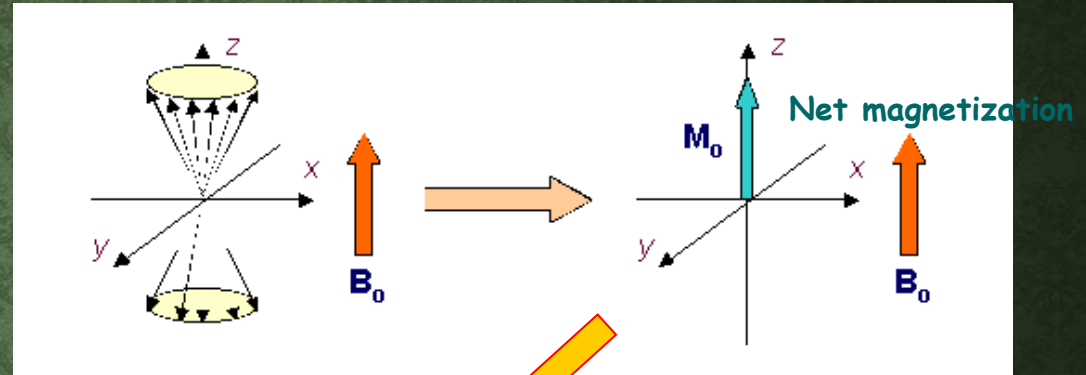
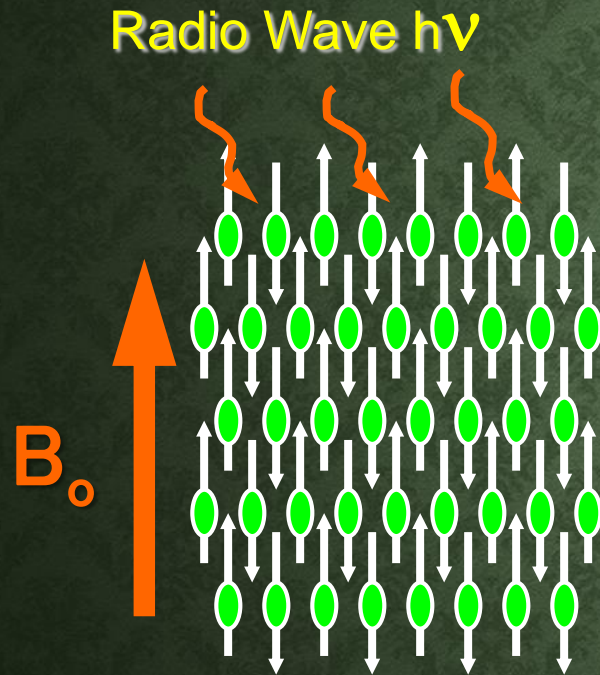
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### Features:

1. Dramatically increased spectral resolution !
2. Dramatically increased sensitivity of insensitive nuclei !  
Enhancement factor  $\propto (\gamma_H / \gamma_I)^3$
3. Opened a door for thru-bond sequential resonance assignment (Thru J-coupling).
4. The idea can be extended to higher dimension to include multiple nuclei and field gradients etc

# NMR Spectroscopy

## Classical view



$$\theta = \gamma B_{1Y} T$$

Magnetization will be flipped around Y-axis toward X-Y plane by an angle  $\theta$ , determined by the RF field strength and the pulse duration.

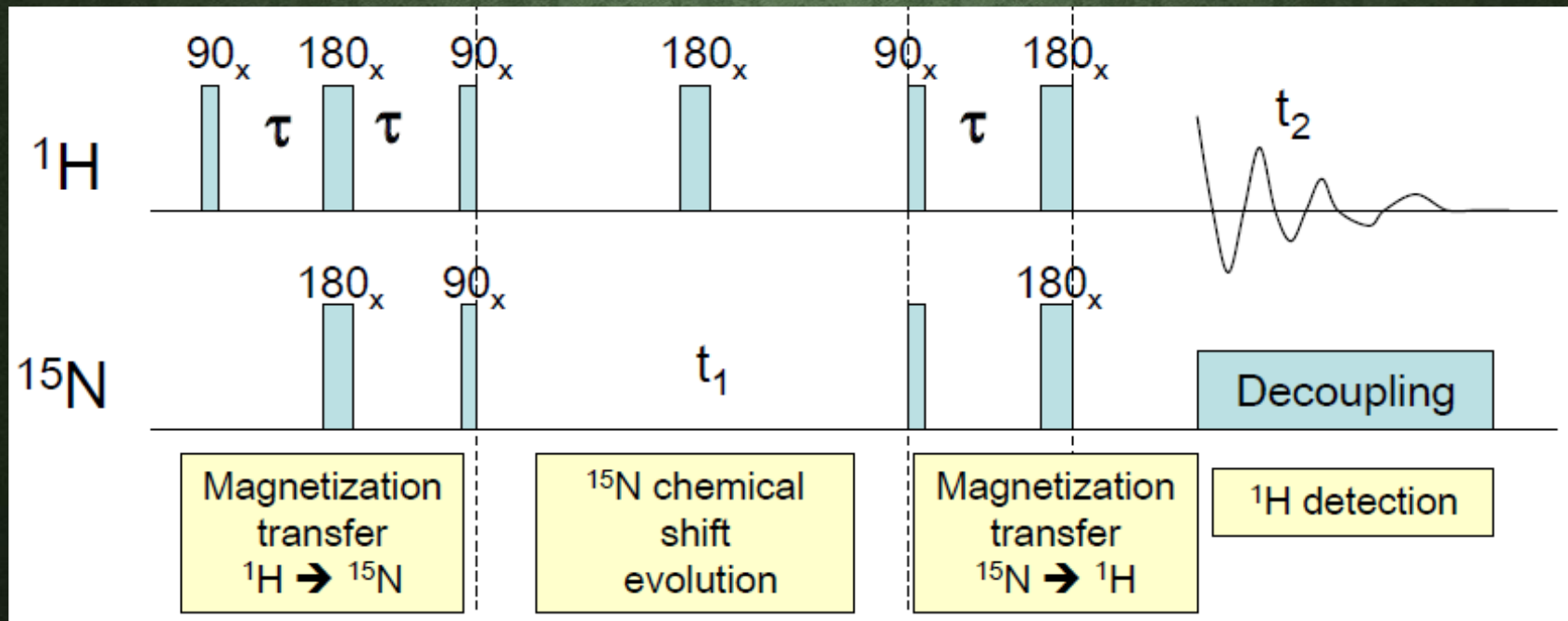
$\theta = 90^\circ$  it is call a  $90^\circ$  pulse or  $\pi/2$  pulse (maximum signal)

$\theta = 180^\circ$  it is call a  $180^\circ$  pulse or  $\pi$  pulse (No signal)



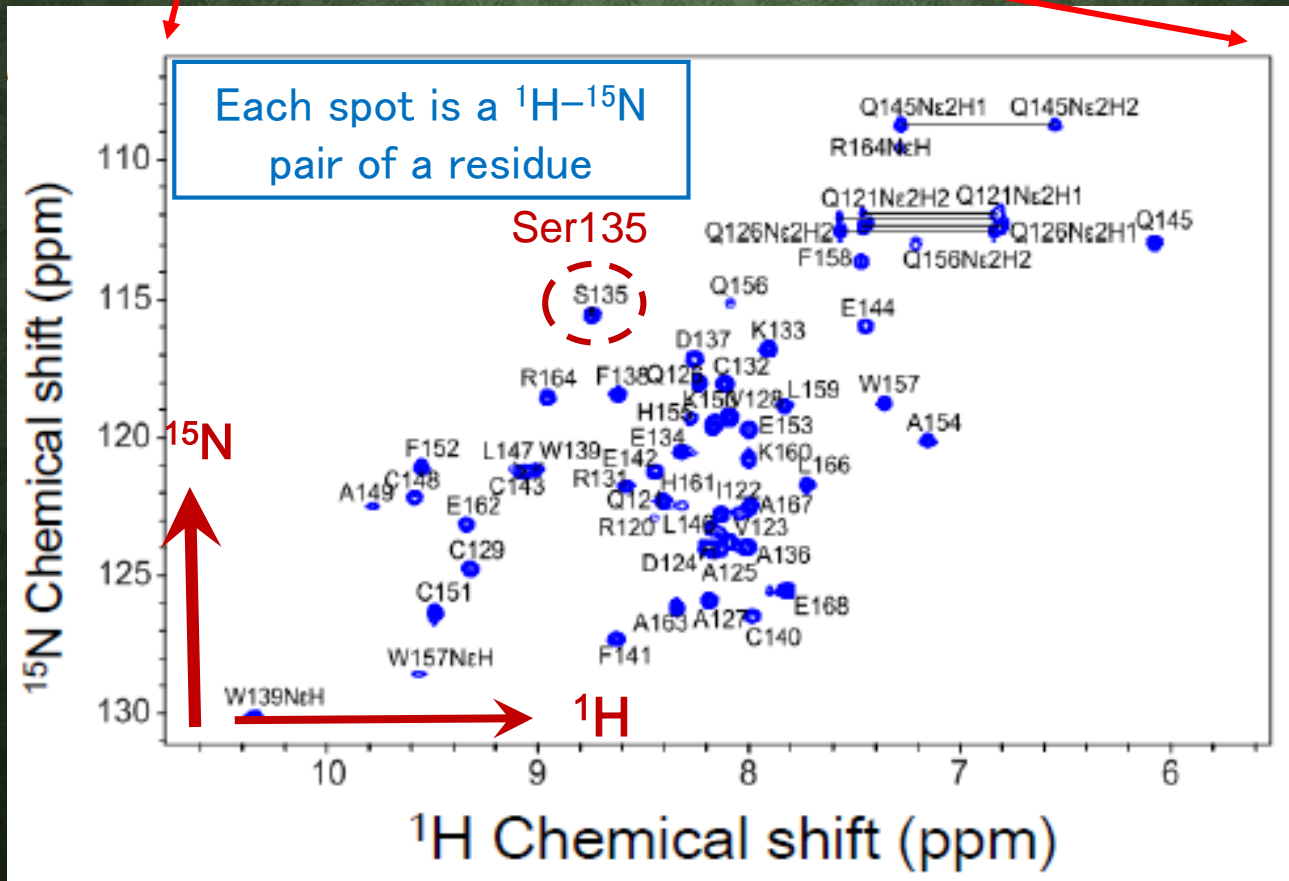
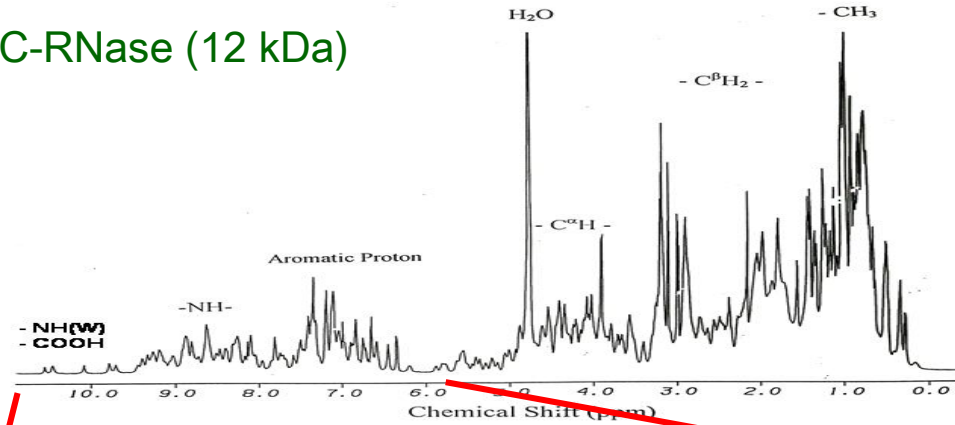
# Pulse sequence for $^{15}\text{N}$ -HSQC expt

Protein peptide chain



Efficiency  $\propto \sin(2\pi J\tau)$ ; Maximum transfer when  $2\pi J\tau = \pi/2$ .

# RC-RNase (12 kDa)



# Biomedical Applications

Molecules → Cell → tissue → Organ → Whole body

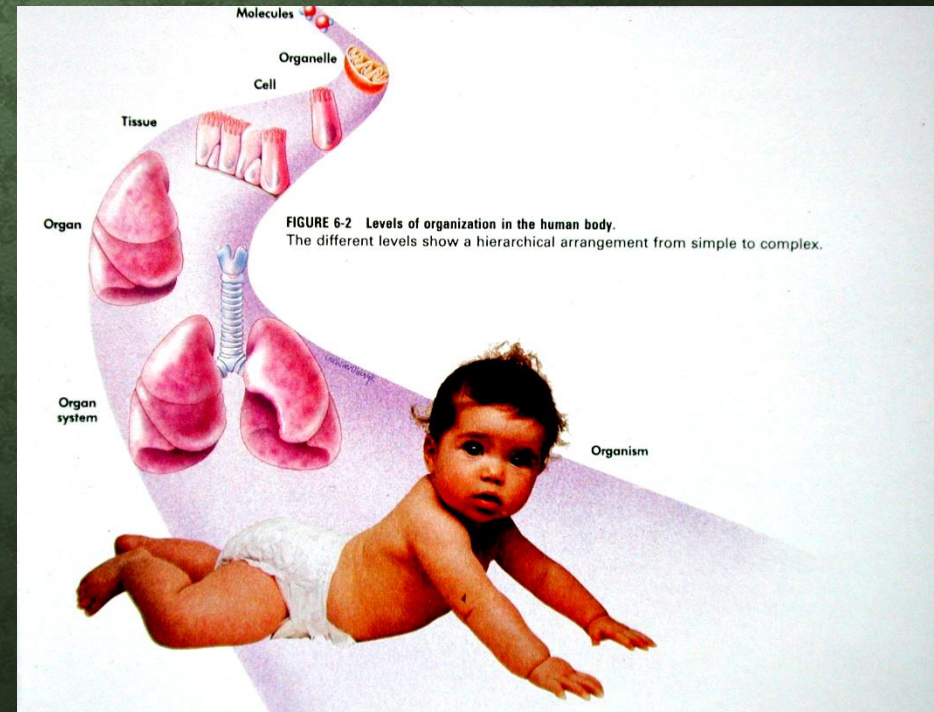
## 1. Chemical Identification:

- A. Identification of metabolites (Metabonomics)
- B. Drug discovery.

## 2. Macromolecular structure:

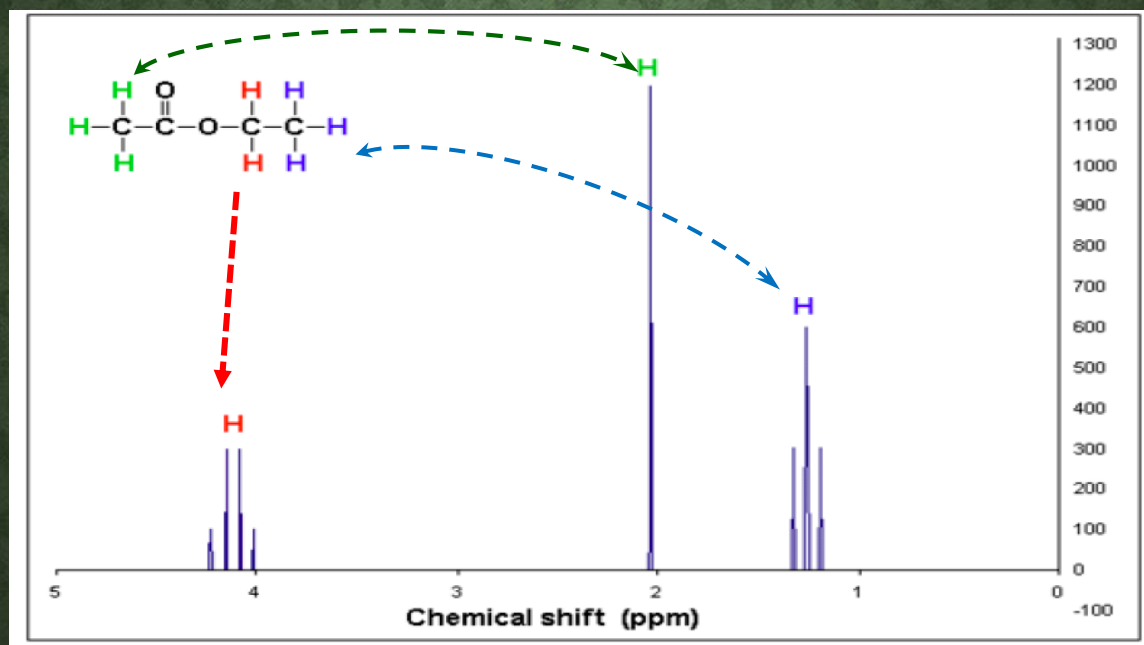
## 3. Macromolecular Dynamics:

## 4. Magnetic Resonance Imaging (MRI):



# 1. Chemical Identification:

Proton spectrum of ethyl acetate



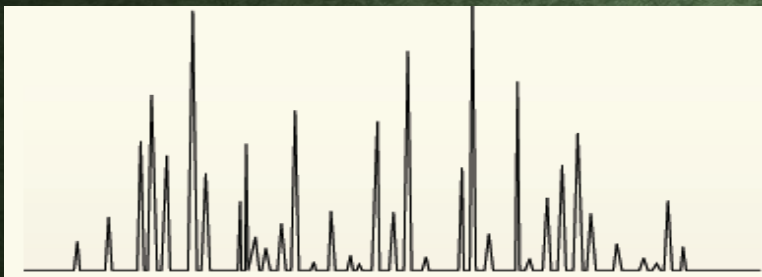
**NMR spectrum is the finger print of a chemical**

→ Organic synthesis, natural product identification etc.

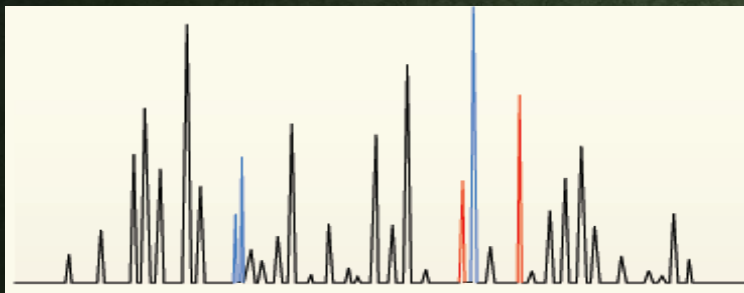
## 2. Metabonomics – (Nicholson and Lindon, Nature 455, 1054, 2008)

Metabonomics aims to measure the global, dynamic metabolic response of living systems to biological stimuli or genetic manipulation. It seeks an analytical description of complex biological samples and to characterize and quantify all the small molecules in such a sample (**Urine, blood, plasma etc**).

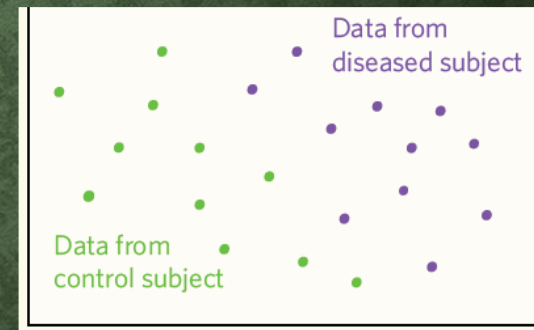
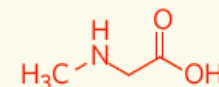
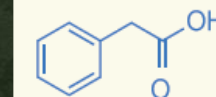
Raw data (Urine, blood etc)



Pattern recognition



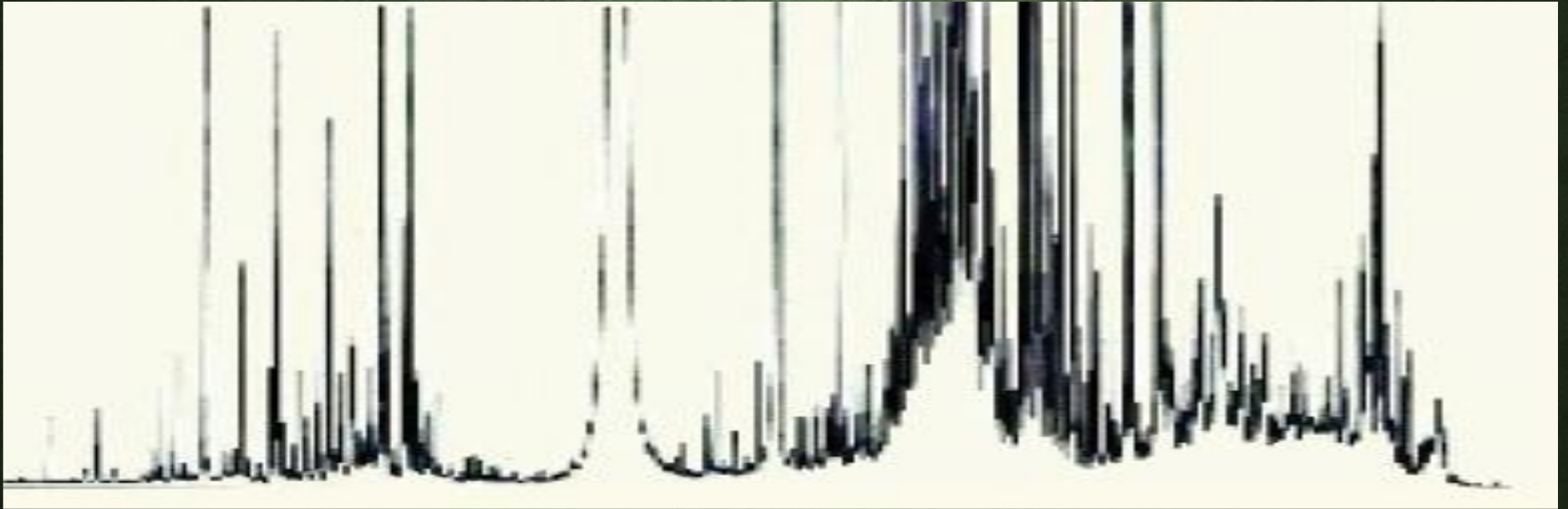
Identify metabolites



Statistical analysis

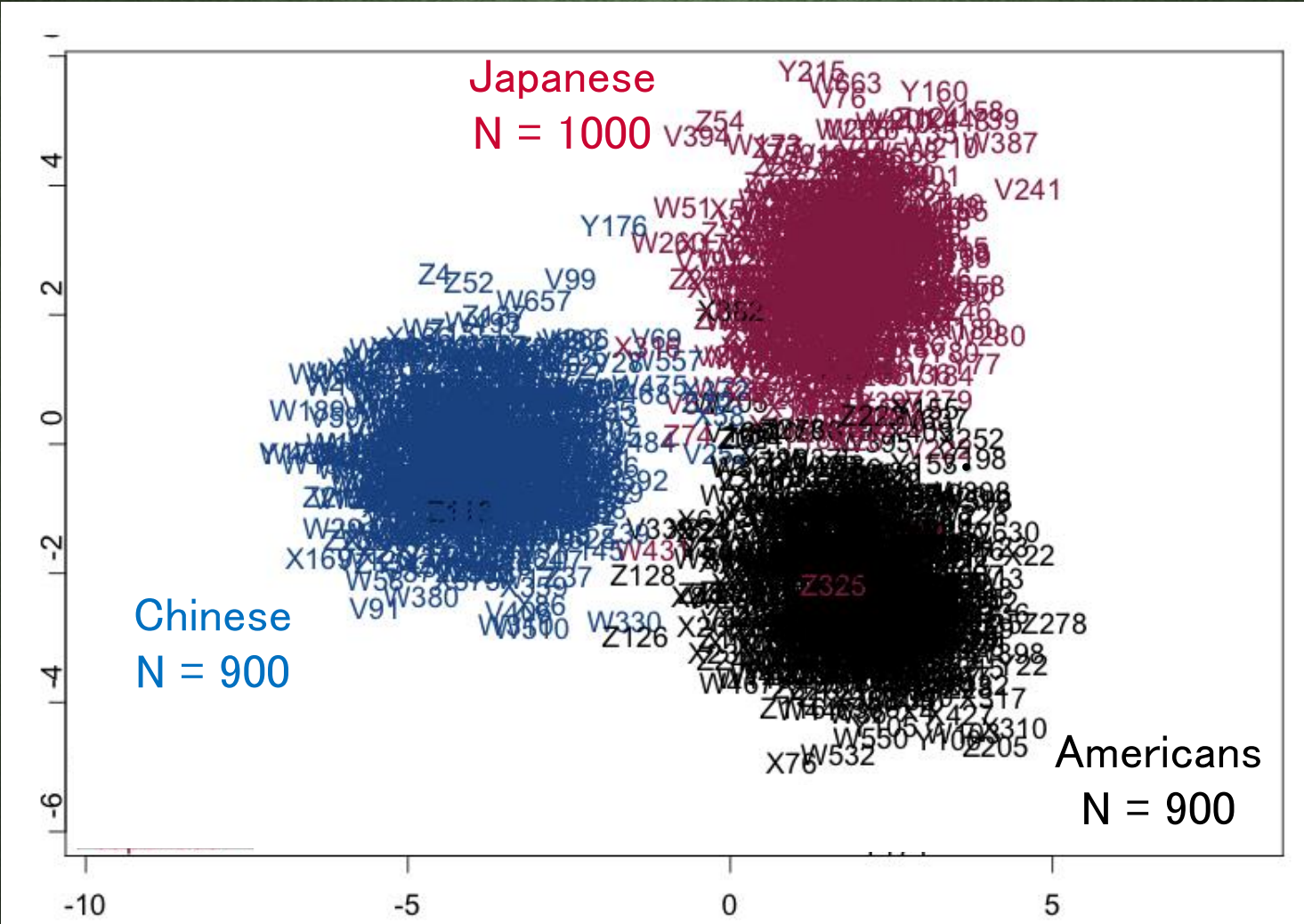


## NMR spectrum of human urine

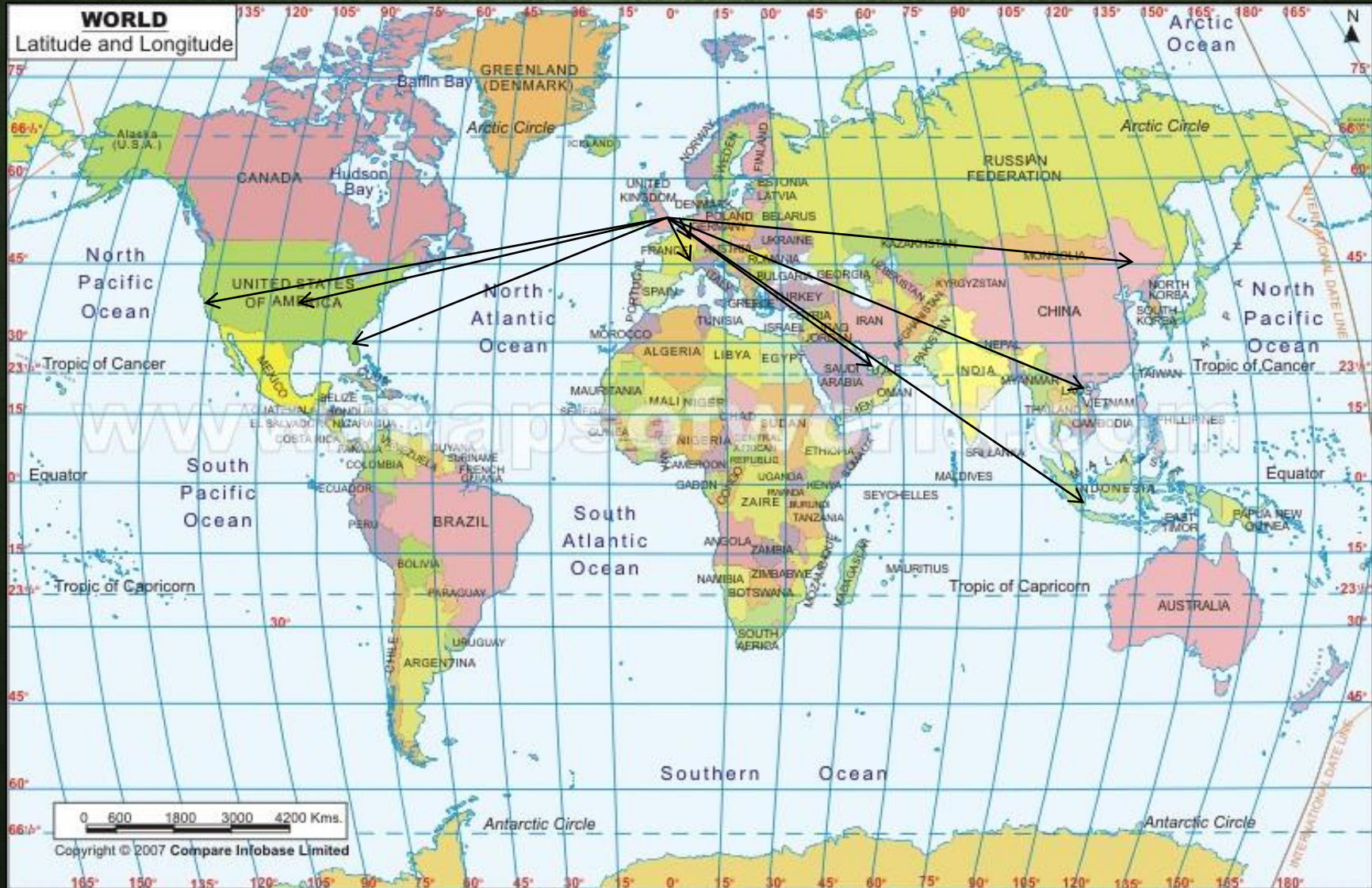


**Very complex !**

Population studies show:  
**Metabolic variation is much larger than genetic variation !**  
(Urinary Metabotypes)



# The World Phenome Center network



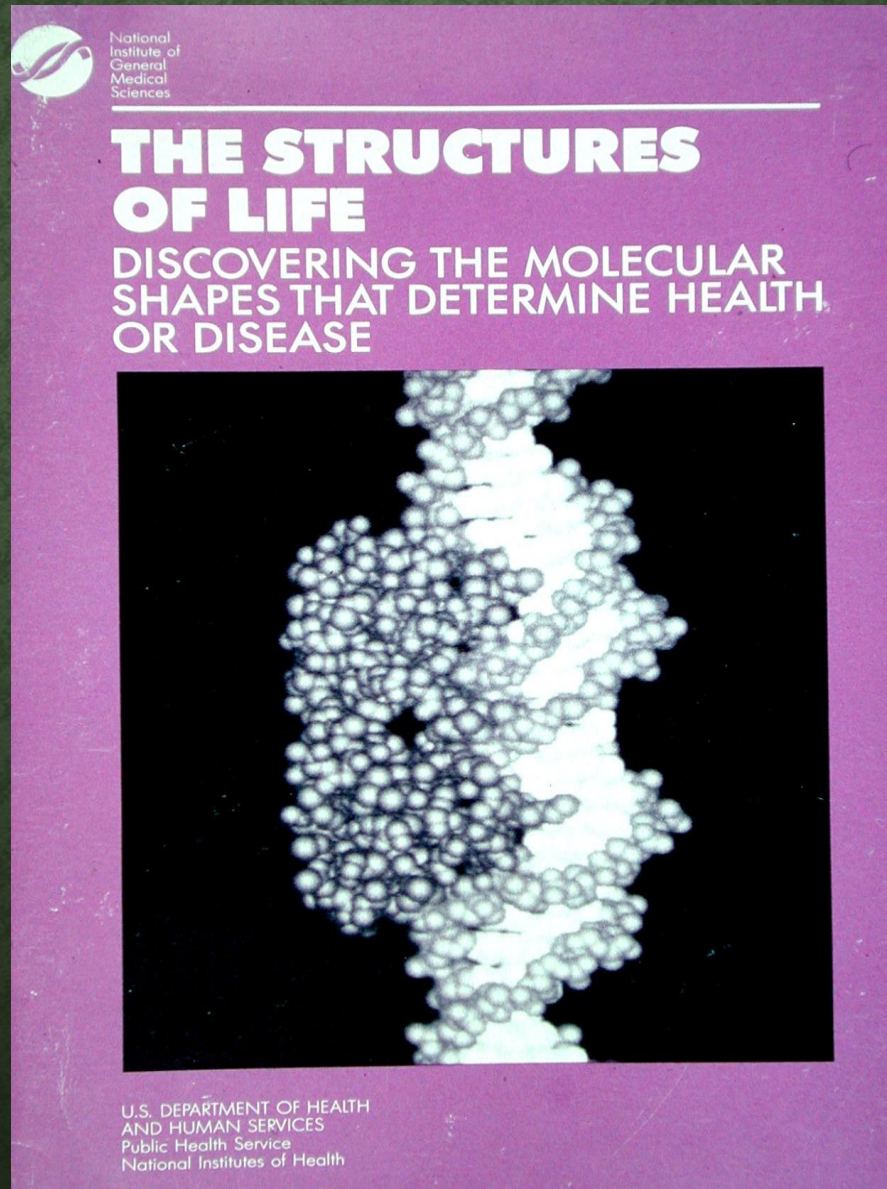


## 中研院台灣人體生物資料庫 (Taiwan Biobank)



- Collect and sequencing 300k samples (200K healthy, 100K patients of various diseases).  
(Already Collected over 60k samples now.)
- Perform genome sequence data of all samples for researchers performing other analyses (Data mining).
- Already identified diabetes markers from genome analysis.
- Hope to include NMR- and Mass-based metabonomics data.

## 2. Macromolecular structure/function



15 February 2001

# nature

www.naturejpn.com

## the human genome

### Nuclear fission

Five-dimensional energy landscapes

### Seafloor spreading

The view from under the Arctic ice

### Career prospects

Sequence creates new opportunities

naturejobs  
genomics special



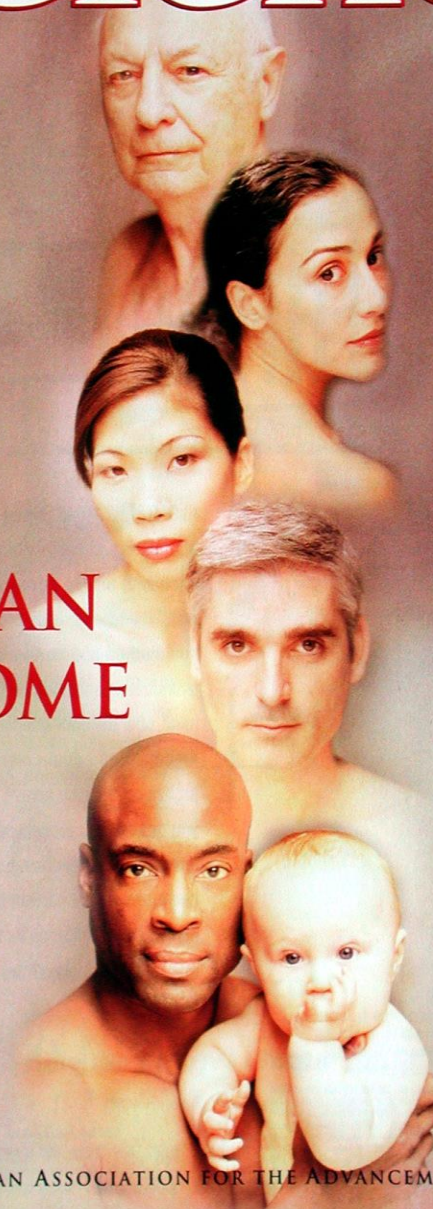
Sup.

# Science

16 February 2001

Vol. 291 No. 5507  
Pages 1145-1434 \$9

## THE HUMAN GENOME

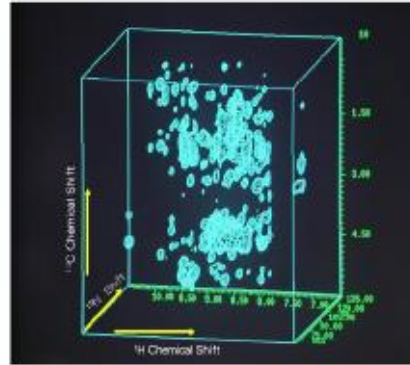
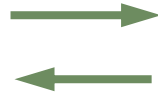


AMERICAN ASSOCIATION FOR THE ADVANCEMENT OF SCIENCE

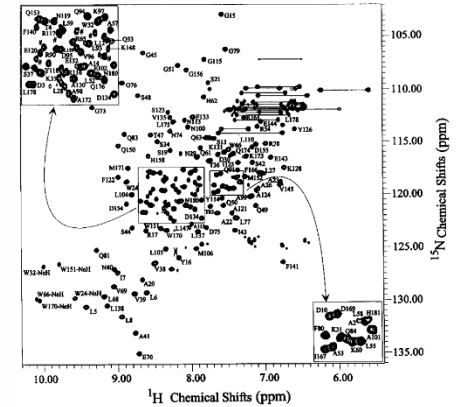
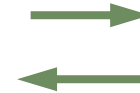
# Determine Protein Structure by NMR



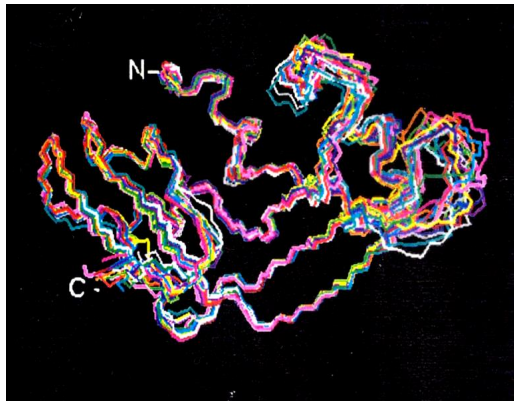
NMR Sample  
(1 mM, 0.4 ml)  
<sup>2</sup>H, <sup>13</sup>C, <sup>15</sup>N-label



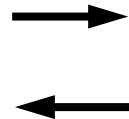
Obtain NMR spectra



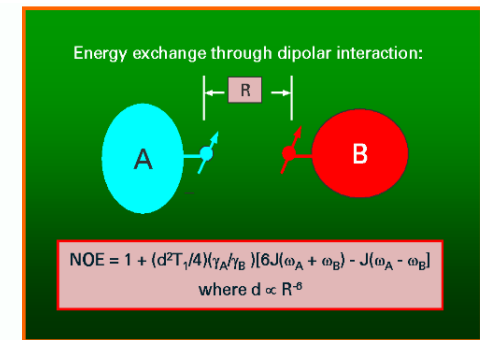
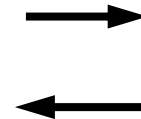
Assign resonances



NMR structures  
(Ensemble of 20 structures)



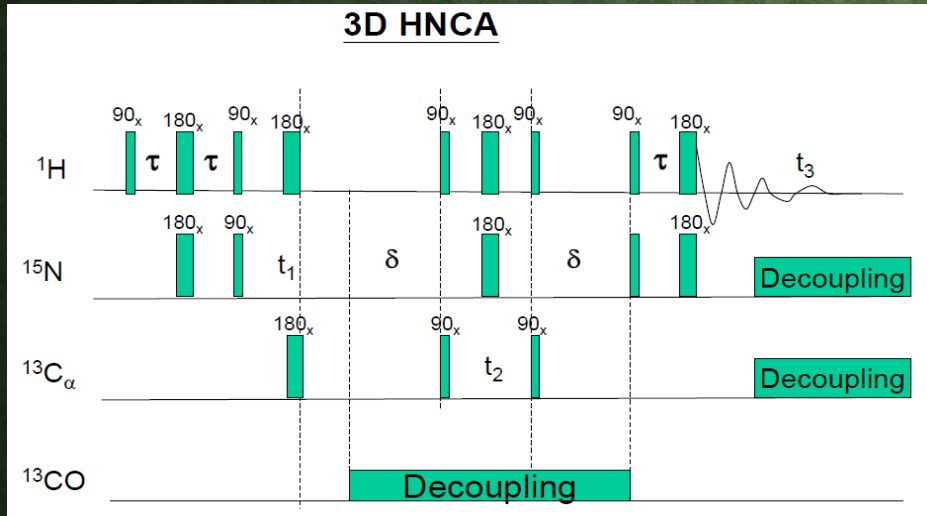
Calculate structures



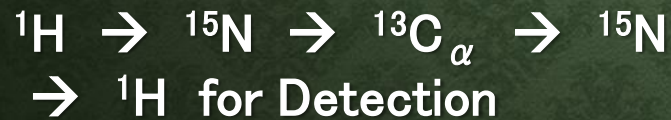
Obtain restraints  
(Distances, angles,  
Orientations etc)

# Sequential resonance assignments

Heteronuclear multidimensional NMR experiments thru J-coupling



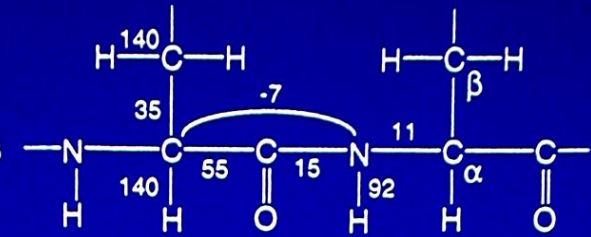
M transfer pathway for HNCA:



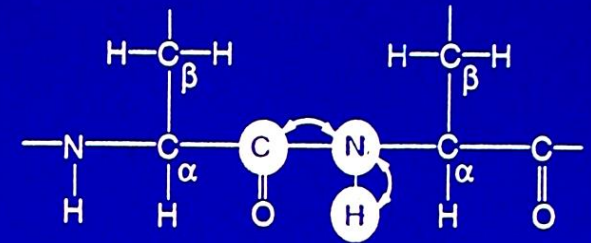
→ Detect  ${}^1\text{H}$ ,  ${}^{13}\text{C}$ ,  ${}^{15}\text{N}$  resonances

→ Permit sequential correlation of backbone  ${}^1\text{H}$ - ${}^{13}\text{C}$ - ${}^{15}\text{N}$  resonances !!!

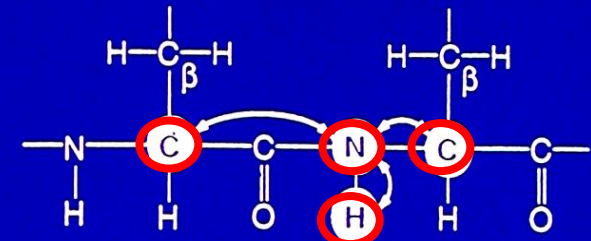
(a) J couplings



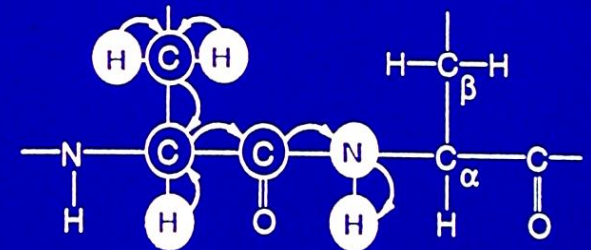
(b) HNC(O)



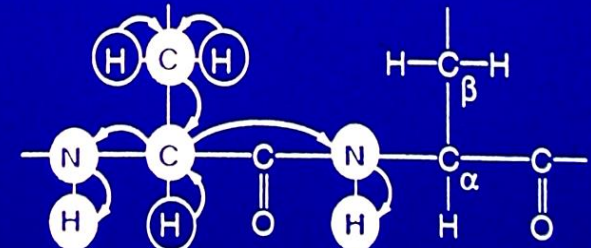
(c) HNCA



(d) HBHA-(CBCACO)NH



(e) CBCANH



# Structure Calculation

1. Build a random structure of the given sequence.
2. Energy minimization with least violation by molecular dynamics and simulated annealing to generate many structures.

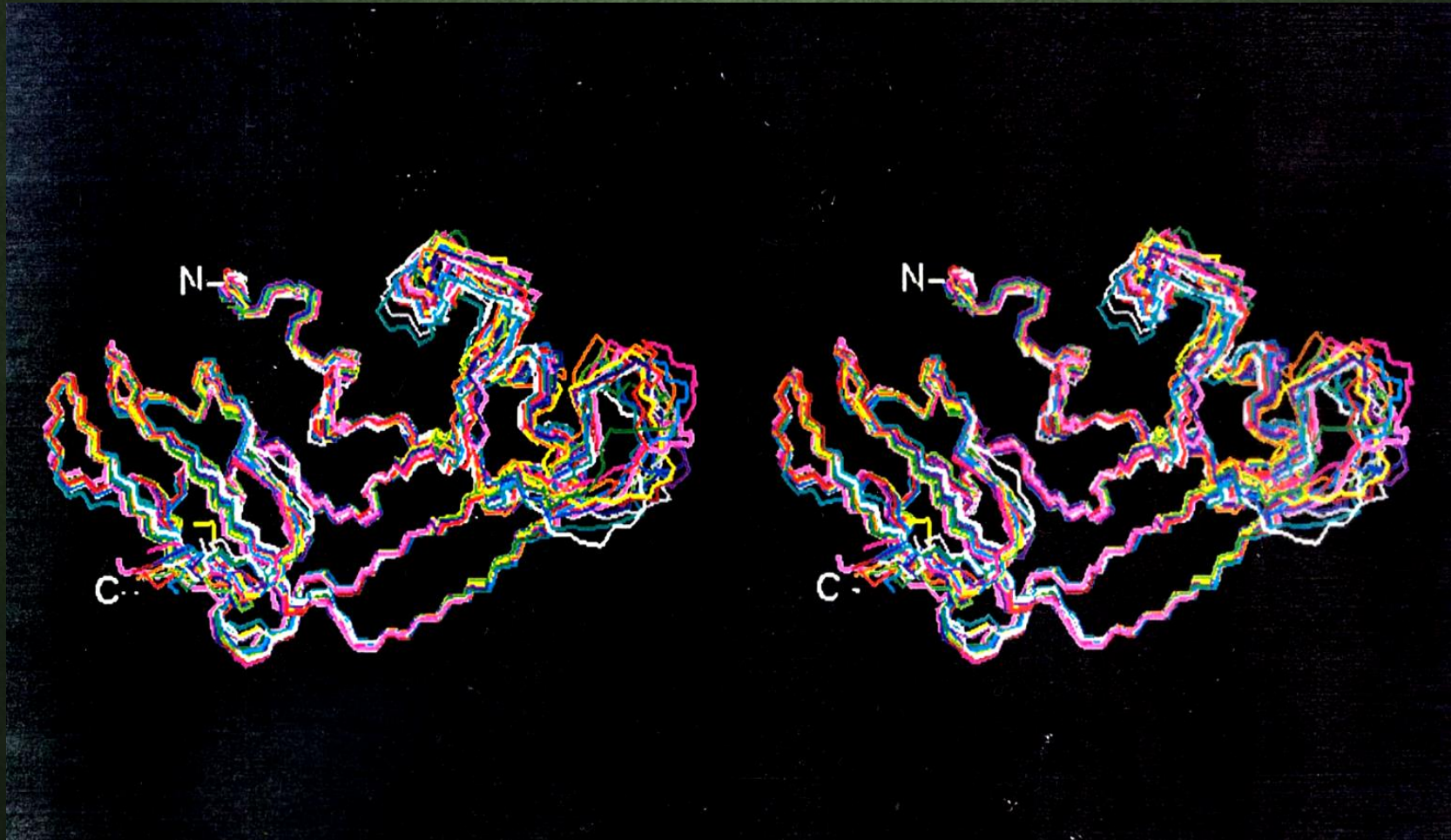
$$E_{\text{total}} = E_{\text{bond}} + E_{\text{angle}} + E_{\text{improper}} + E_{\text{VDW}} + E_{\text{cdih}} + E_{\text{NOE}} + E_{\text{RDC}} + \dots$$

$$E_{\text{bond}} = \sum k_b (b - b_0)^2; \quad E_{\phi} = \sum k_{\phi} (\phi - \phi_0)^2; \quad E_{\text{VDW}} = \sum k_{ij} [(\sigma_{ij}/r_{ij})^{12} - \sigma_{ij}/r_{ij}]^6$$
$$E_{\text{improper}} = \sum k_{\text{impr}} (\omega - \omega_0)^2; \quad E_{\text{cdih}} = \sum k_{\text{cdih}} (\Psi - \Psi_0)^2;$$
$$E_{\text{NOE}} = \sum k_{\text{NOE}} (\gamma - \gamma_0)^2; \quad E_{\text{RDC}} = \sum k_{\text{RDC}} (\theta - \theta_0)^2;$$

3. Select 20 structures of least NOE violation ( $> 0.5 \text{ \AA}$ ).
4. Criteria for good structures:
  - a) No NOE violation
  - b) RMSD  $< 0.5 \text{ \AA}$
  - c) No dihedral angle violation (Ramachandran diagram)

# NMR structure of RC-Rnase

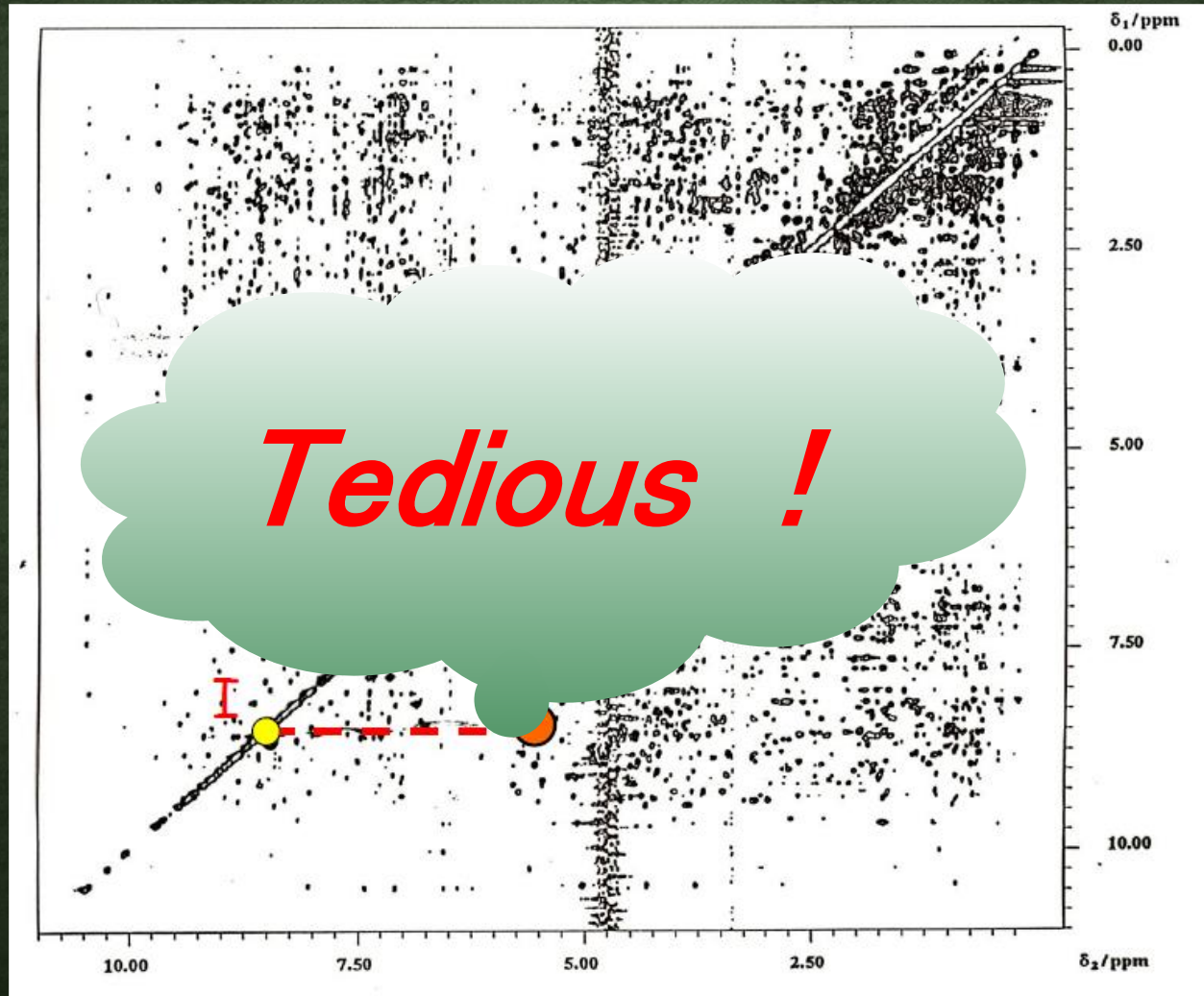
Ensemble of a set of lowest energy structures



# $^1\text{H} - ^1\text{H}$ NOESY spectrum of RC-Rnase

Identify short  $^1\text{H} - ^1\text{H}$  distances

$^1\text{H}$  chemical shift (ppm)

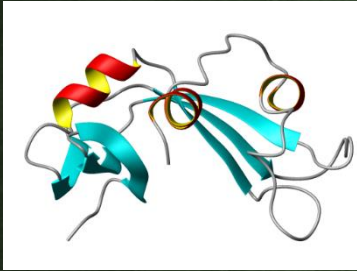


$^1\text{H}$  chemical shift (ppm)

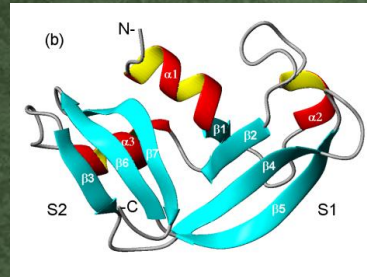


# Gallery of structures determined

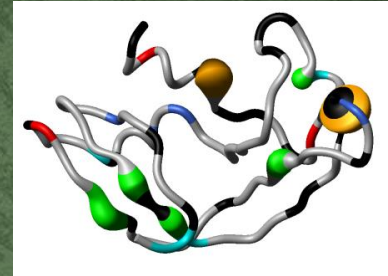
RC-RNase



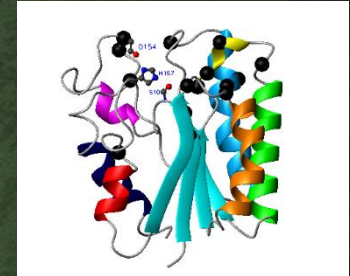
Onconase



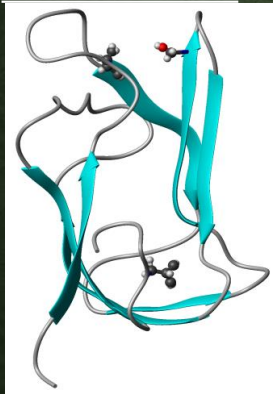
Dynamics of onconase



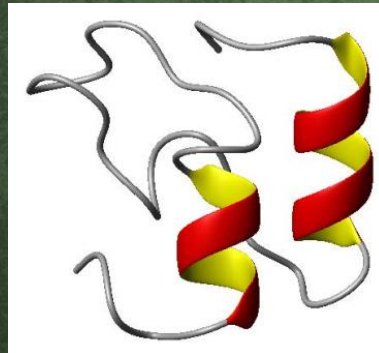
E. Coli Thioesterase



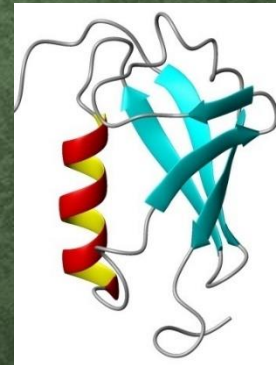
BCKD - LBD



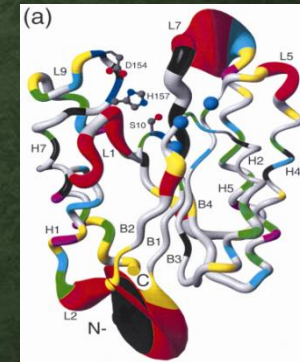
BCKD - SBD



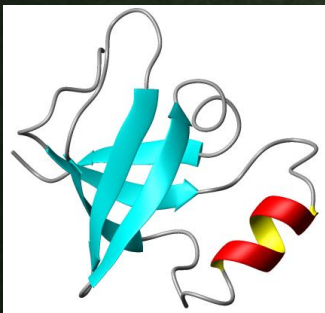
SUMO-3



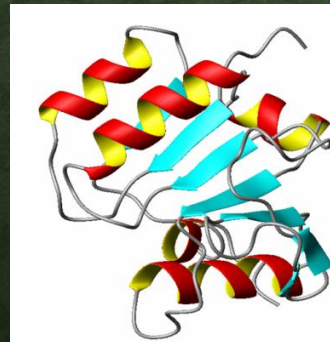
Dynamics-Fast Motion



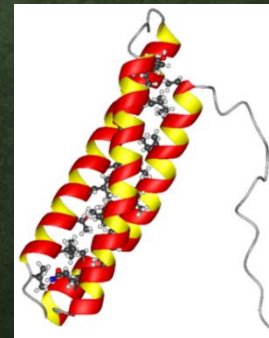
KP Feo A protein



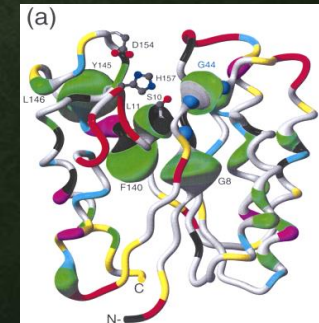
KP CoA Binding Protein



Blo t 5 Allergen

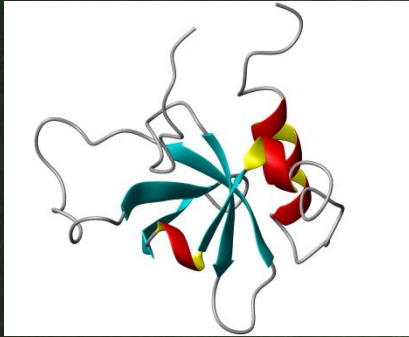


Slow Motion

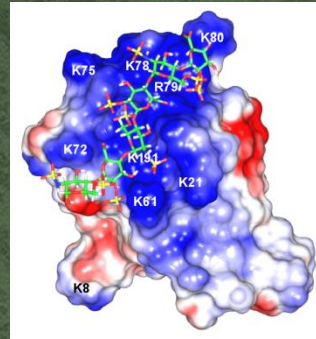


# Gallery of structures determined

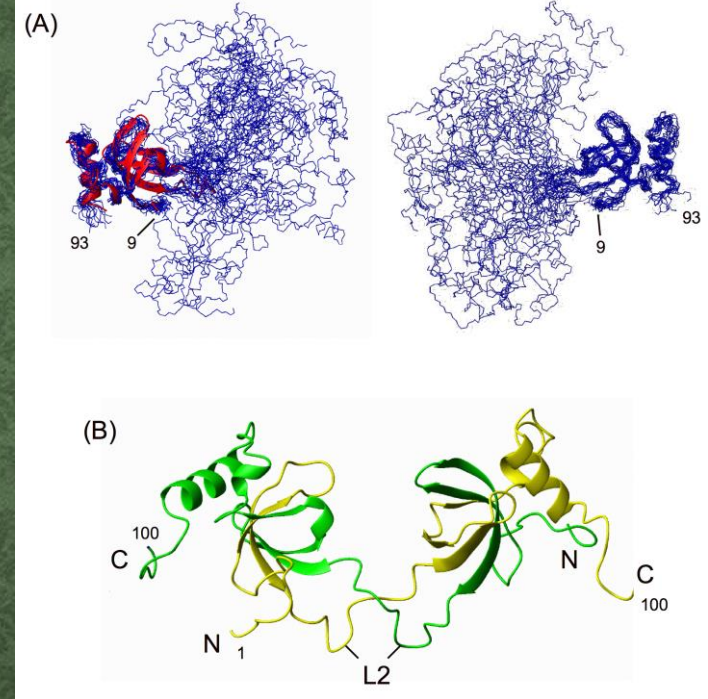
PWWP-domain of HDGF



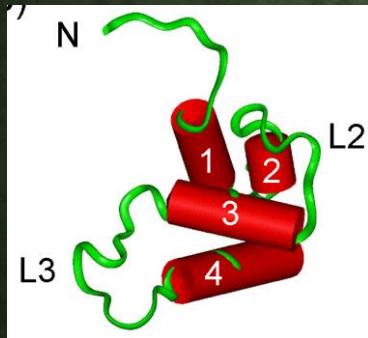
HDGF/heparin complex



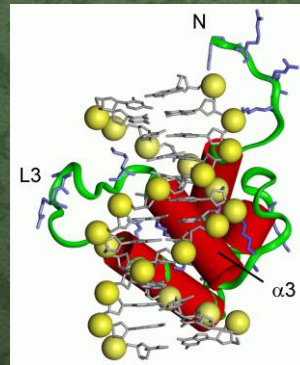
HDGF dimer of HDGF



Telomere binding protein

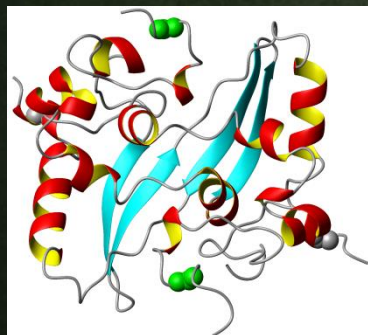


AtTRP/DNA complex

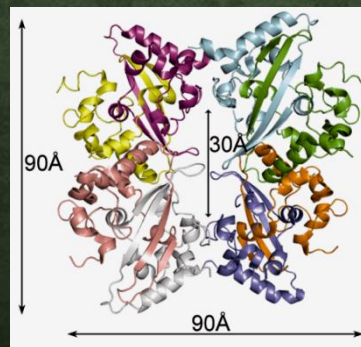


Model of N248-365

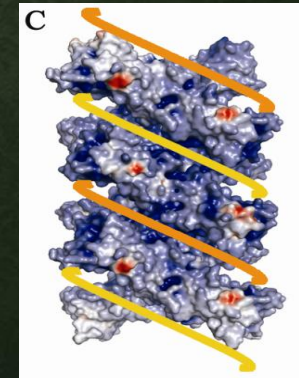
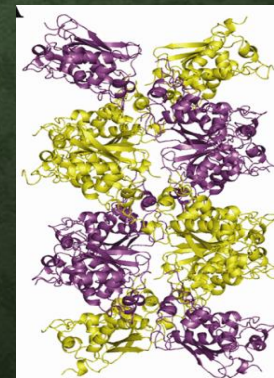
N248-365 of SARS CoV



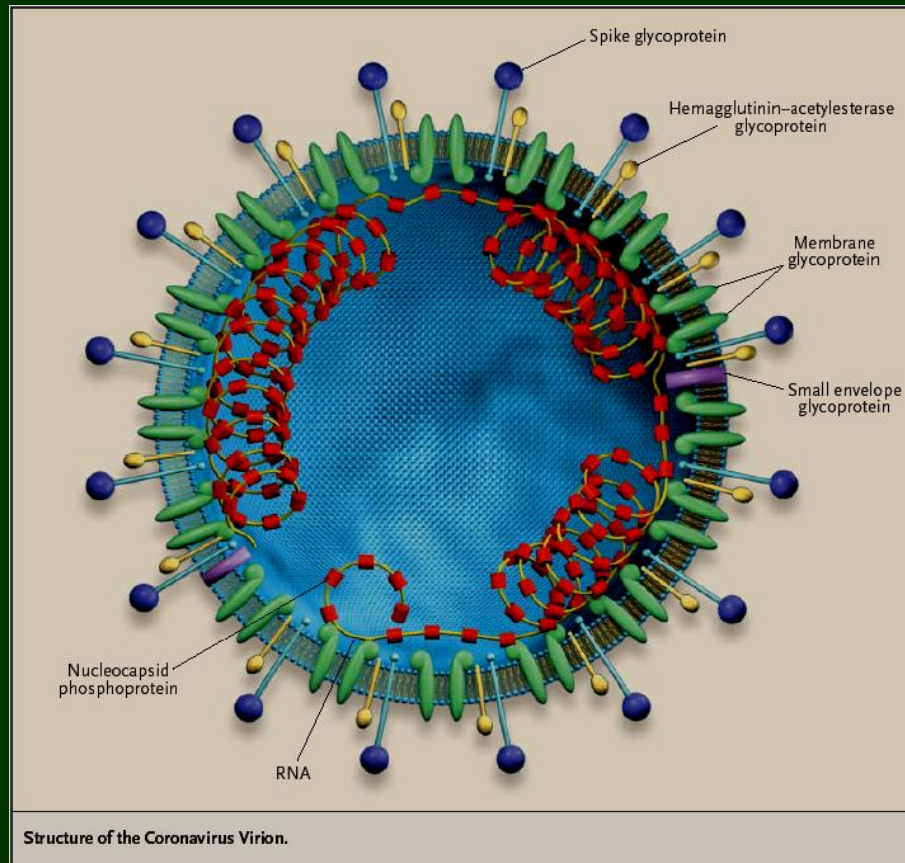
N248-365 of SARS CoV octamer



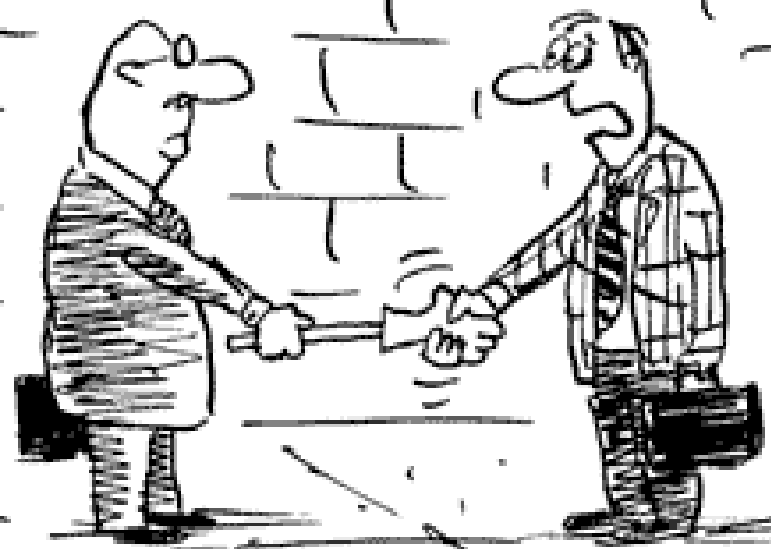
of SARS CoV/RNA complex



## 2.1. Packaging of SARS Coronavirus Ribonucleocapsid



HI, DOCTOR. I'M GLAD I RAN INTO YOU. I HEARD THAT SHAKING HANDS CAN SPREAD THE SARS VIRUS... IS THAT TRUE?



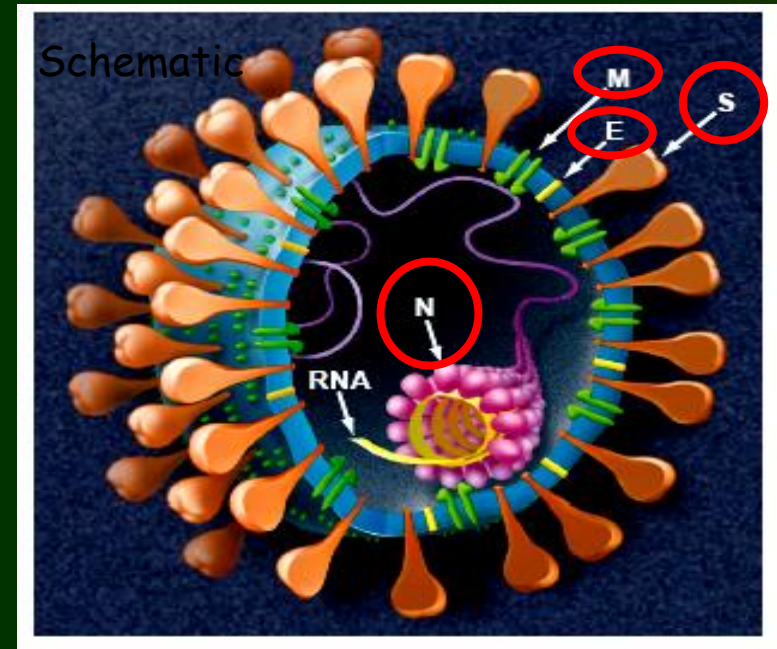
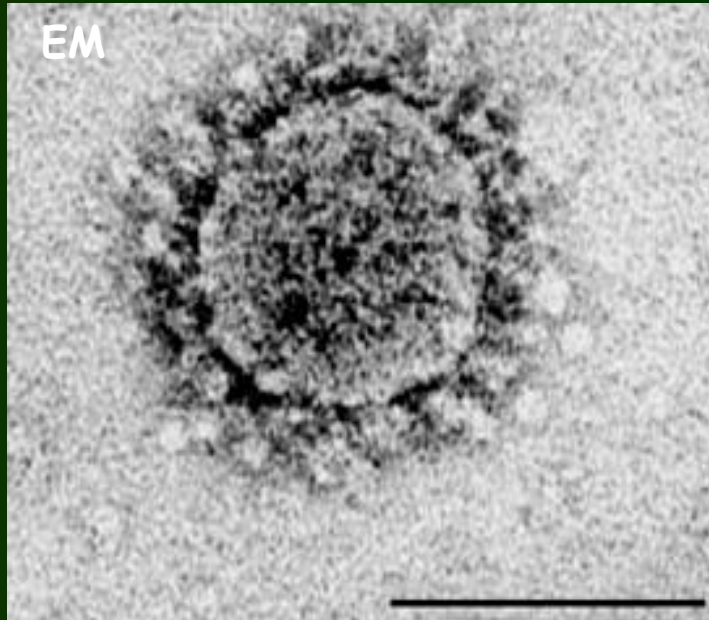
BUS STOP



STAYSKAL  
TAMPA 4/03  
TRIBUNE

# Causative agent – SARS Coronavirus

1. A single stranded plus-sense enveloped RNA virus.
2. Genome of 29,751 nt, containing 14 ORF encoding 28 proteins



## Four Structural proteins:

S: Spike protein (1255 a.a.);

M: Membrane protein (221)

E: Envelope protein (76 a.a.)

N: Nucleocapsid protein (422 a.a.)

## Nucleocapsid Protein (NP)

- The most abundant viral protein and a major antigenic determinant:
  - ➔ Target for detection and vaccine developments.
- Binds to RNA to form a helical ribonucleoprotein (RNP):
  - ➔ Important in virion assembly, packaging and release.
- Interacts with various host proteins and implicated in functions such as replication and apoptosis etc:
  - Interacts with AP-1 signal transduction pathway ?
  - Interacts with Smad3 and Modulates transforming Growth Factor- Signaling
  - Inhibits Cell Cytokinesis and Proliferation by Interacting with Translation Elongation Factor 1 $\alpha$

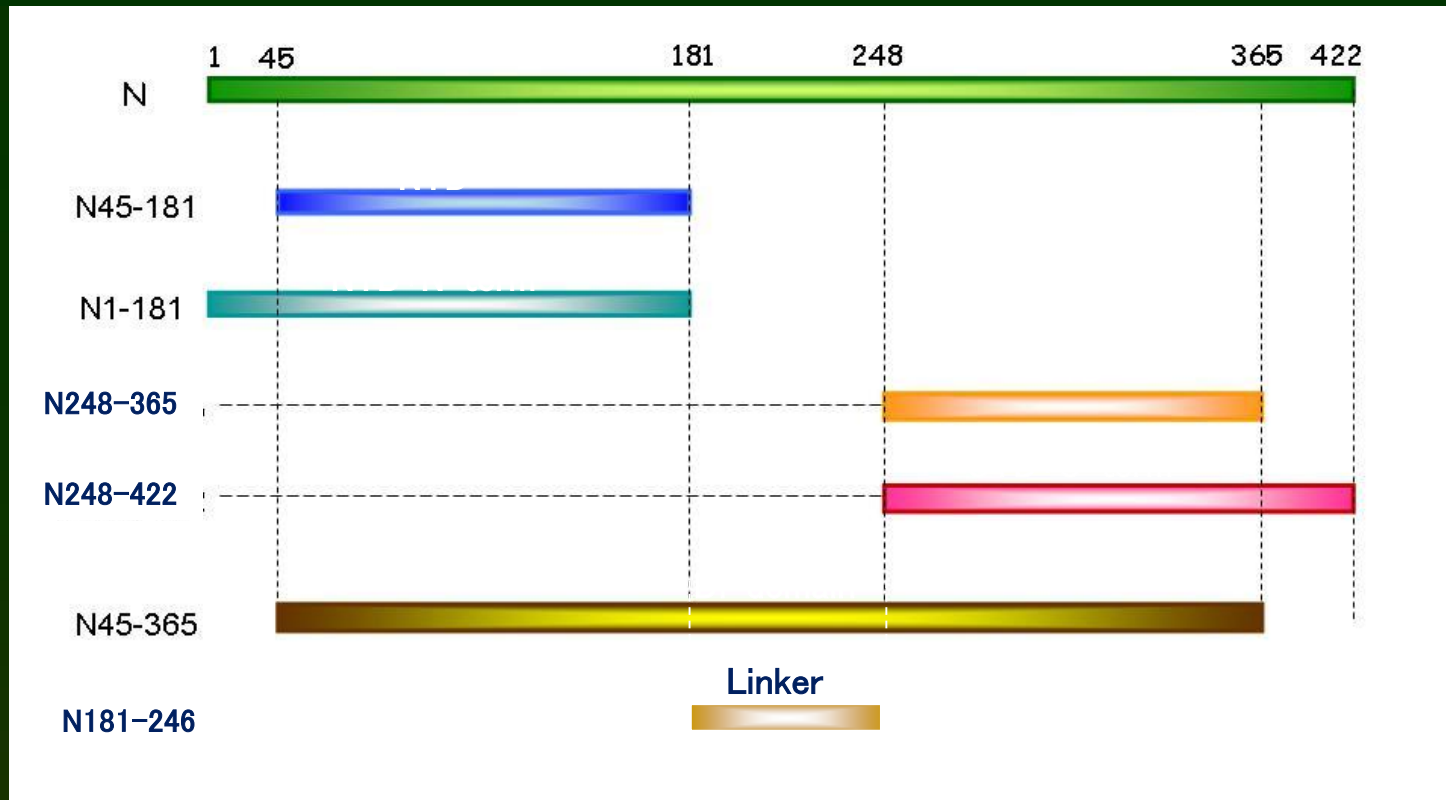
# Goal

Unravel the packaging mechanism of helical ribonucleocapsid (RNP) :

1. Dissect N protein domain architecture
2. Probe N protein interaction with RNA.
3. Determine the tertiary structure of N protein.
4. Understand how RNA packs with N protein to form the helical RNP.

## Dissecting Domain architecture of N protein

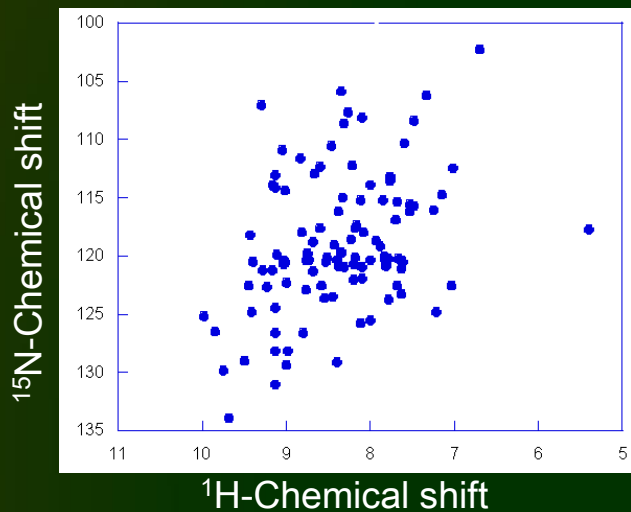
- The full length protein (422 a.a.) cannot be crystallized and the NMR spectrum is bad
- Divide and conquer – Construct many sub-fragments and characterize their structures.





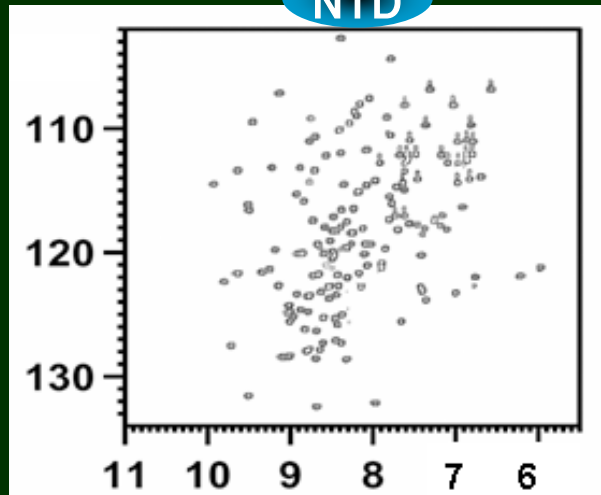
# Characterization of protein order by 2D $^{15}\text{N}$ -HSQC

Folded



45-181

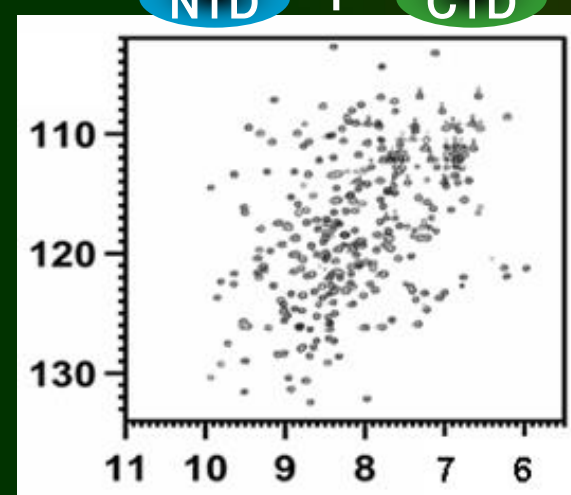
NTD



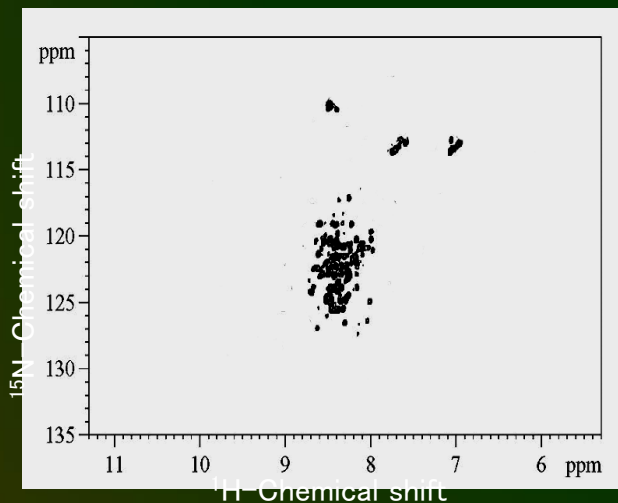
Overlay

NTD

+ CTD

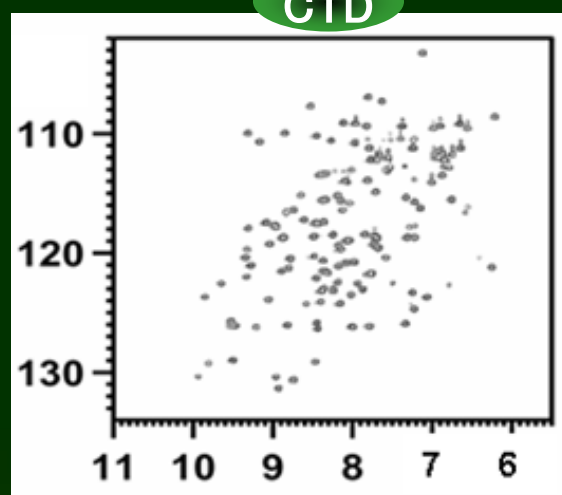


Disordered protein



248-365

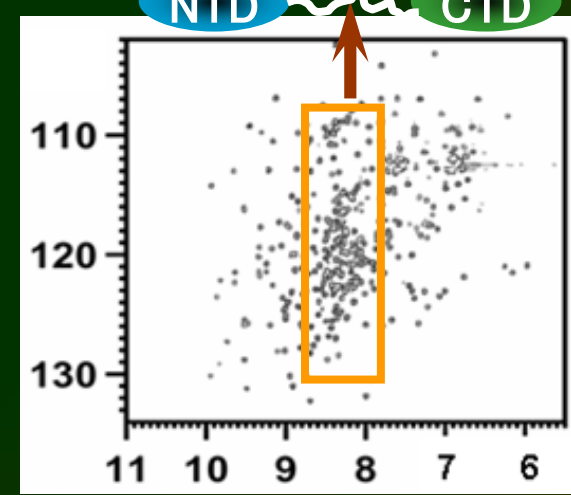
CTD



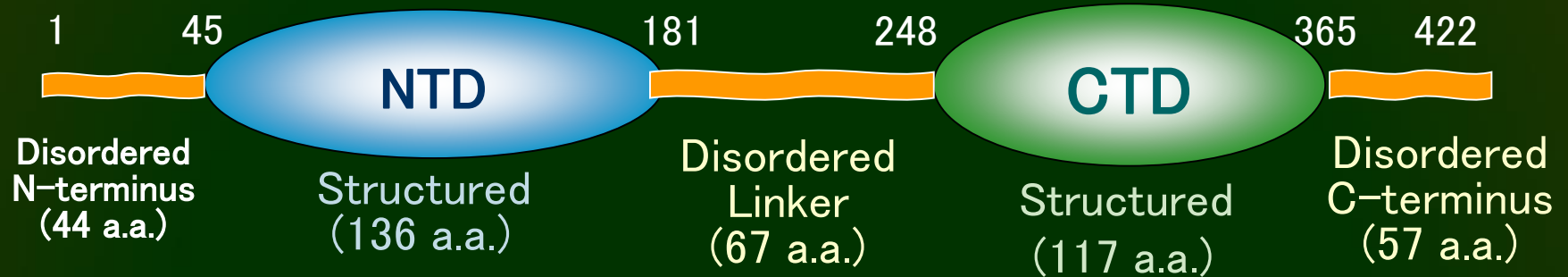
45-365

NTD

CTD

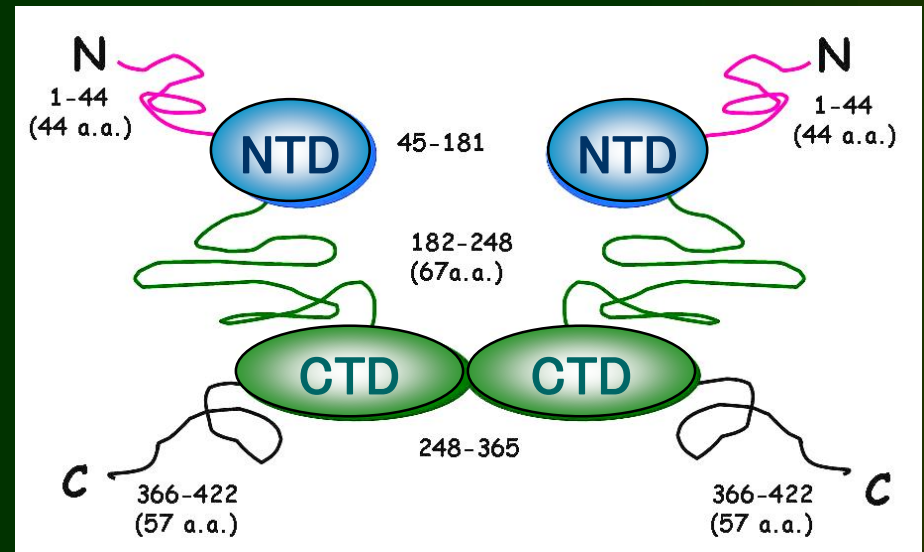


## Domain architecture of SARS-CoV NP

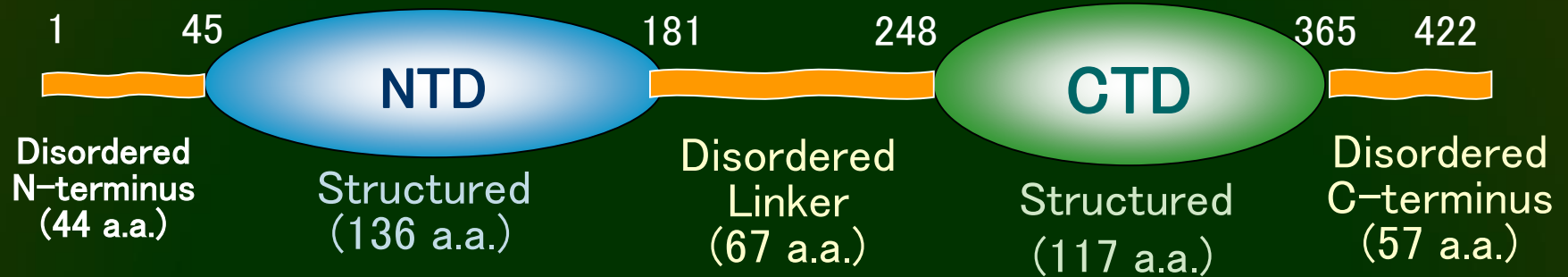


### CTD forms a dimer

- Light scattering
- Analytical Ultra-Centrifugation
- Size exclusion chromatography
- Chemical cross linking
- NMR relaxation



## Domain architecture of SARS-CoV NP



- ~ 50% of SARS-CoV residues exist in intrinsically disordered state.
- Nucleocapsid proteins belong to a class of proteins with the most disordered residues.

Why ?

What are the advantages ?

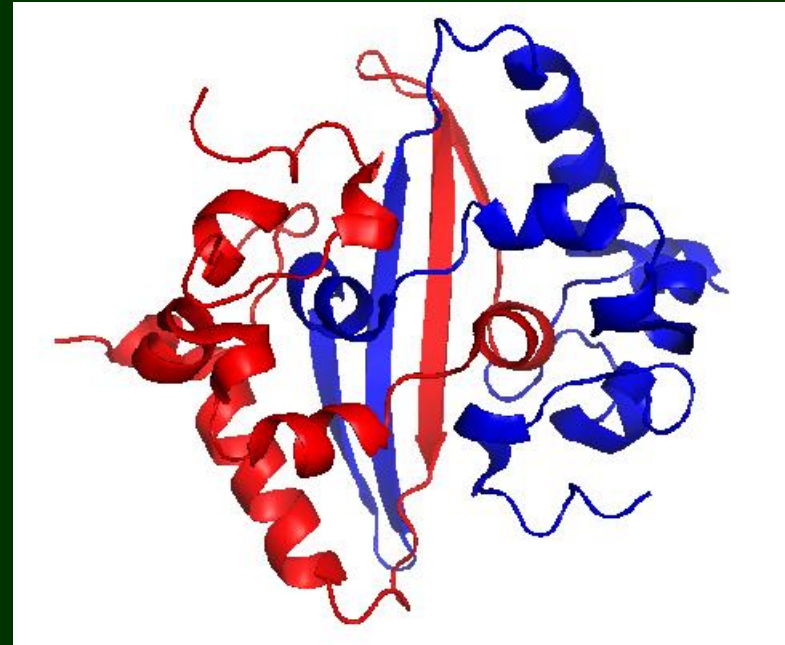
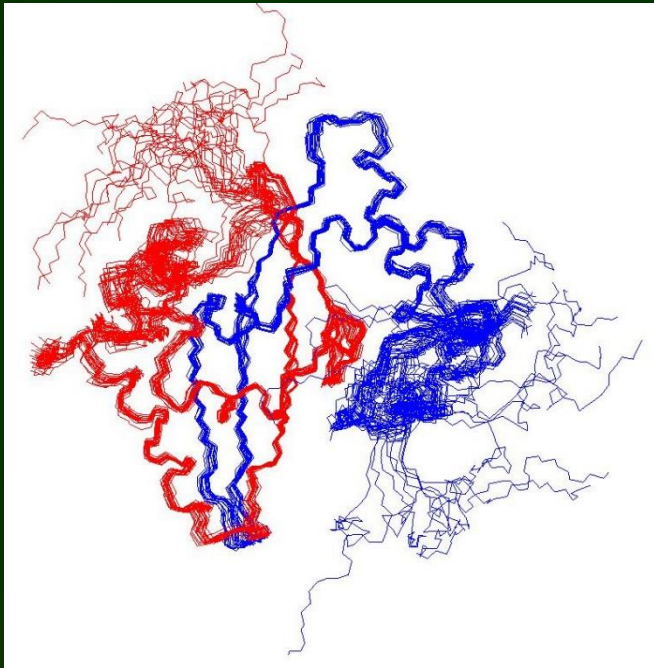
## Advantage of intrinsic disorder

1. Increase collision cross section.
2. Adapt to different shapes.
3. Coupled allosteric effect (Multi-valency effect).



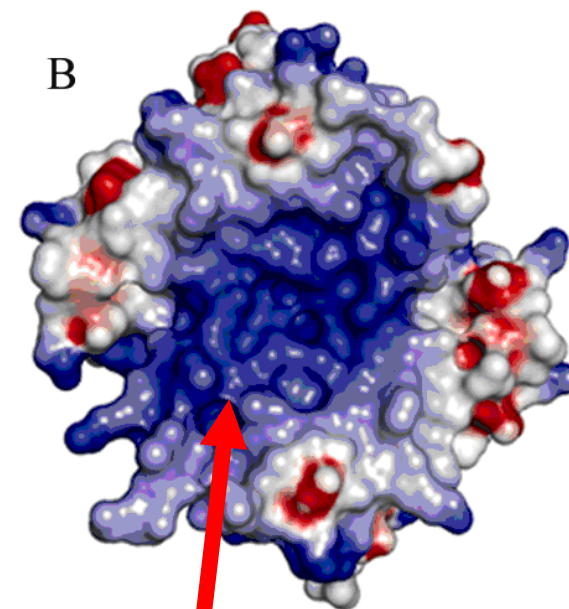
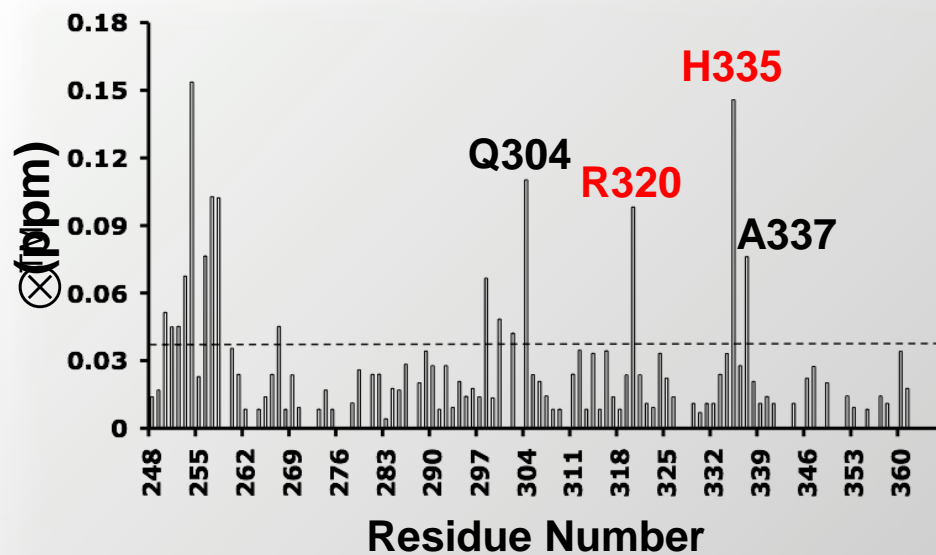
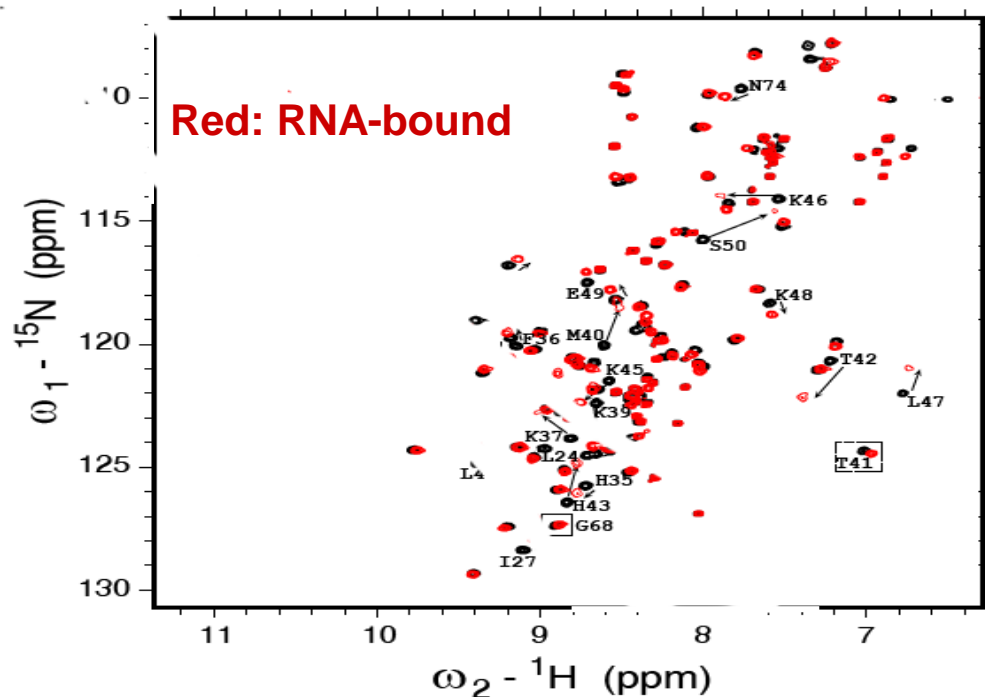
## NMR Structure Of SARS-CoV NP CTD

→ 28 kDa homo-dimer solved by Stereo-Array Isotope Labeling (SAIL) method (M. Kainosho of Nagoya U)



A flatten rectangular domain-swapped dimer

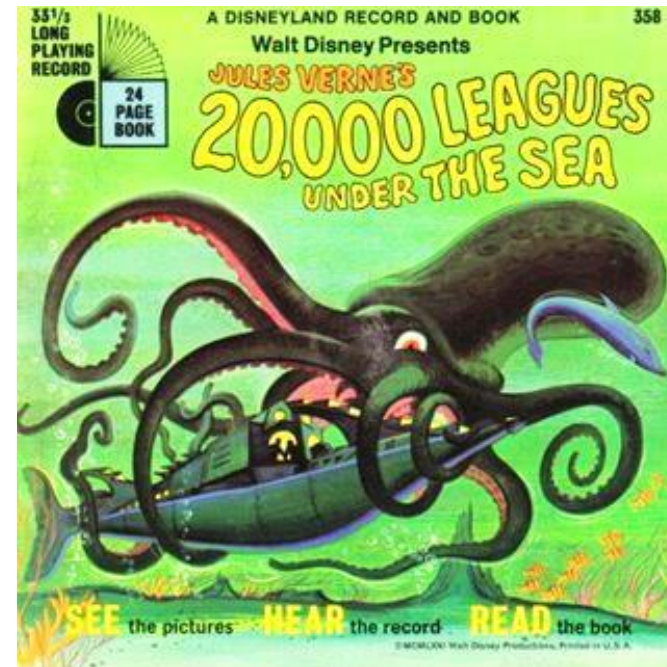
# Identification of RNA binding site in CTD



Primary RNA binding site.

# N – Nucleic Acid Interaction

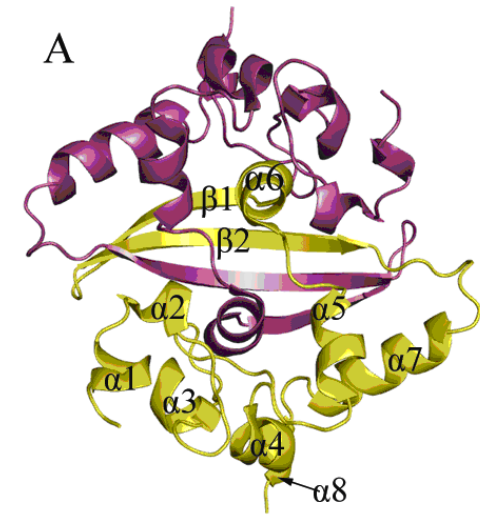
N protein binds to nucleic acid at multiple sites cooperatively, much like an octopus clinching onto its prey.



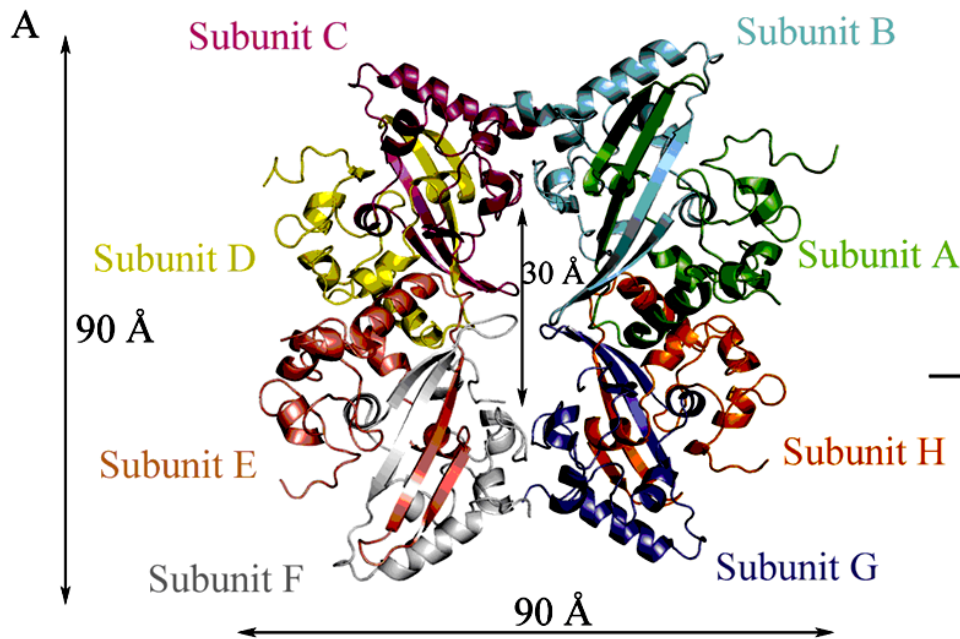
➔ Modular nature and intrinsic disorder are keys to binding cooperativity and RNP packaging

# X-ray crystallography

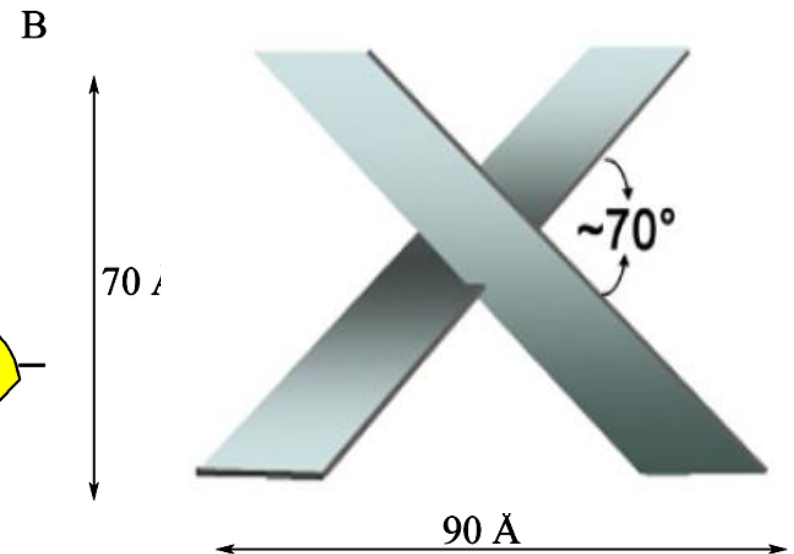
- Structure similar to that determined by NMR.
- CTD packs as an octamer in an unit cell.



Top view



Side view

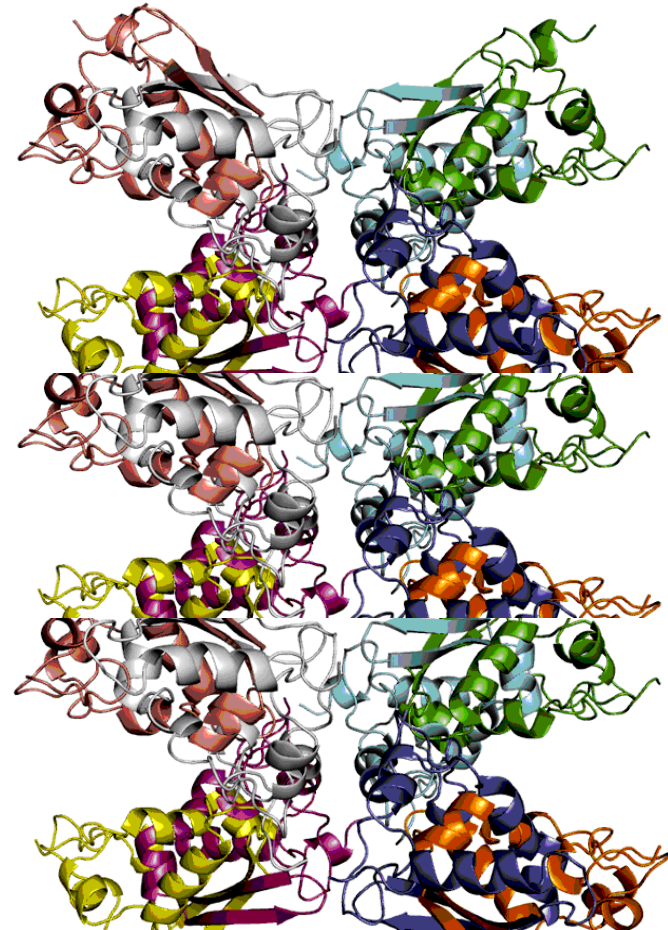
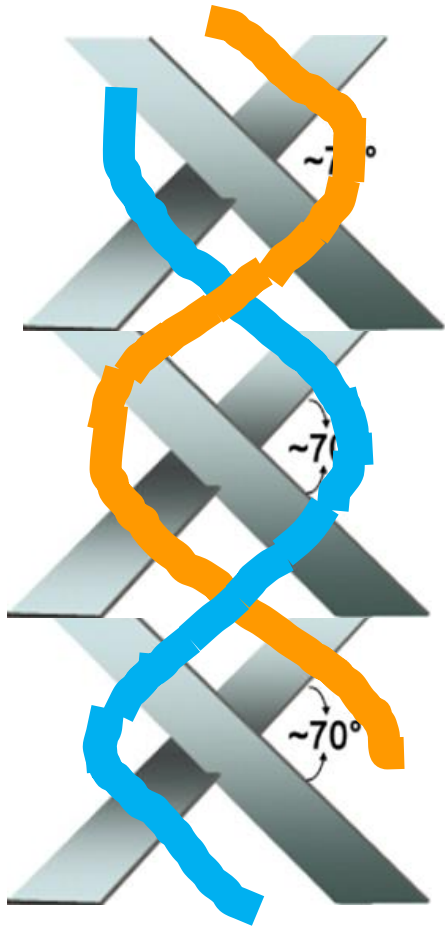




# Crystal packing

---

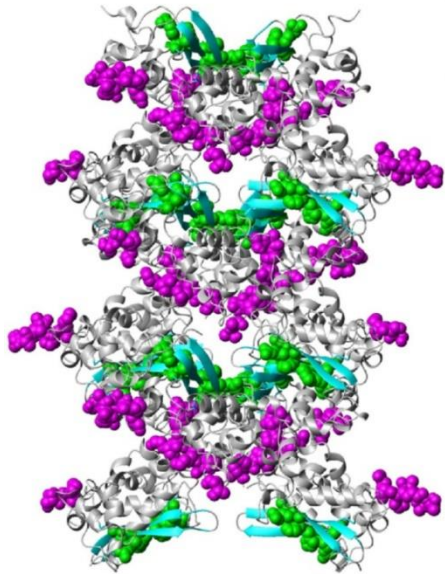
- Stacking of 3 octamers forms a complete turn of a left-handed twin helix.



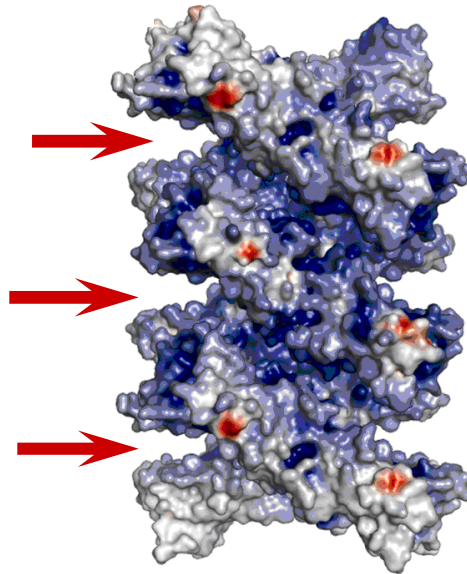
# DNA binding sites are located in the positively charged grooves

---

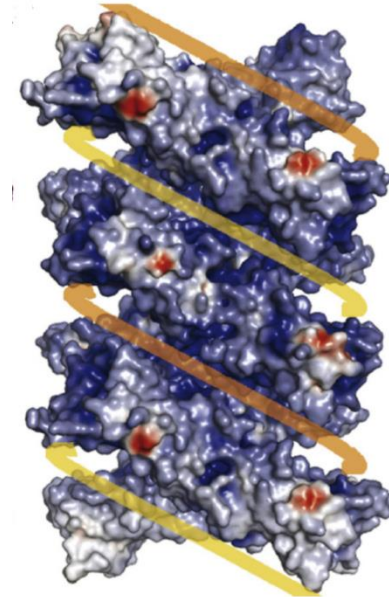
DNA binding site  
NMR (magenta)



Surface Charge Potential



RNA binding model



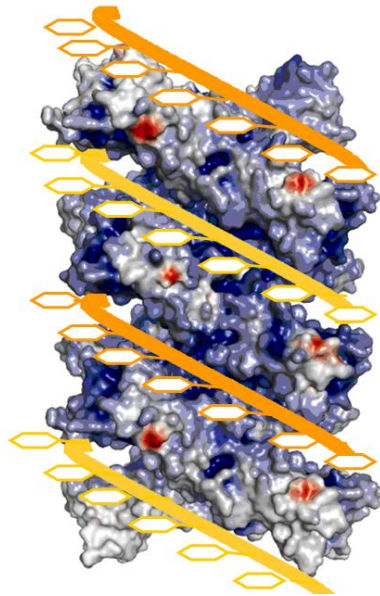
→ We propose that RNA binds to the Left-handed helix grooves.

## Key features of SARS CoV N protein

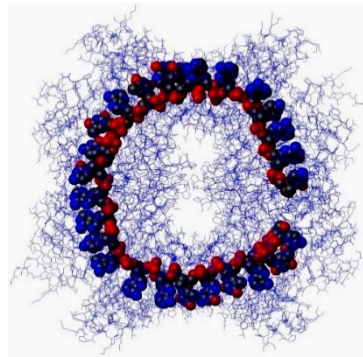
- **A modular protein:** It consists of two structured domains and three disordered segments.
- **It is highly flexible:** ~50% of the residues are intrinsically disordered (ID).
- **A sticky protein:** It binds to RNA at multiple sites cooperatively.
- **The CTD forms a dimer and packs in helical structure in crystal.**

## Proposed model of the N/RNA complex

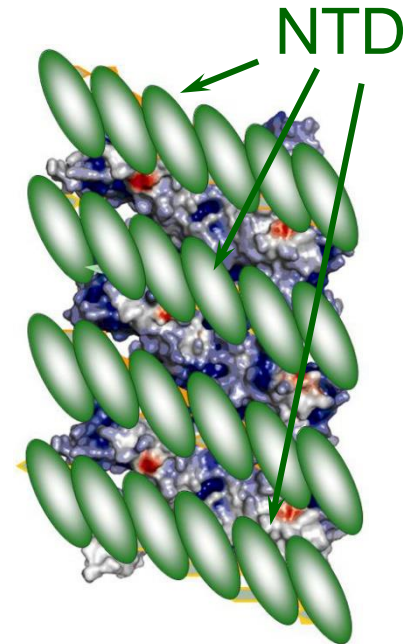
- CTD forms the core of the left-handed twin-helix .
- Backbone of RNA wraps around CTD core and with bases facing outward.
- NTD covers the exterior and interacts with the bases.



Side view



Top view

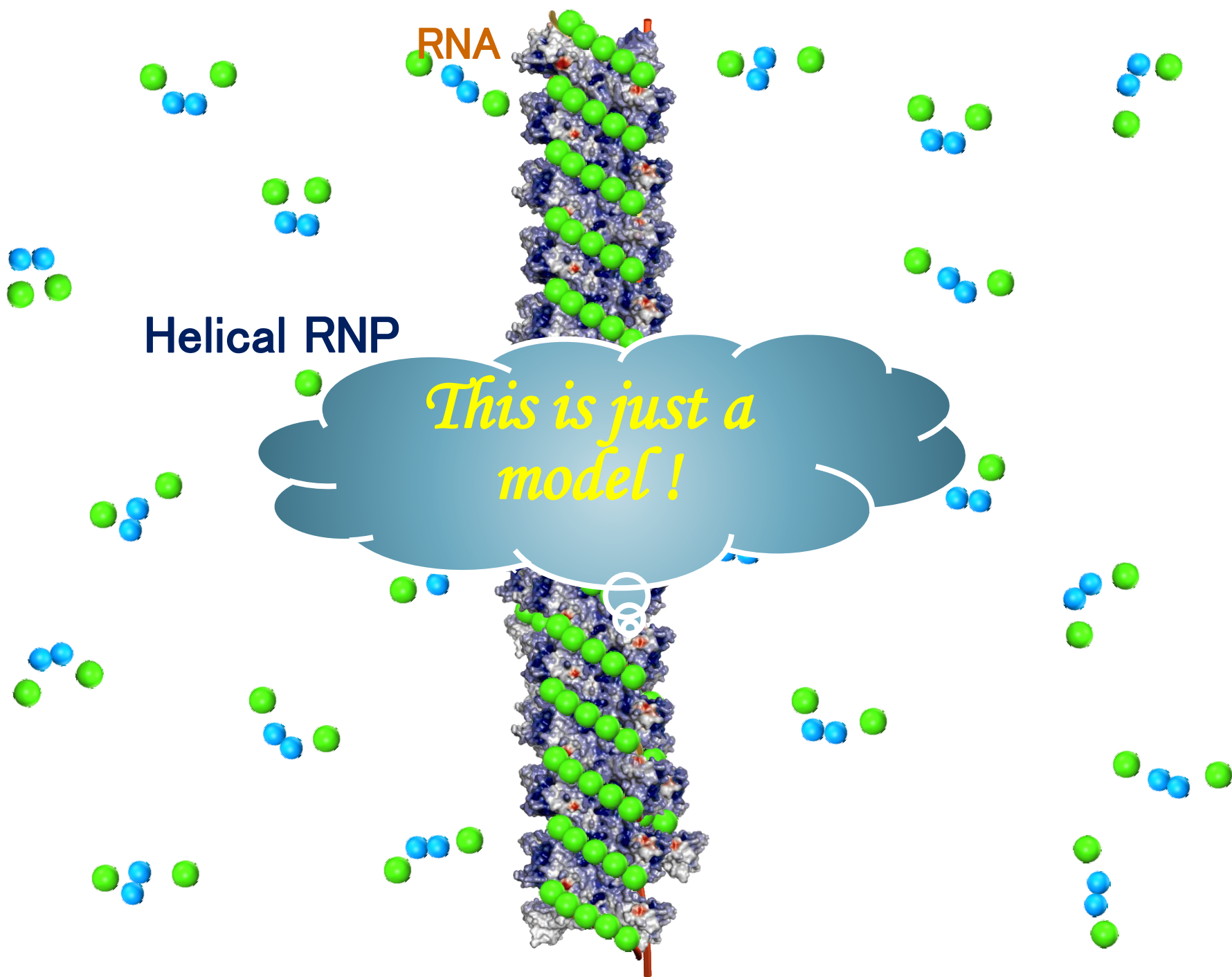


N/RNA complex (RNP)

RNA

Helical RNP

*This is just a model!*



# Acknowledgements



**Dr. Chungke Chang**

## Huang's lab

**Dr. Chungke Chang**

**Dr. Shih-Che Su**

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**Hsin-hao Hsiao**

**Dr. Chi-fon Chang**

**Dr. Wen-Jing Wu**

**Yuan-hsiang Chang**

**Tsan-Hung Yu**

**Liliarty Riag**

**Yen-Chieh Chiang**

## X-ray crystallography

**Dr. Chwan-Deng Hsiao**

**Chun-Yuan Chang**

**Yi-Wei Chang**

## SAXS (NSRRC, Taiwan)

**Dr. Yu-shan Huang (SAXS)**

## SAIL NMR (Nagoya U)

**Prof. M. Kainosho**

**Mitsuhiro Takeda**

## NMR Structure

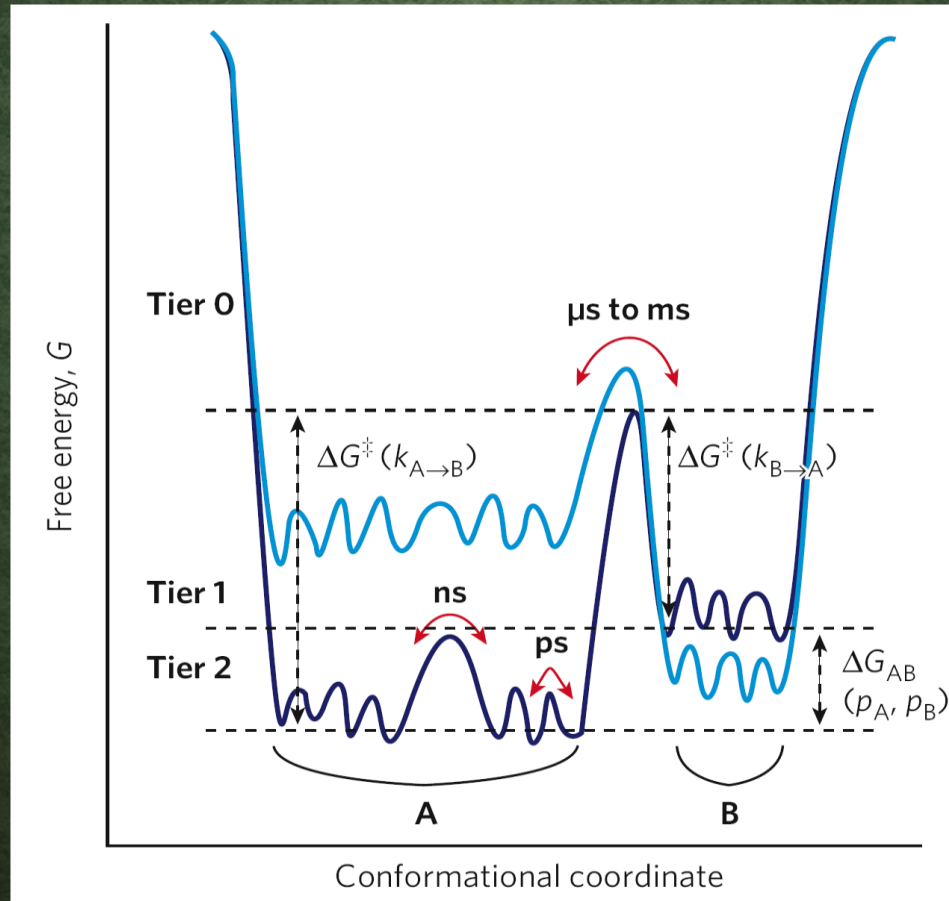
**Prof. Peter Guetert**

**(RIKEN)**

## 3. Dynamics

# Protein Dynamics

- Energy landscape of protein conformations



- Ref. 1. Henzler-Wildman & Kern (2007) Nature 450 :964-72  
2. Boehr and Wright (2006) Chem Rev. 106(8):3055-79

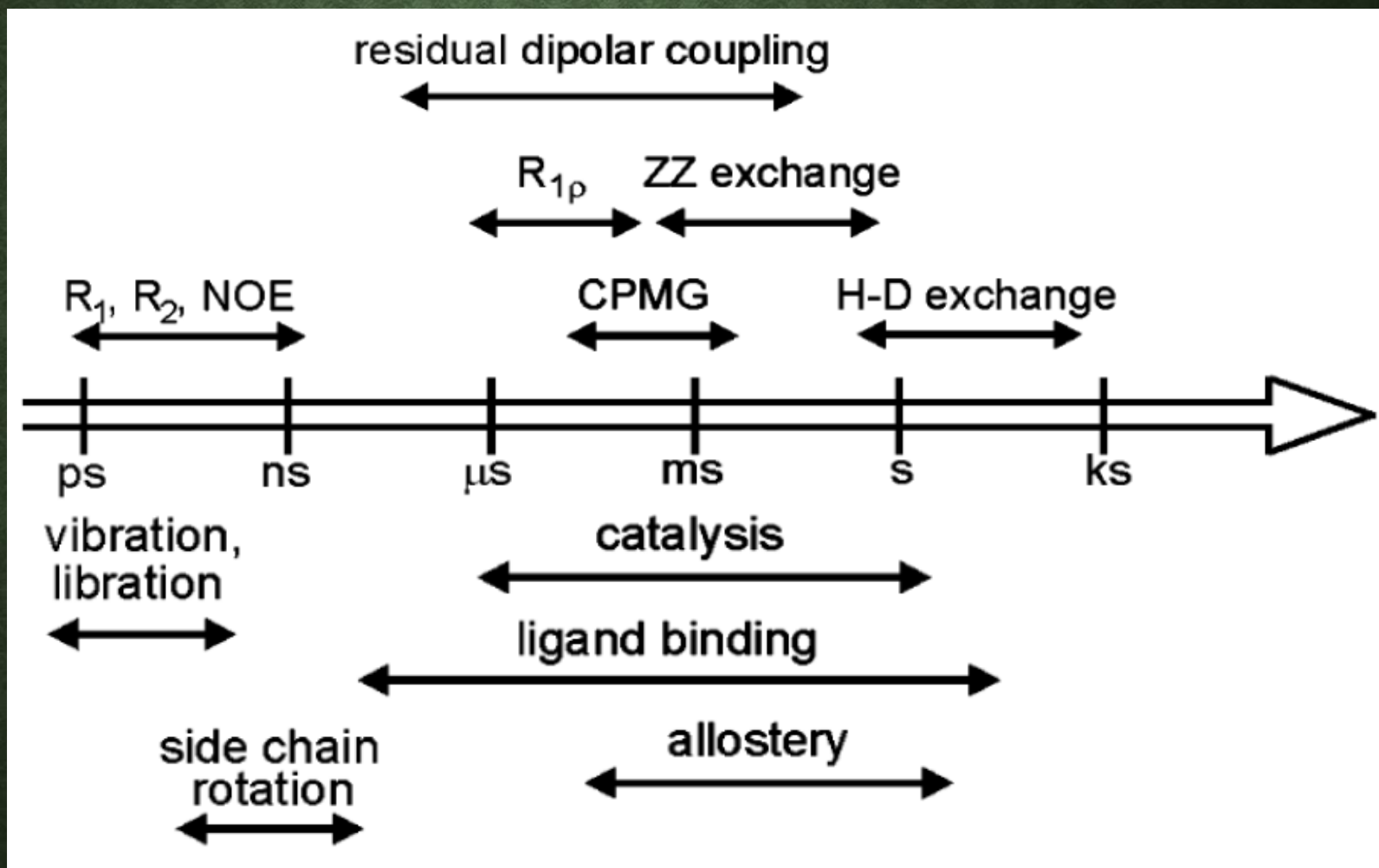


# Measurement of Macromolecular Dynamics by NMR

NMR  
experiments

Time scale

Biological  
processes

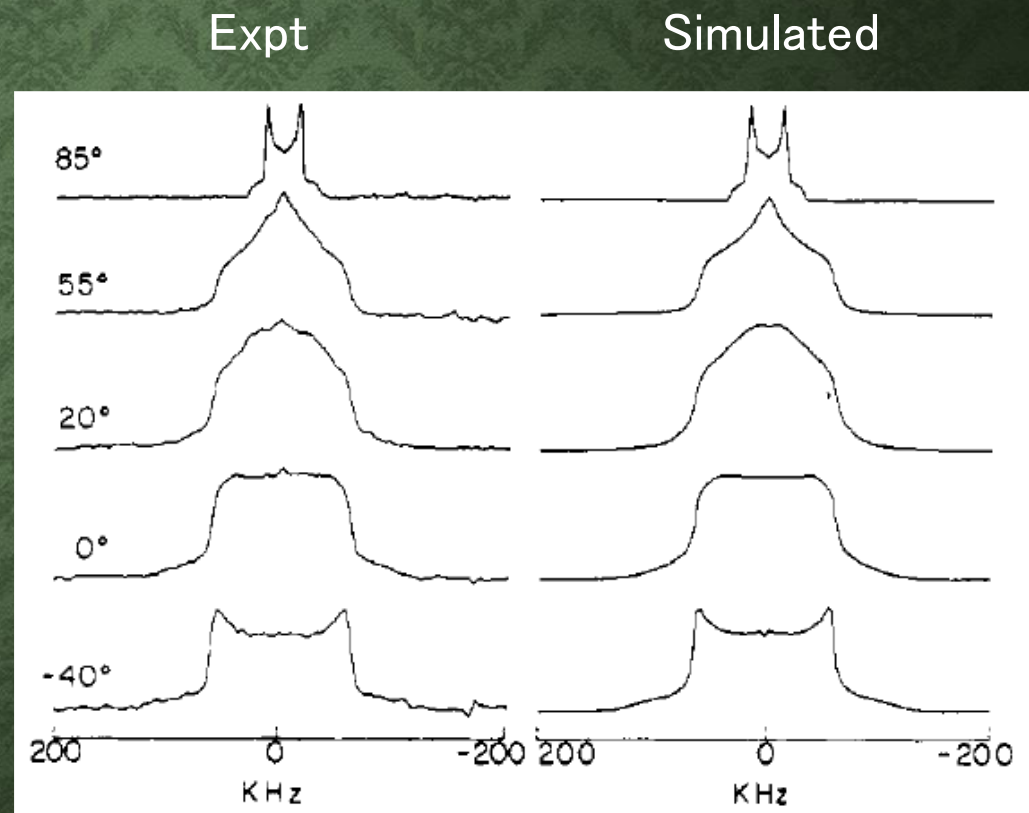
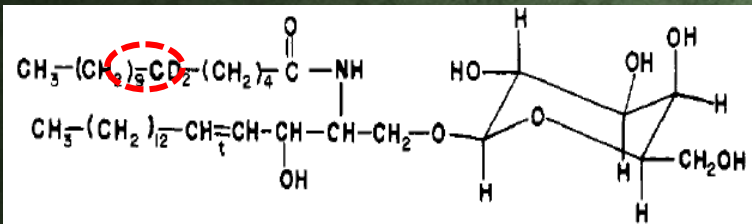


**NMR can measure a wide range of dynamic processes**

# Characterize the restricted rotational isomerization of polymethylene chains by deuterium NMR lineshape simulation

Huang et al J. Am. Chem. Soc. 102, 7377-7379 (1980)

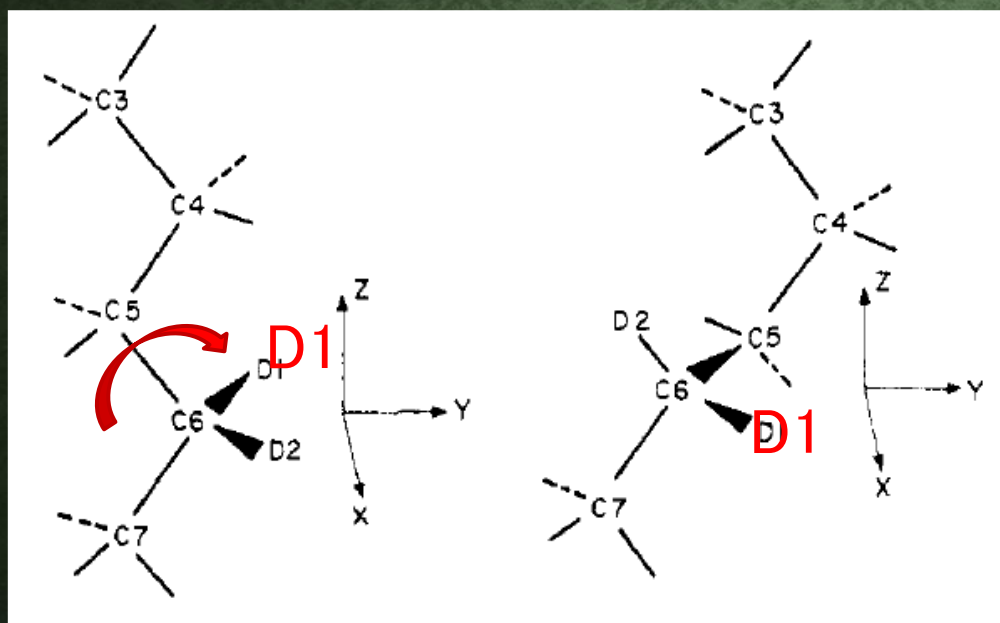
## N-palmitoylglycosylceramide



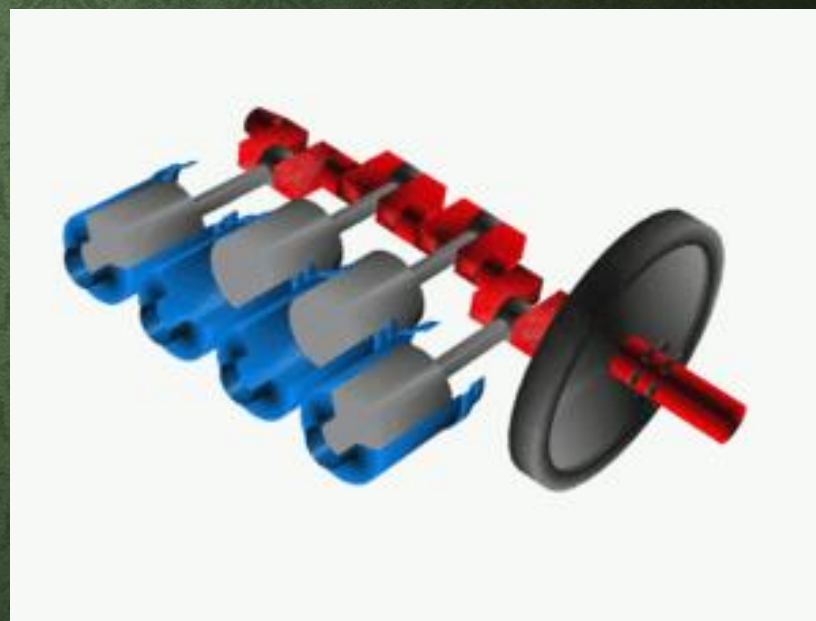
Deuterium quadrupole spectra were simulated with two site flipping model similar to that of the crankshaft motion.

Huang et al J. Am. Chem. Soc. 102, 7377-7379 (1980)

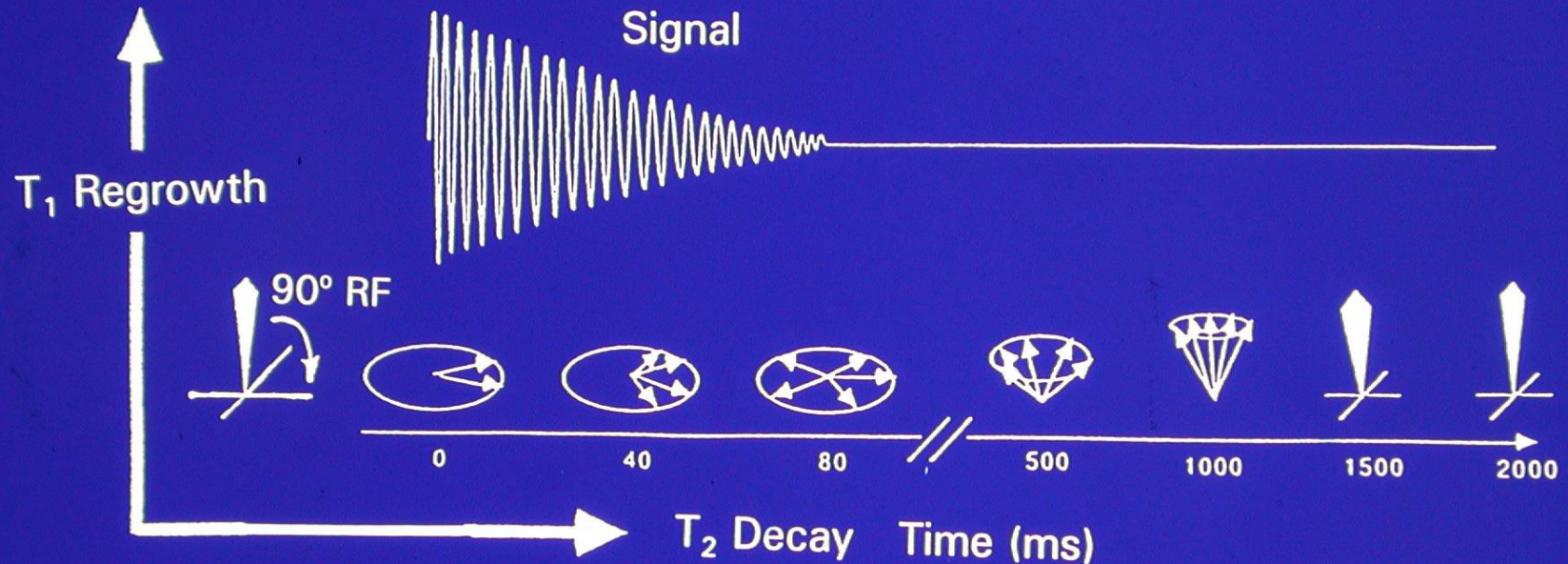
## Tetrahedral two site flipping model



## Crankshaft motion



# Liquid state – NMR Relaxation



Spin-lattice relaxation ( $T_1$ ) and spin-spin relaxation ( $T_2$ ) of nuclear spins. Figure shows the evolution of the magnetization after it has been flipped by 90° pulse.

# Relaxation Mechanism

Dominated by **dipolar** and **chemical shift anisotropic** interactions, and are related to the spectral density functions,  $J(\omega)$ , by the following equations:

$$R_1 = 1/T_1 = (d^2/4)[J(\omega_H - \omega_N) + 3J(\omega_N) + 6J(\omega_H + \omega_N)] + c^2J(\omega_N) \quad (1)$$

$$R_2 = 1/T_2 = (d^2/8)[4J(0) + J(\omega_H - \omega_N) + 3J(\omega_N) + 6J(\omega_H) + 6J(\omega_H + \omega_N)] + (c^2/6)[4J(0) + 3J(\omega_N)] + R_{ex} \quad (2)$$

$$XNOE = 1 + (d^2/4)(\gamma_H/\gamma_N)[6J(\omega_H + \omega_N) - J(\omega_H - \omega_N)] T_1 \quad (3)$$

where  $d = (\mu_o h \gamma_N \gamma_H / 8\pi^2)(r_{NH}^{-3}),$

(Dipolar term)

$c = \omega_N(\sigma_{\parallel} - \sigma_{\perp})/\sqrt{3}.$

(Chemical shift term)

$\mu_o$  : permeability constant of free space;

h: Planck constant;

$\gamma_i$  : magnetogyric ratio of spin i;

$\omega_i$ : Larmor frequency of spin i;

$r_{NH} = 1.02 \text{ \AA}$ : length of the NH bond vector;

$R_{ex}$ : exchange rate;

$\sigma_{\parallel} - \sigma_{\perp} = -170 \text{ ppm}$  (size of the CSA tensor of the backbone amide nitrogen).

## What is $J(\omega)$ ? - Modelfree analysis

For a rigid macromolecule undergoing Brownian motion with a rotational correlation time  $\tau_m$  and local internal motion with rotational correlation time  $\tau_s$  the spectral density function,  $J(\omega)$  is given by:

$$J(\omega) = \frac{2}{5} \left[ \frac{S^2 \tau_m}{1 + (\omega \tau_m)^2} + \frac{(1 - S_f^2) \tau'_f}{1 + (\omega \tau'_f)^2} + \frac{(S_f^2 - S^2) \tau'_s}{1 + (\omega \tau'_s)^2} \right]$$

$S^2$ : Order parameters (Magnitude of motion)

$\tau$  : Correlation times (Speed of motion)

$R_{ex}$  : Chemical exchange rate (Slow motion in ms or  $\mu$ s regime)



**Fitting  $T_1$ ,  $T_2$  and NOE data to determine**

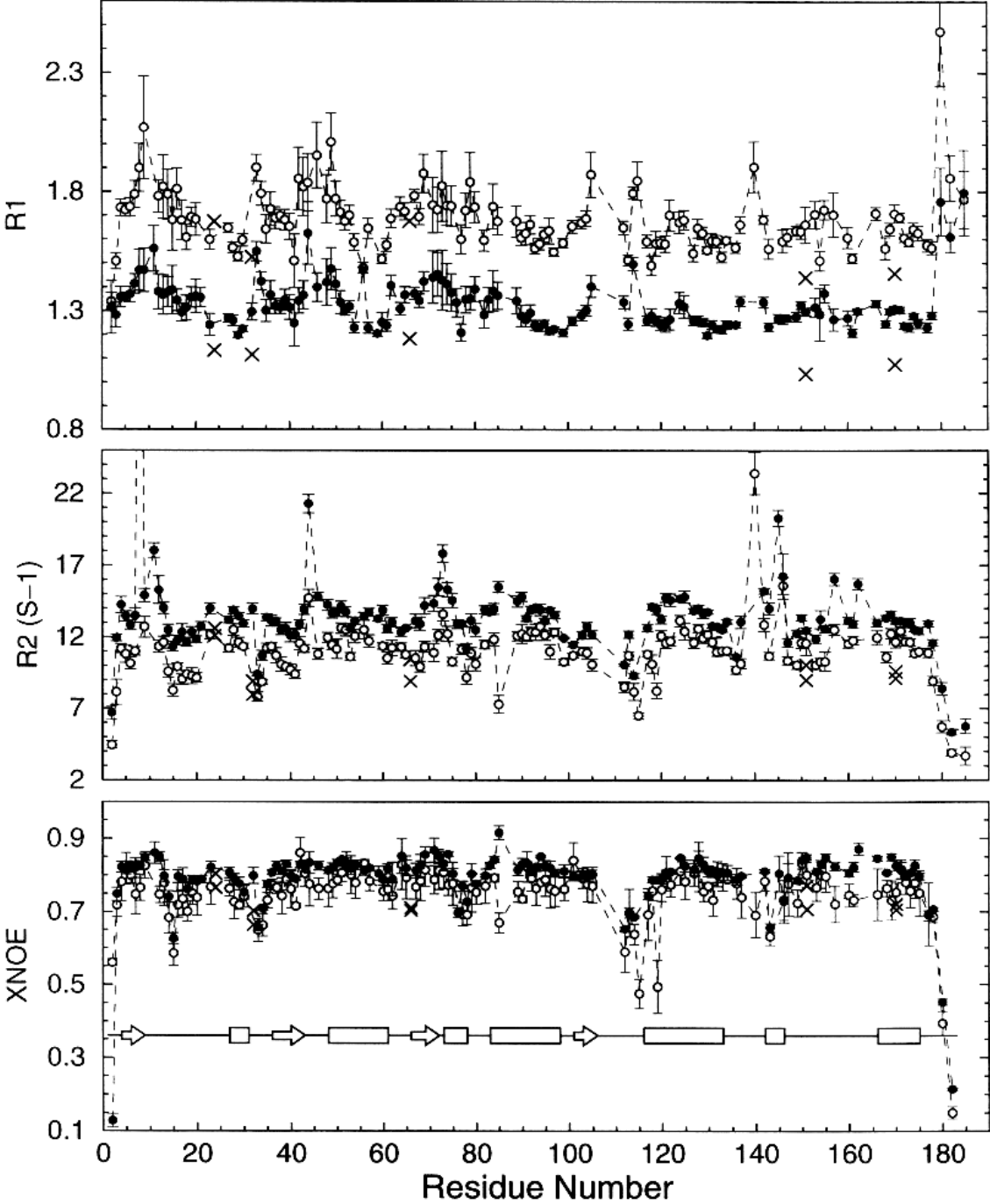
**$S^2$ ,  $\tau$  and  $R_{ex}$**

# Relaxation Data

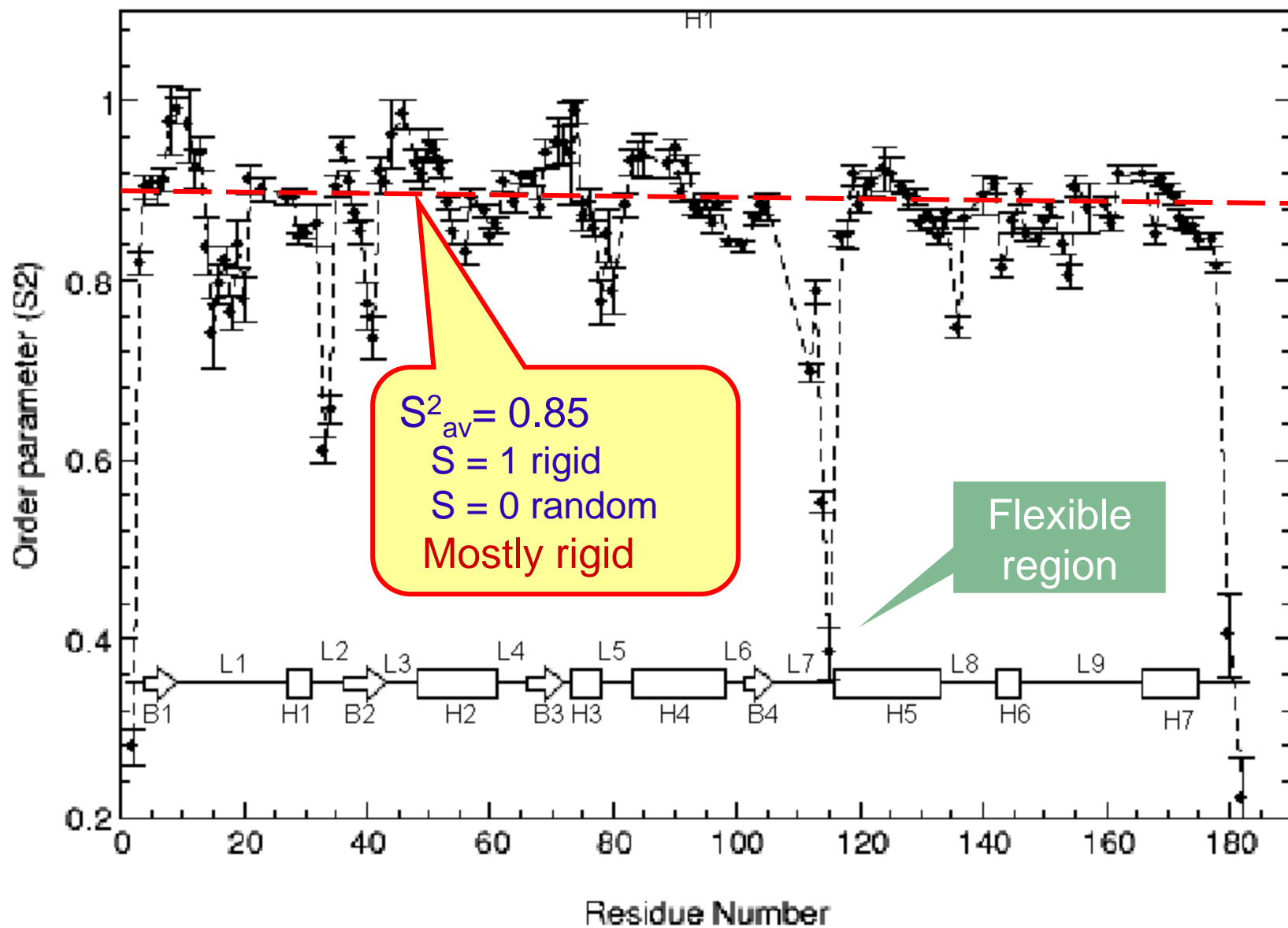
Obtained in two fields:

○ : 500 MHz

● : 600 MHz

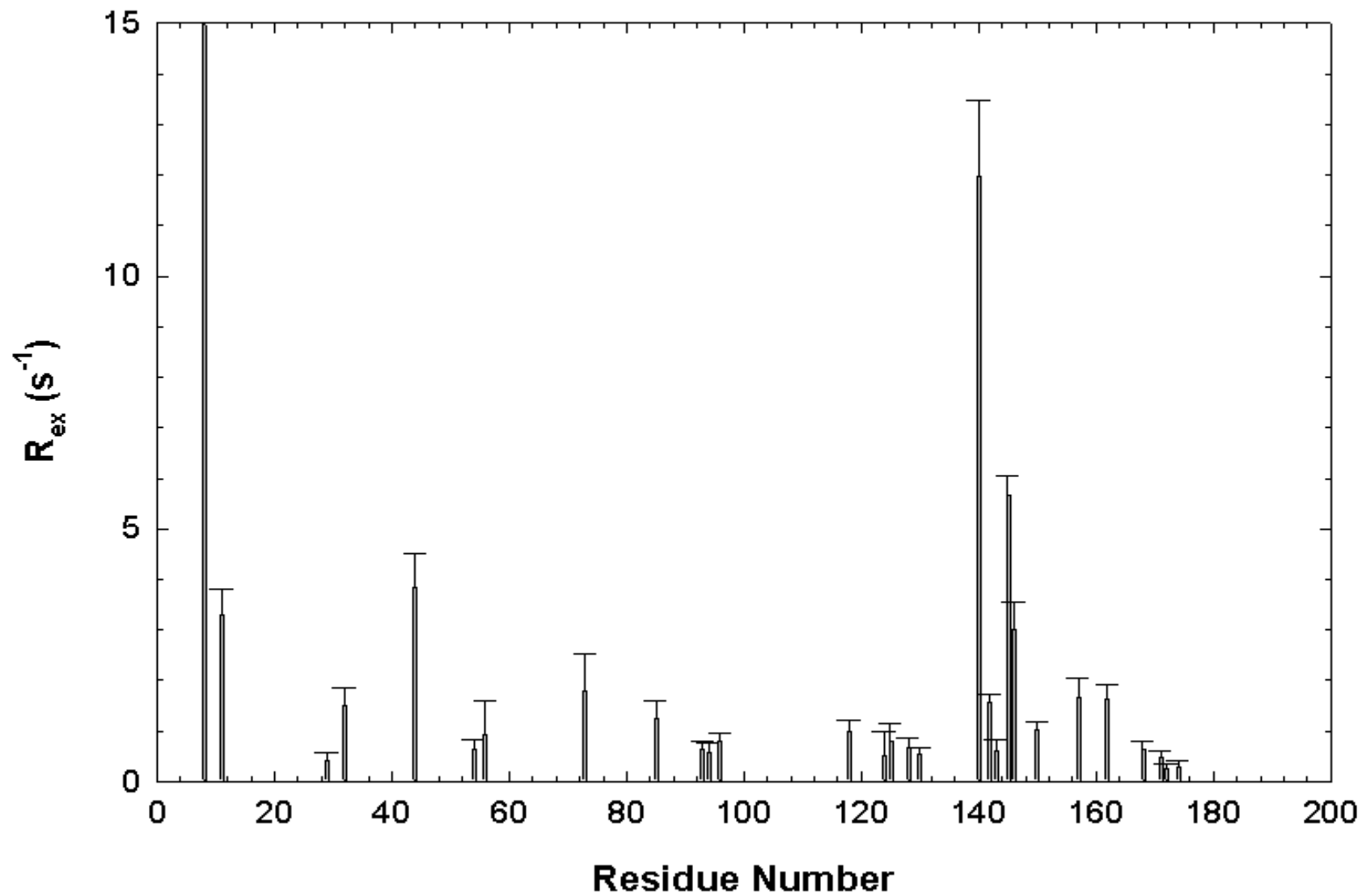


# Order parameter



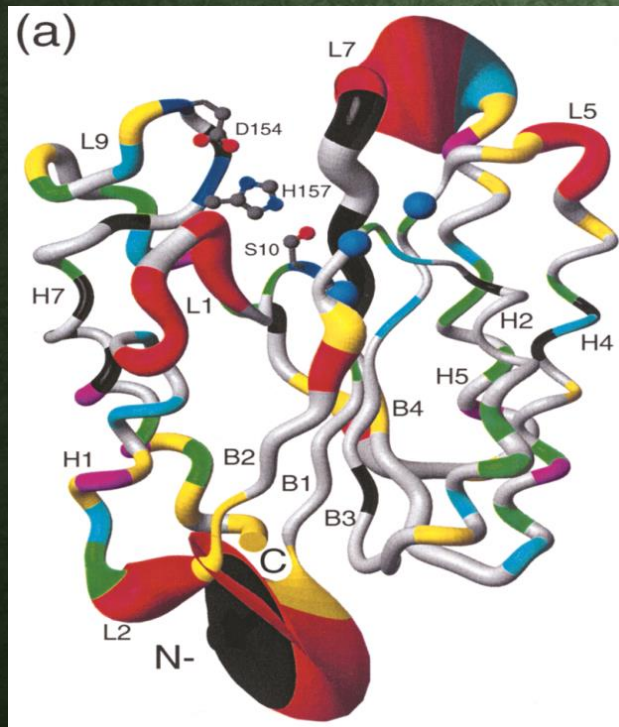


Exchange rate – Residues with low motion



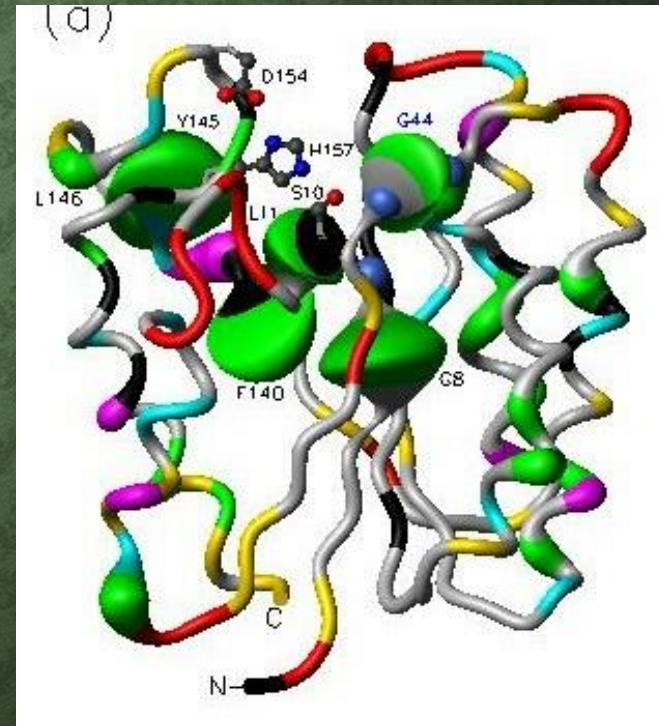
# Dynamics of E. coli Thioesterase I

## Order parameter



## Order parameter

## Slow motion



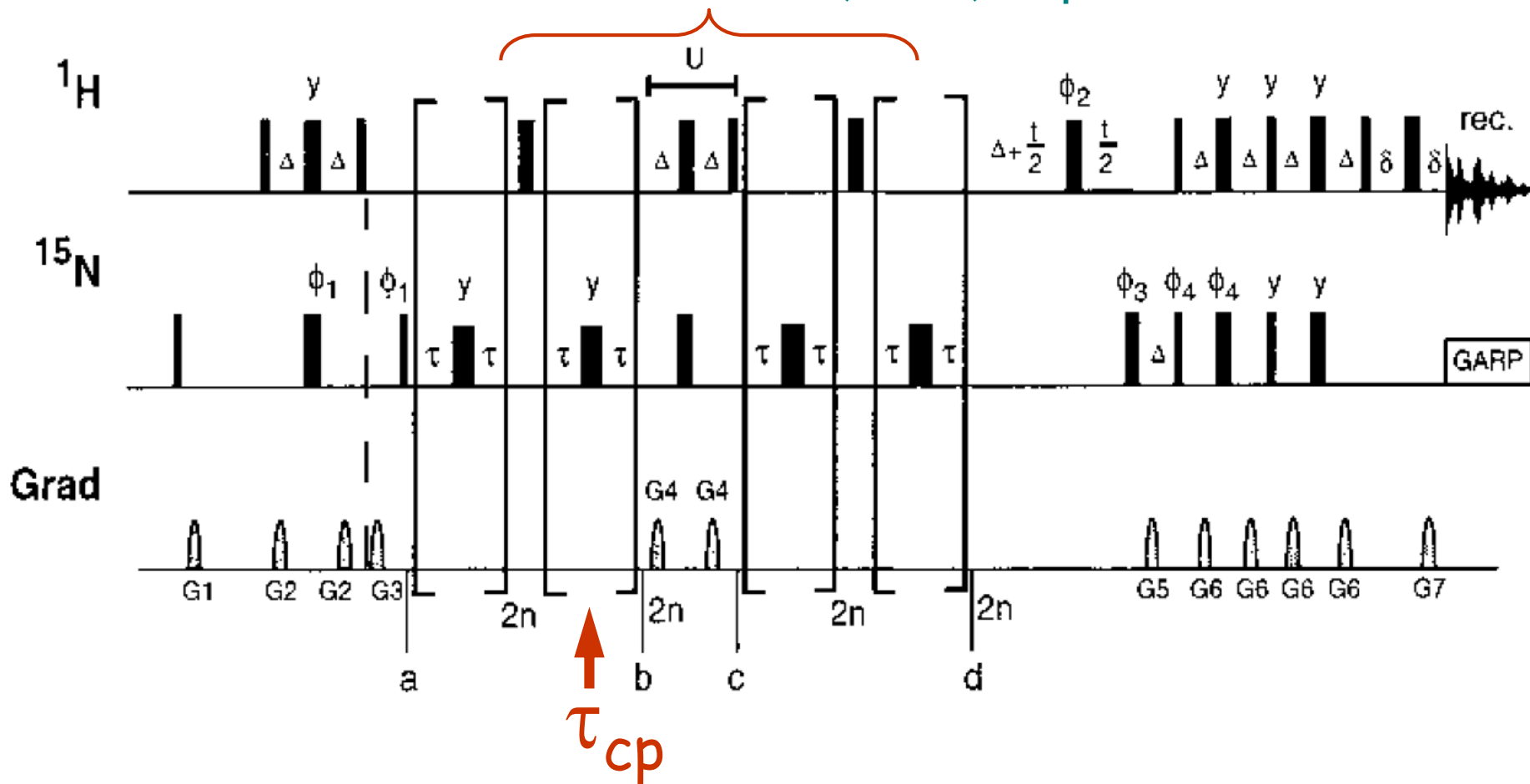
## Exchange term

Huang, et al. (2001) J. Mol. Biol. 307, 1075-1090.

# Measuring millisecond time scale motion

Ref. Loria, Rance, and Palmer III (*JACS*. 1999, *121*, 2331–2332)

## Carr–Purcell–Meiboom–Gill (CPMG) Sequence

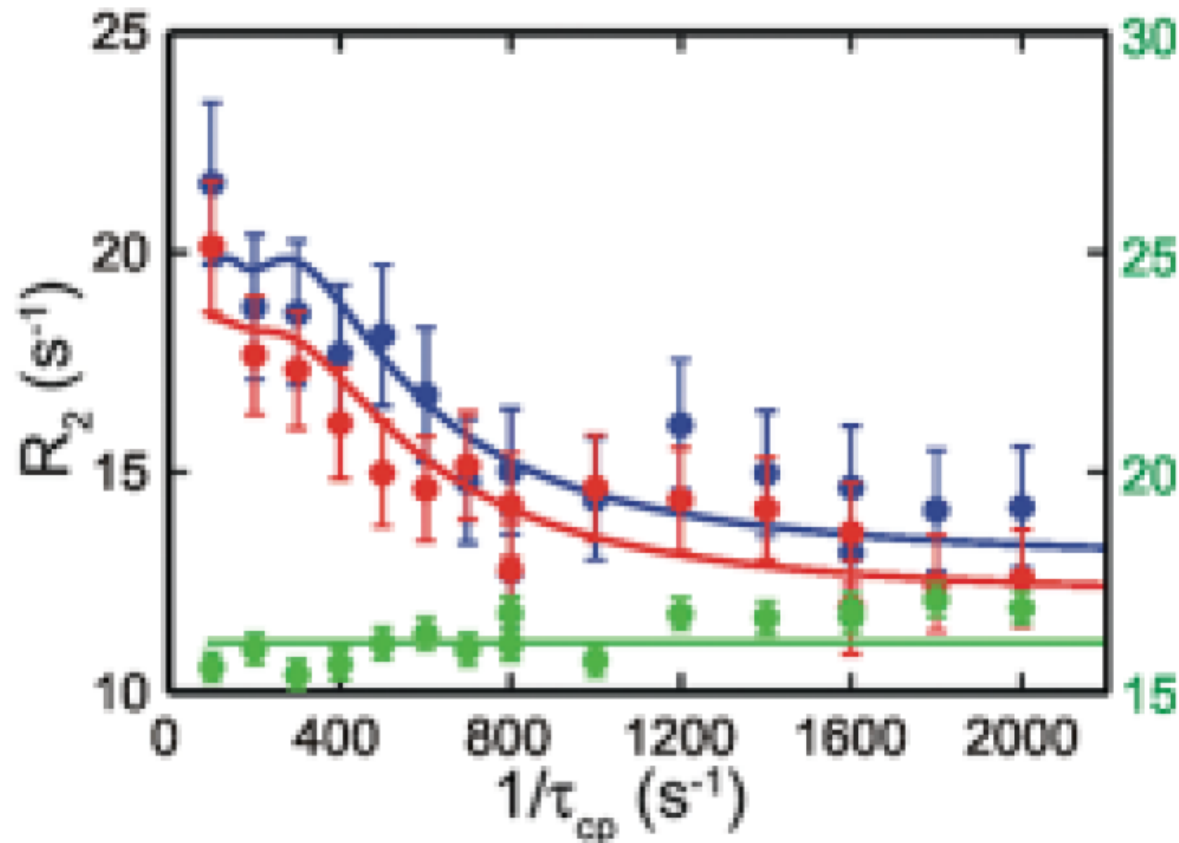


$$R_{2(\tau_{cp})} = \epsilon R_{in} + (1 - \epsilon)R_{anti} + R_{ex}$$

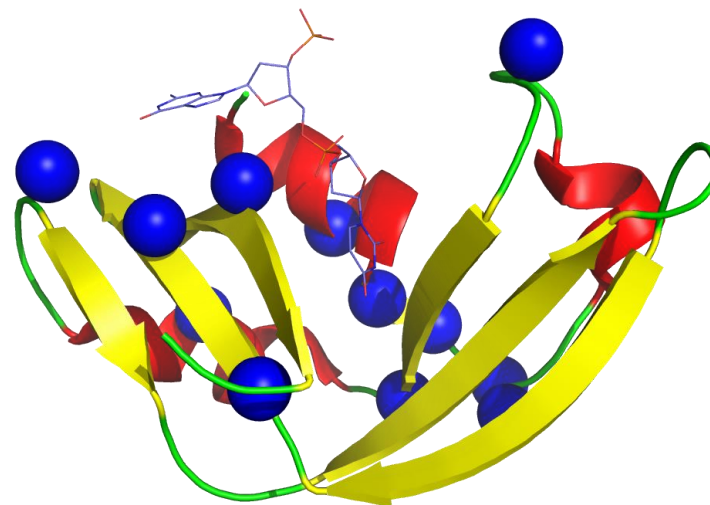
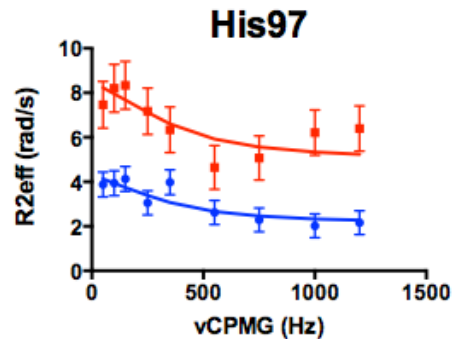
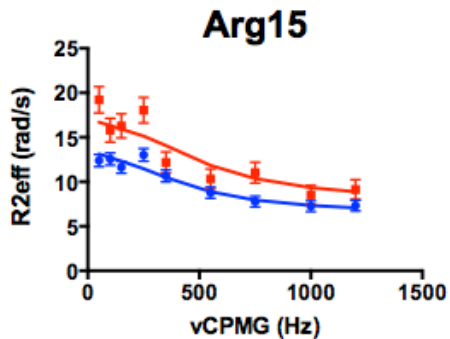
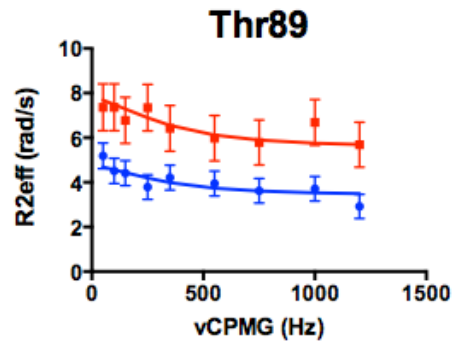
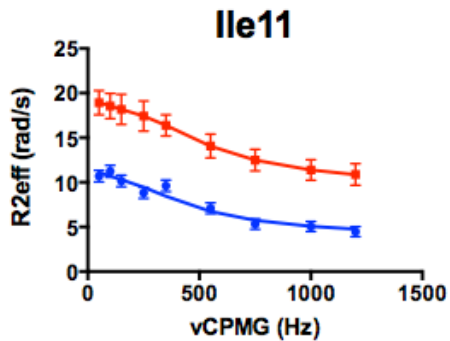
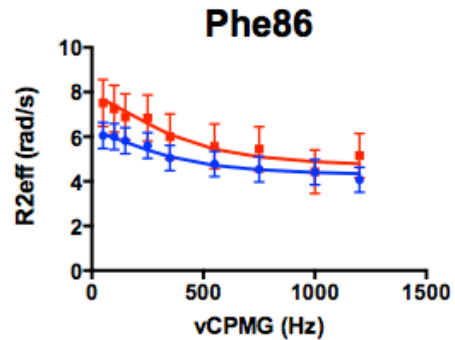
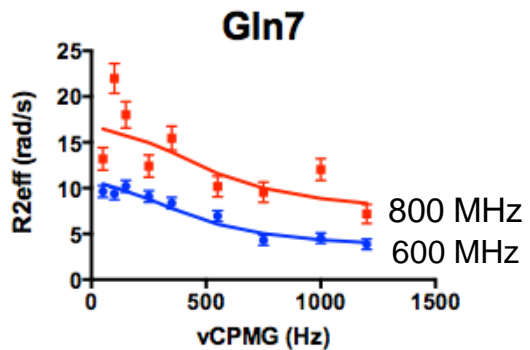
$$R_{ex} = \Phi_{ex} \tau_{ex} [1 - (2\tau_{ex}/\tau_{cp}) \tanh(\tau_{cp}/2\tau_{ex})]$$

} Solve for  $\tau_{ex}$  for different  $\tau_{cp}$   
(measure 0.5 – 5 ms range)

In which  $\Phi_{ex} = (\omega_1 - \omega_2)^2 \rho_1 \rho_2$ ;  $\rho_i$  and  $\omega_i$  are the populations and Larmor frequencies for the nuclear spin in site  $i$ , respectively; and  $\tau_{ex}$  is the lifetime of the exchanging sites.



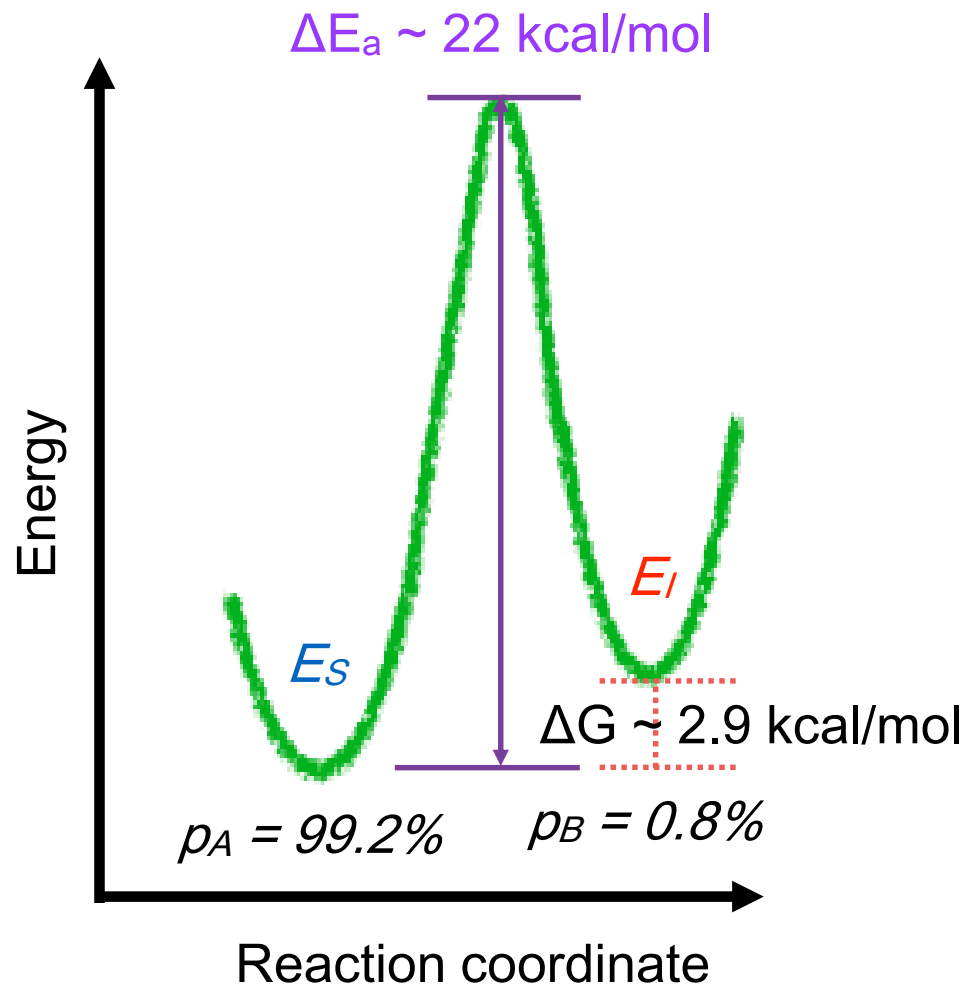
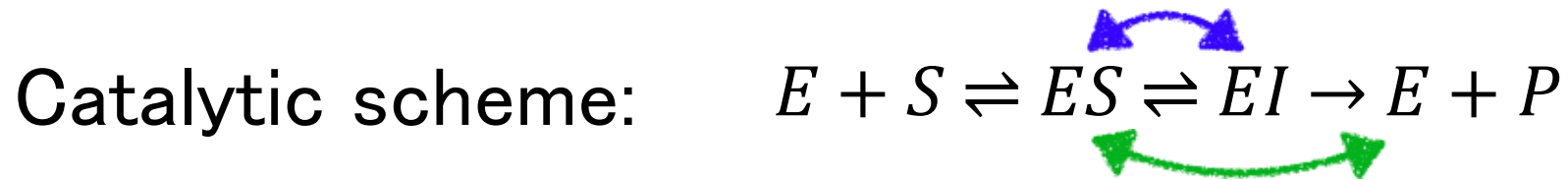
# Onconase



$$k_{ex} = 2,029 \pm 351 \text{ s}^{-1}$$

$$p_A = 99.2 \pm 0.11\%$$

$$\Delta G_{eq} \sim 2.9 \text{ kcal/mol}$$

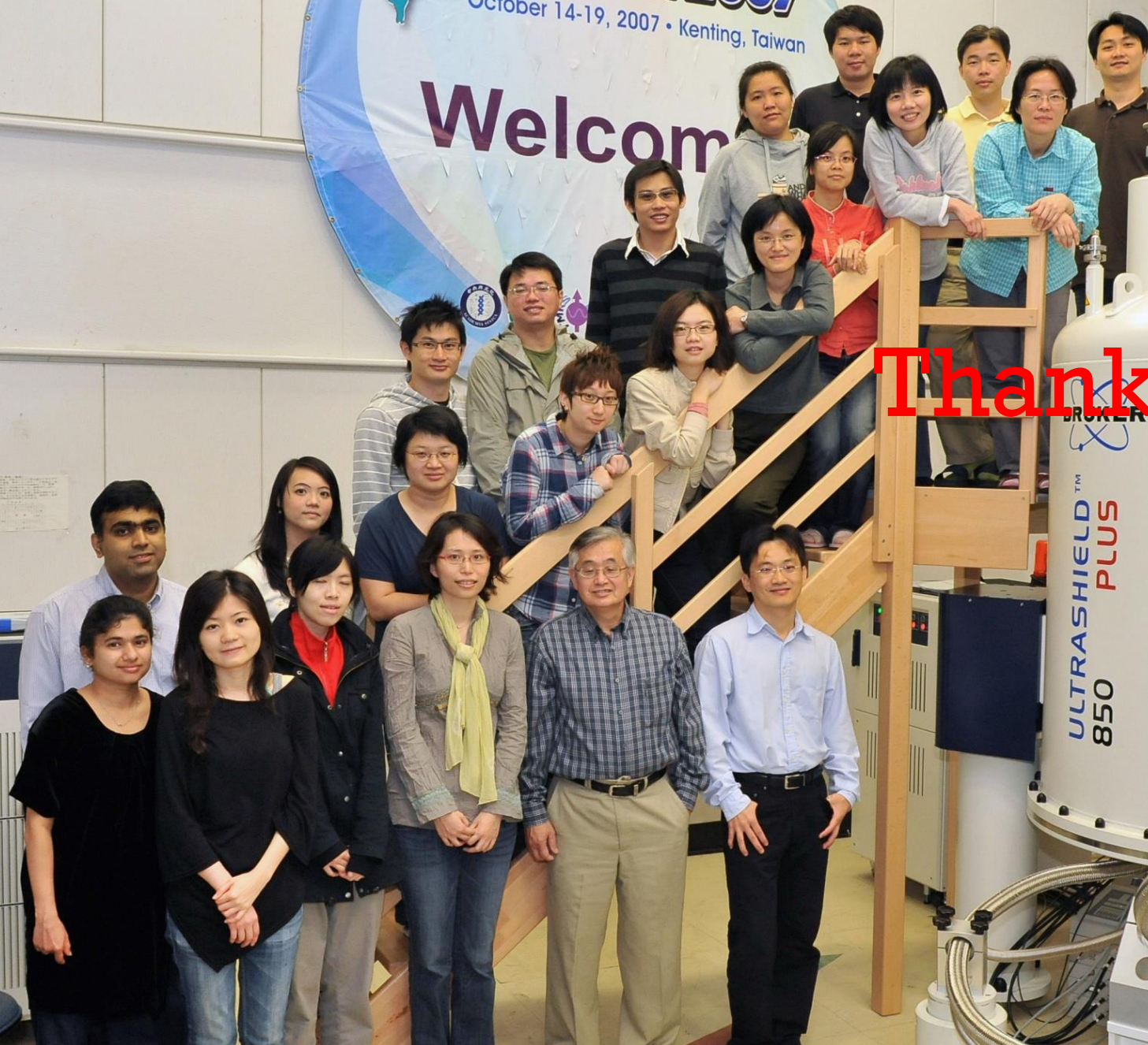




## Reflection of a Wonderful Journal

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1. NMR is a prime example of the importance of basic research. The impact of basic research often takes long time to realize.
2. Science is full of surprises. It is only limited by your imagination.  
Griffin “John Waugh basically invented the field of solid-state NMR when everyone else had left the field because they thought it was never going to work,”
3. Many areas of today’s science is inter-disciplinary in nature and a broad knowledge is essential.



Thank you!

